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AFAPL-TR-65-45 Part VIII



ROTOR-BEARING DYNAMICS DESIGN TECHNOLOGY

Part VIII: Spiral Grooved Floating Ring Journal Bearing

J. Vohr C. Chow

Mechanical Technology Incorporated

TECHNICAL REPORT AFAPL-TR-65-45, PART VIII April 1969

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Air Force Aero Propulsion Laboratory
Air Force Systems Command
Wright-Patterson Air Force Base, Ohio

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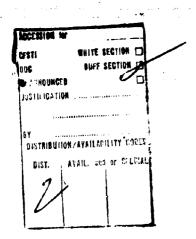
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Air Force Aero Propulsion Laboratory Air Force Systems Command Wright-Patterson Air Force Base, Ohio

FOREWORD

This report was prepared by Mechanical Technology Incorporated, 968 Albany-Shaker Road, Latham, New York 12110 under USAF Contract No. AF33(615)-3238. The contract was initiated under Project No. 3048, Task No. 304806. The work was administered under the direction of the Air Force Aero Propulsion Laboratory, with Mr. Michael R. Chasman (APFL) acting as project engineer.

This report covers work conducted from 1 May 1967 to 1 May 1968.

This report was submitted 31 July 1968. This report is Part VIII of final documentation issued in multiple parts.

This technical report has been reviewed and is approved.

Arthur V. Churchill, Chief

Fuels, Luhrication and Hazards Branch Support Technology Division Air Force Aero Propulsion Laboratory

ABSTRACT

In this volume is presented an analysis of the static and dynamic characteristics of the spiral-grooved journal bearing operating with incompressible lubricant in both laminar and turbulent regimes. Both single film and floating ring bearing configurations are considered. Extensive design data are presented giving load capacity, attitude angle, bearing torque, bearing flow rate, stiffness and damping coefficients and critical rotor mass for limit of stable operation. In addition, two computer programs accompany the volume, and instructions and listings of the programs are included. These programs may be used to obtain data for cases not covered by the presented design data.

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SYMBOLS

B _{xx} ,B _{xy} ,	Bearing damping coefficients, lb-sec/in.
^В уж ^{, В} уу	
B _{xx} ,B _{xy} B _{yx} ,B _{yy}	Dimensionless damping for overall floating ring bearing, $\overline{B}_{xx} = \frac{B_{xx}C_1}{\mu LD_1} \left(\frac{C_1}{R_1}\right) \text{etc.}$
$(\overline{B}_{xx})_1, (\overline{B}_{xy})_1$ $(\overline{B}_{yx})_1, (\overline{B}_{yy})_1$	Dimensionless damping for inner film, $(\overline{B}_{xx})_{1} = 2\pi \frac{B_{xx1}C_{1}}{\mu LD_{1}} (\overline{R}_{1})^{2} \text{ etc.}$
$(\overline{B}_{xx})_{2}, (\overline{B}_{xy})_{2}$ $(\overline{B}_{yx})_{2}, (\overline{B}_{yy})_{2}$	Dimensionless damping for outer film, $(\overline{B}_{xx})_2 = \frac{B_{xx2}C_2}{\mu LD_2} (\frac{C_2}{R_2}) \text{ etc.}$
С	Bearing mean radial clearance, in.
C D	Bearing mean radial clearance, in. Bearing diameter, in.
_	
D	Bearing diameter, in.
D e	Bearing diameter, in. Eccentricity, in.
D e F _r	Bearing diameter, in. Eccentricity, in. Radial component of bearing film force = Wcosø, lb.
D e F _r F _t	Bearing diameter, in. Eccentricity, in. Radial component of bearing film force = Wcosø, lb. Tangential component of bearing film force = Wsinø, lb.
D e Fr ft Fx,Fy	Bearing diameter, in. Eccentricity, in. Radial component of bearing film force = Wcosø, lb. Tangential component of bearing film force = Wsinø, lb. Bearing film forces in x and y directions, lb.
D e Fr ft Fx,Fy	Bearing diameter, in. Eccentricity, in. Radial component of bearing film force = Wcosø, lb. Tangential component of bearing film force = Wsinø, lb. Bearing film forces in x and y directions, lb. Dimensionless radial (cosine) component of bearing film
e Fr Ft Fx,Fy Fr	Bearing diameter, in. Eccentricity, in. Radial component of bearing film force = Wcosø, lb. Tangential component of bearing film force = Wsinø, lb. Bearing film forces in x and y directions, lb. Dimensionless radial (cosine) component of bearing film force = Wcosø $C^2/\mu(N_1+N_0)R^4$

Local film clearance, in. Local film clearance in groove region, in. Local film clearance in ridge region, in. h h' Dimensionless clearance = h/C K_{xx}, K_{xy} Bearing stiffness coefficients, lb/in. K_{vx},K_{vv} $\overline{k}_{xx}, \overline{k}_{xy}, \overline{k}_{yx}, \overline{k}_{yy}$ Dimensionless stiffness for overall floating fing bearing, $\frac{K}{K_{xx}} = \frac{\frac{K_{xx} C_1}{\mu N_1 L D_1}}{\frac{C_1}{R_1}} \cdot \frac{\frac{C_1}{R_1}}{\exp(-\frac{1}{R_1})} = etc.$ $(\overline{K}_{xx})_{1}, (\overline{K}_{xy})_{1}, (\overline{K}_{yy})_{1}$ $(\overline{K}_{yx})_{1}, (\overline{K}_{yy})_{1}$ $(\overline{K}_{xx})_{1} = \frac{K_{xx1} c_{1}}{\mu(N_{1} + N_{2})LD_{1}} (\frac{c_{1}}{R_{1}}) \quad etc.$ Bearing length, in. Length of grooved region, in. M Shaft mass, 1b. Mc Critical mass for threshold of whirl instability in floating ring bearing, 1b. Inner film critical mass. M_{c1}

Outer film critical mass.

M_{c2}

M _r	Radial component of restoring moment, in-lb.						
M _t	Tangential component of restoring moment, in-1b.						
<u>M</u> _c	Dimensionless critical mass = $\frac{\frac{M_c N_1 c_1^3}{\mu R_1^2 LD_1}}$						
H _{c1}	Dimensionless critical mass = $\frac{M_{c1}(N_1 + N_2)C_1^3}{\mu R_1^2 LD_1}$						
й _{с2}	Dimensionless critical mass = $\frac{\frac{M_{c2}N_2C_2^3}{\mu R_2^2 LD_2}}$						
	ensionless radial (cosine) component of bearing film						
	force moment = $M_r C^2/\mu(N_1 + N_0)R^5$						
M _t	Dimensionless tangential (sin) component of bearing film force moment = $M_t C^2/\mu(N_1 + N_o)R^5$						
m.	Ring mass, 1b.						
N	Speed = N ₁ + N ₂ , rps						
N ₁	Speed of journal, rps						
N ₂	Ring speed, rps						
N	Speed of inner member, rps						
N _o	Speed of outer member, rps						
n	Ring speed ratio = N_2/N_1						
P	Pressure, 1b/in ²						
P _s	Supply pressure, 1b/in ²						

P	Dimensionless pressure = $PR_1^2/\mu N_1 C_1^2$
P	Smoothed, "overall" pressure distribution around spiral
	grooved journal, lb/in ²
P _s	Dimensionless supply pressure = $P_s R_1^2 / \mu N_1 C_1^2$
P _{s1}	Dimensionless supply pressure, inner film = $P_R R_1^2 / \mu (N_1 + N_2) c_1^2$
P _{s2}	Dimensionless supply pressure, outer film = $P_g R_2^2/\mu N_2 C_2^2$
Q	Total lubricant flow rate, in 3/sec.
Q _p	Lubricant flow due to self pumping of spiral grooves, in 3/sec.
Q _s	Lubricant flow due to pressurization of supply, in 3/sec.
Q	Dimensionless total lubricant flow rate = $Q/R^2C(N_i + N_o)$
R	Bearing radius, in.
Re	Overall Reynolds number = $2\pi N_1 R_1 C_1 / \nu$
R_{h}	Local Reynolds number = $2\pi (N_i - N_o)Rh/v$
Rel	Inner film Reynolds Number = $2\pi\rho(N_0 - N_2)R_1C_1/\mu$
Re ₂	Outer film Reynolds Number = $2\pi\rho N_2 R_2 C_2/\mu$
s	Overall Sommerfeld Number = $\frac{\mu N_1 D_1 L}{W} \left(\frac{R_1}{C_1}\right)$
s ₁	Inner film Sommerfeld Number = $\frac{\mu(N_1 + N_2)D_1L}{W} \left(\frac{R_1}{C_1}\right)^2$
s ₂	Outer film Sommerfeld Number = $\frac{\mu N_2 D_2 L}{W} \left(\frac{R_2^2}{C_2}\right)$
T _B	Bearing torque, in-1b.

T _j	Journal Torque, in-1b.
T _B	Dimensionless bearing torque = T _B /WC
Ŧ,	Dimensionless journal torque = Tj/WC
t	Time, sec.
ប	Surface velocity of bearing, in/sec.
ū	Mean flow velocity in direction of rotation, in/sec.
ū _p	Mean flow velocity due to pressure gradient = u - V/2, in/sec.
v	Surface speed of journal, in/sec.
W	Bearing load, lb.
ws, wn	Mass flow components, lb/(sec-in ²)
₹ '	Mean flow velocity in axial direction, in/sec.
ж,у	Coordinates in direction of and normal to load vector, in.
- - <u> </u>	Ratio of length of grooving to total length of bearing = L_1/L
z z, z, xy,	Complex dimensionless bearing impedences
z _{yx} ,z _{yy}	
z¹	Dimensionless Z coordinate = Z/L
Greek	
α	Ratio of groove width to groove plus land width = $a_g/(a_g + a_r)$
β	Groove angle, deg. (radians in equations)
r	Ratio of groove clearance to ridge clearance = hg/hg
Υ	Misalignment angle, deg. (radians in equations)

-	Whirl frequency ratio = v/ω
E	Eccentricity ratio = e/C
η, ξ	Skewed coordinates
θ, Ζ	Cylindrical coordinates
λ	Dimensionless parameter = $\frac{\mu RL}{\pi} (C/R)^2$
μ	Viscosity, lb-sec/in ²
ν .	Kinematic viscosity, in2/sec.
ν	Whirl frequency, radians/sec.
ρ	Density, lb/in ³
	Attitude angle, deg. (radians in equations)
6'	Moment attitude angle, deg. (radians in equations)
ယ	Total rotational speed = $(\omega_1 + \omega_2)$, radians/sec.
ω ₁	Rotational speed journal, radians/sec.
ω ₂	Rotational speed ring, radians/sec.

Subscripts

Refers to inner film
Refers to outer film

INTRODUCTION

In many applications of rotating machinery it is desirable to lubricate bearings with the process fluid in order to avoid the complication of a separate lube system with accompanying seal problems. In many instances, process fluids may have low kinematic viscosities which result in operation of the bearings in the turbulent flow regime.

Bearing power loss rises rapidly with Reynolds number in turbulent film bearings. In a number of prototype systems involving rotary machines operating in the turbulent regime, the bearing power loss has been an appreciable percentage of the net system output. In addition to the effect on system efficiency, high bearing power losses mean that large quantities of lubricant must be circulated through the bearing for cooling.

A very attractive bearing for use in applications where power loss is important is the floating ring bearing. This is a journal bearing in which a loose ring is fitted between the shaft and the bearing housing. This ring is free to rotate when the journal rotates, and by so doing, can reduce the rate of shear between adjacent bearing surfaces thereby reducing power loss.

In plain bearing form, the principal disadvantage of the floating ring bearing is the rather poor stability characteristics of plain journal bearings, particularly when lightly loaded. There are a variety of configurations of journal bearings which offer improved stability over plain journal bearings. These include the tilting pad journal bearing, the Rayleigh step journal bearing, multi-lobed journal bearings, and the spiral-grooved journal bearing. Of these, the most suitable for use in a floating ring configuration is the spiral-grooved bearing. In addition to improved stability characteristics over plain bearings, the spiral-grooved bearing also has several other attractive advantages. These include the ability to self-pump lubricant axially through the bearing film and the ability to operate without cavitation at high eccentricity ratios without using a pressurized lubricant supply.

because of the potential advantages of spiral-grooved floating ring journal bearings for many applications, an analysis was performed of this bearing for both laminar and turbulent flow regimes. This analysis and the results obtained there-of form the subject of this report. Extensive performance data are presented for both floating ring and single film configuration of the spiral-grooved bearing. These data include stiffness and damping coefficients and evaluations of critical mass for fractional frequency whirl instability.

DESCRIPTION OF SINGLE FILM AND FLOATING-RING SPIRAL GROOVED JOURNAL BEARINGS

A typical spiral-grooved journal bearing is shown schematically in Fig. 1. The configuration shown is that in which the grooving on the ends of the journal tends to pump inward, thereby pressurizing the interior of the bearing. Because of the symmetry of this configuration, there is no net flow of lubricant through the bearing.

Other possible configurations for the single film spiral-grooved bearing are shown in Fig. 2. Configuration 1 is as described above. Configuration 2 is an arrangement wherein spiral grooving is inscribed on one end of the bearing in a manner so as to pump fluid exially through the bearing toward the smooth or seal end. The exial flow of lubricant can remove heat from the bearing. The flow through the bearing can be increased by pressurizing the grooved end of the bearing to a supply pressure P₈ as shown.

Configuration 3 shows a symmetrical arrangement wherein lubricant is pumped by spiral grooves outward from the center of the bearing. Lubricant may be supplied to the center of the bearing at an elevated pressure P_S. Configuration 3 consists, essentially, of two bearings of configuration 2 placed 'back to back'.

In all the configurations illustrated in Figs. 1 and 2, the spiral-grooving is shown inscribed on the journal which is considered to be the rotating member. One could, instead, inscribe the grooving on the stationary member and, for an incompressible lubricant, the performance of the bearing would be essentially the same. In this report, we shall only consider the case where the grooves are inscribed on the rotating member, this being the most common situation in practice.

The performance of a spiral-grooved bearing depends on the values of the groove parameters β (groove angle), α (ratio of groove width to total width), Γ (ratio of groove clearance to ridge clearance), and \overline{Y} (ratio of length of grooving to total length of bearing). These groove parameters are defined in Fig. 1. By a suitable choice of these parameters, one can optimize various performance characteristics of the bearing. In this report, we have chosen to present performance data for the case where the groove parameters are set at those values which yield maximum radial component of bearing stiffness at zero eccentricity.

The radial component of bearing stiffness at zero eccentricity is defined as the limiting value of W cos ϕ/e as e approaches zero where W is bearing load, as the journal displacement from the center of the bearing and ϕ is the attitude angle for the bearing (see Fig. 3). In determining the optimum values of grove parameters for maximum radial stiffness, it turned out that optimum values of α , β and Y did not vary appreciably with Reynolds number or with L/D ratio in the range $0.5 \le L/D \le 1.0$. For simplicity, therefore, a fixed set of optimum values for these parameters was settled upon as valid for all Reynolds numbers and all L/D ratios between 0.5 and 1.0. The optimum value of groove depth ratio Γ however, did vary significantly with Reynolds number. Optimum values of α , β , \overline{Y} and Γ selected for configuration 1 and configuration 2 type bearings are given in Tables 1 and 2 below.

<u>TABLE 1</u>

OPTIMUM VALUES OF GROOVE PARAMETERS SELECTED FOR CONFIGURATION 1 BEARING

Reynolds No.	α	β	Y	r	
laminar, Re < 500	0.5	151.5°	0.75	2.1	
1,000	11 -	ŧı	41	2.7	
5,000	*1	11	Ħ	3.0	
9,000	**	•	**	3.0	

TABLE 2
OPTIMUM VALUES OF GROOVE PARAMETERS SELECTED FOR CONFIGURATION 2 BEARING

Reynolds No.	α	β	¥	r	
laminar, Re < 500	0.55	149°	0.67	2.4	
1,000	**	17	11	3.1	
5,000	•	11	11	3.8	
9,000	81	11	11	3.8	

Fig. 4 shows a schematic drawing of a floating-ring bearing. A floating-ring bearing is a journal bearing in which there is a loose ring between the shart and the bearing housing. In this way, the fluid film is separated into an inner film and an outer film. The quantities connected with the inner film are identified by subscript 1, whereas subscript 2 refers to the outer film. The floating-ring bearing shown in Fig. 4 is shown with spiral-grooving on the journal and on the outer surface of the floating ring. The configuration of the grooving is such as to pump lubricant outward from the axial midplane of the bearing. Lubricant is supplied to the two lubricant films at supply pressure P via supply holes in the bearing and in the floating ring. Circumferential grooves machined at the midplane of the journal and the floating ring distribute the lubricant at uniform pressure around the journal and around the outside of the floating ring. The ring is free to rotate, and under the influence of shear stress from the revolving journal, turns at some ring speed N2 less than the speed N1 of the journal. Since in journal bearings, load capacity is essentially proportional to $(N_1 + N_2)$ whereas power loss is roughly proportional to $(N_1 - N_2)$, it follows that rotation of the ring will improve the load capacity of the inner film while reducing the power loss. This is the principle of operation of the floating ring bearing.

Calculation of the performance characteristics of the floating ring bearing requires calculation and matching of the performance characteristics of the individual lubricant films. These individual performance characteristics depend on the values selected for the groove parameters, with the possibility of having different groove parameters for the inner and outer films. For the calculations presented in this report, the groove parameters were taken to be the same for the inner and outer film and were selected to be those which provide maximum radial component of bearing stiffness for each individual bearing film. (See Table 2).

A description of the analysis of the turbulent single film and floating ring spiral-grooved journal bearings is given in the next section.

<u>ANALYSIS</u>

Analysis of the performance characteristics of the turbulent, spiral-grooved, single film and floating-ring journal bearing is based on the concept of solving for the "overall", "smoothed" pressure distribution around the bearing, neglecting the local zig-zag details of the pressure profiles which arise due to the discontinuous groove-ridge geometry. The theoretical basis for this analytical approach is discussed in detail in Reference 1. Essentially, this analytical approach is valid in the limit as the number of grooves approaches an infinite number, but practically speaking, the analysis proves to be quite accurate when applied to bearings having a reasonable number of grooves. Experimental verification of this analytical approach has been provided by a number of investigations (References 2 and 3).

The differential equation that had been derived in Reference 1 for the smoothed, overall pressure distribution around a spiral-grooved journal bearing was rederived in the present study to take account of the effects of turbulence in the bearing film. This derivation is presented in Appendix 1. The effects of turbulence in the bearing film are accounted for by means of the linearized turbulent lubrication theory developed by Ng and Pan (Reference 4). In this theory, which is based on the concept of a turbulent eddy viscosity, there are developed turbulent flow correction factors G_{x} and G_{y} which relate the mean pressure flow in the direction of rotation (x direction) and the axial direction (x direction) to the pressure gradients in these respective directions. The relationships developed are

$$\frac{1}{u_p} = -\frac{h^2}{\mu} G_{x} \frac{\partial P}{\partial x} \tag{1}$$

$$\overline{w} = -\frac{h^2}{\mu} G_z \frac{\partial P}{\partial z}$$
 (2)

where

 $u_p = u - \frac{v}{2}$ = the mean flow velocity in the x direction minus 1/2 the surface velocity of rotation

w = the mean flow velocity in the axial direction

h = local film clearance

 μ = viscosity

In the generalized theory for turbulent fluid films developed by Elrod, Ng and Pan (Reference 5), $G_{\rm x}$ and $G_{\rm g}$ are functions of the pressure gradient in the film, the angle between the pressure gradient and the direction of rotation, and the Reynolds number based on rotational velocity. In the linearized theory of Ng and Pan, $G_{\rm x}$ and $G_{\rm z}$ are functions only of the local Reynolds number $R_{\rm h}=\rho V h/\mu$. Values of $G_{\rm x}$ and $G_{\rm z}$, plotted as a function of $R_{\rm h}$, are shown in Figure 5.

A discussion of the theoretical basis of the linearized theory of turbulence is beyond the scope of this present report. For such a discussion, the reader can consult Reference 4. In this report, we have simply applied the results of this theory to derive the differential equation for a spiral-grooved journal bearing with turbulent, incompressible lubricant. This differential equation, obtained in Appendix I, is given below in dimensionless form.

$$\frac{\partial w^{\frac{1}{2}}}{\partial \theta} + \frac{\cos \beta}{R} \frac{\partial w^{\eta}}{\partial \theta} + \sin \beta \frac{\partial w^{\eta}}{\partial z}$$

$$+ \left(\frac{\partial}{\partial t} + \frac{V}{R} \frac{\partial}{\partial \theta} \right) \left(R \rho \sin \beta \left[\alpha h_g + (1-\alpha)h_r \right] \right) = 0$$
 (3)

where

$$W^{\xi} = R \sin \beta \left\{ -\frac{\rho}{12\mu} h_{r}^{3} \left[G_{1r} \left(\overline{A}_{2} \frac{\partial \overline{P}}{\partial \xi} - \alpha \overline{B}_{1} \frac{\partial \overline{P}}{\partial \eta} - \alpha \overline{B}_{2} \right) + G_{2r} \frac{\partial \overline{P}}{\partial \eta} \right] + \rho h_{r} \frac{(U-V)}{2R} \right\}$$

$$W^{\eta} = R \sin \beta \frac{\rho}{12\mu} \left\{ \alpha h_g^3 \left[G_{3g} \frac{\partial \overline{P}}{\partial \eta} + G_{2g} (\overline{A}_2 \frac{\partial \overline{P}}{\partial \xi} - \alpha \overline{B}_1 \frac{\partial \overline{P}}{\partial \eta} - \alpha \overline{B}_2) \right] + (1-\alpha)h_r^3 \left[G_{3r} \frac{\partial \overline{P}}{\partial \eta} + G_{2r} (\overline{A}_2 \frac{\partial \overline{P}}{\partial \xi} - \alpha \overline{B}_1 \frac{\partial \overline{P}}{\partial \eta} - \alpha \overline{B}_2) \right] \right\}$$

$$\frac{\partial \overline{P}}{\partial \eta} = \frac{\partial \overline{P}}{\partial \theta} \frac{\cos \beta}{R} + \frac{\partial \overline{P}}{\partial z} \sin \beta$$

$$\frac{\partial \overline{b}}{\partial \overline{b}} = \frac{\partial \overline{b}}{\partial \overline{b}}$$

$$A_1 = G_{1r} h_r^3$$

$$A_2 = -G_{1g} h_g^3$$

$$A_3 = A_2 - \alpha(A_2 + A_1)$$

$$B_1 = G_{2g} h_g^3 - G_{2r} h_r^3$$

$$B_{2} = \frac{6\mu(h_{x} - h_{x})}{R} \quad (U-V)$$

$$\overline{A}_{1} = A_{1}/A_{3}$$

$$\overline{A}_{2} = A_{2}/A_{3}$$

$$\overline{B}_{1} = B_{1}/A_{3}$$

$$\overline{B}_{2} = B_{2}/A_{3}$$

and where G_{1r} , G_{1g} , G_{2r} , G_{2g} , etc. are lumped, turbulent flow correction factors defined by Eqs. (65),(66) and (67) in Appendix I.

Eq. (3) was solved numerically on a digital computer using the method of columnwise influence coefficients developed by Castelli and Shapiro (Ref. 6) and Castelli and Pirvic. (Ref. 7). Two separate computer programs were developed, one to obtain results for the static and dynamic characteristics of a single film spiral-grooved bearing, and the second to calculate the overall static performance characteristics of a spiral-grooved floating-ring bearing.

Calculation of Performance of Single Film, Spiral-Grouved Journa! Bearing

The computer program for calculating the performance characteristics of a single-film spiral-grooved journal bearing requires that the following quantities be specified. (Symbols are defined in the nomenclature).

Reynolds number based on mean radial clearance in the seal region of the bearing = $\frac{2\pi\rho(N_i - N_i)RC}{u}$

L/D ratio C/R ratio

Dimensionless pressure at both ends of the bearing =
$$\frac{p}{\mu(N_1 + N_0)}$$
 (2)

Speed ratio factor =
$$\frac{N_o - N_i}{N_i + N_o}$$

Dimensionless rate of change of eccentricity ratio = $\frac{\partial \epsilon}{\partial t}/2\pi(N_1 + N_0)$

Dimensionless whirl speed ratio = $\frac{\partial \dot{p}}{\partial t}/2\pi(N_1 + N_0)$

Dimensionless rate of change of misslignment angle = $\frac{\partial y}{\partial t}/2\pi(N_1 + N_0)$

Eccentricity ratio, &

Angle of misalignment, γ

Groove geometry parameters α , β , Γ , \overline{Y}

In addition, one must specify whether the bearing is of configuration 1 or configuration 2 (see Fig. 2). Subject to the above input conditions, Eq. (3) is solved by the computer program to determine the dimensionless pressure distribution \overline{P} . From this pressure distribution, the computer program then determines the following performance characteristics of the bearing.

Dimensionless tangential (sin) component of bearing film force,

$$\overline{F}_{t} = \frac{W \sin \phi}{\mu (N_{i} + N_{o})R^{2}} \left(\frac{C}{R}\right)^{2} \quad \text{(see Fig. 3)}$$

Dimensionless radial (cos) component of bearing film force,

$$\overline{F}_{r} = \frac{W \cos \phi}{\mu (N_{i} + N_{o})R^{2}} \left(\frac{C}{R}\right)^{2} \quad \text{(see Fig. 3)}$$

Dimensionless tangential (sin) component of the moment exerted by the bearing film force about an axis through the initial end of the bearing

$$\widetilde{M}_{c} = \frac{M \sin \delta}{\mu (N_{c} + N_{c})R^{3}} \left(\frac{c}{R}\right)^{2}$$

Dimensionless radial component of the moment swarted by the bearing film force about an axis through the initial end of the bearing,

$$\overline{M}_{r} = \frac{H \cos \phi}{\mu (N_1 + N_0)R^3} \left(\frac{G}{R}\right)^2$$

Dimensionless flow through the journal,
$$\overline{Q} = \frac{Q}{R^2 C(N_1 + N_0)}$$

Dimensionless bearing torque,
$$\overline{T}_{B} = \frac{T_{B}}{WC}$$

Dimensionless journal torque,
$$T_j = \frac{T_j}{WC}$$

The problem of cavitation of the bearing film is handled by the approximate method of setting all sub-ambient fluid film pressure equal to zero before integrating for loads and flows. Experience with plain journal bearings indicates that this approach yields values for load which are on the order of 5% to 10% conservative when compared to a more exact treatment (Ref. 8). For spiral-grooved bearings, the extent of cavitation is much less than for plain bearings. Thus, one would expect that the error introduced by the approximate method of handling cavitation would not be significant in the case of spiral-grooved bearings.

In the calculation of bearing torque, it is assumed that regions of subambient pressure are cavitated and therefore do not contribute to the shear stress on the journal or bearing.

The program for the single film bearing calculates values of the radial and tangential components of fluid film force $F_{\rm r}$ and $F_{\rm t}$ as functions of the steady state eccentricity of the journal, e, the instantaneous rate of change of eccentricity of the journal, $\partial e/\partial t$, and the instantaneous whirl velocity of the journal $\partial \phi/\partial t$. Let us now see how this program may be used to obtain

stiffness and damping coefficients for the bearing. Consider the reference axes x and y shown in Fig. 3 where x is taken as the direction of the steady state load, W, and y is normal to this. The stiffness and damping coefficients are defined by

$$dF_{x} = -K_{xx} \times -B_{xx} \frac{\partial x}{\partial t} - K_{xy} = -B_{xy} \frac{\partial y}{\partial t}$$
 (4)

$$dF_{y} = -K_{yx} x - B_{yx} \frac{\partial x}{\partial t} - k_{yy} y - B_{yy} \frac{\partial y}{\partial t}$$
 (5)

It is shown in Appendix II that for bearings possessing rotational symmetry, $K_{\chi\chi}$, $K_{\chi\chi}$ etc. may be determined from derivatives of F_{r} and F_{t} with respect to e and è by means of the following expressions

$$K_{xx} = \frac{\partial F_{x}}{\partial e} \cos^{2} \phi + \frac{\partial F_{t}}{\partial e} \cos \phi \sin \phi$$
 (6)

$$B_{KK} = \frac{\partial F_{r}}{\partial \dot{e}} \cos^{2} \phi + \frac{\partial F_{t}}{\partial \dot{e}} \cos \phi \sin \phi - \frac{\sin \phi}{e} \left[\cos \phi \frac{\partial F_{r}}{\partial \dot{\phi}} + \sin \phi \frac{\partial F_{t}}{\partial \dot{\phi}} \right]$$
 (7)

$$K_{xy} = \frac{\partial F_t}{\partial e} \sin^2 \phi + \frac{\partial F_r}{\partial e} \cos \phi \sin \phi$$
 (8)

$$B_{xy} = \frac{\partial F_t}{\partial \dot{e}} \sin^2 \phi + \frac{\partial F_x}{\partial \dot{e}} \cos \phi \sin \phi + \frac{\cos \phi}{e} \left[\cos \phi \frac{\partial F_x}{\partial \dot{\phi}} + \sin \phi \frac{\partial F_t}{\partial \dot{\phi}} \right]$$
 (9)

$$K_{VX} = -\frac{\partial F_{L}}{\partial e} \cos^{2} \phi + \frac{\partial F_{L}}{\partial e} \cos \phi \sin \phi - \frac{W}{e} \sin \phi \qquad (10)$$

$$B_{yx} = -\frac{\partial F_t}{\partial \dot{e}} \cos^2 \phi + \frac{\partial F_x}{\partial \dot{e}} \cos \phi \sin \phi - \frac{\sin \phi}{e} \left[\sin \phi \frac{\partial F_x}{\partial \dot{\phi}} - \cos \phi \frac{\partial F_t}{\partial \dot{\phi}} \right]$$
(11)

$$K_{yy} = \frac{\partial F_{r}}{\partial e} \sin^{2} \phi - \frac{\partial F_{t}}{\partial e} \cos \phi \sin \phi + \frac{W}{e} \cos \phi$$
 (12)

$$B_{yy} = \frac{\partial F_{x}}{\partial \dot{e}} \sin^{2} \phi - \frac{\partial F_{t}}{\partial \dot{e}} \cos \phi \sin \phi + \frac{\cos \phi}{e} \left[\sin \phi \frac{\partial F_{x}}{\partial \dot{\phi}} - \cos \phi \frac{\partial F_{t}}{\partial \dot{\phi}} \right]$$
(13)

where $\dot{e} = \frac{\partial e}{\partial t}$ is the instantaneous rate of change of eccentricity and $\ddot{\theta} = \frac{\lambda \dot{d}}{\partial t}$ is the whirl velocity of the journal.

The determination of the derivatives $\partial F_r/\partial e$, $\partial F_r/\partial e$ etc. from the single film program is tedious but essentially straight forward. Care must be taken, however, that the changes in e, \dot{e} and $\dot{\phi}$ used to evaluate these derivatives be chosen sufficiently small such that the results accurately apply to infinitesimally small amplitude motions of the journal center about a steady state position*. It is recommended that one keep $\Delta e/C < .05$, $\Delta \dot{e}/2\pi(N_1 + N_0)C < .05$ and $e\ddot{\phi}/2\pi(N_1 + F_0)C$ < .05 for evaluation of the above mentioned derivatives.

A detailed description of how to prepare input for the single film spiral-grooved journal bearing program is given in Appendix III together with a listing of the program.

Calculation of Steady State Performance of Floating Ring Bearing

The program for calculating the performance of a floating ring, spiral-grooved bearing consists, essentially, of two parts. The first part contains the program for a single film, spiral grooved journal bearing described above. This is used to calculate the individual performance characteristics of the inner and outer films of the floating ring bearing. The second part of the program consists of the logic required to determine the correct ring speed and eccentricity ratio of the outer film such that the load capacity of the outer film is equal to the load capacity of the inner film and the torque exerted by fluid shear stresses on the

The linear formulation represented by Eqs. (4) and (5) implicitly carries the assumption that the motions x, y, $\partial x/\partial t$, $\partial y/\partial t$ are vanishingly small.

inner surface of the ring is balanced by the fluid snear stresses on the outer surface of the ring. In detail, the computational procedure works as described below

1. To determine the overall preformance of the floating ring bearing requires that the following quantities be specified as input to the program.

Radius ratio of ring and journal = R_2/R_1 where R_2 is the outside radius of the ring and R_1 is the radius of the journal.

Overall Reynolds number under which the bearing is to be operated Re = $2\pi\rho N_1 R_1 C_1/\mu$

Eccentricity ratio of inner film to be examined = ϵ_1

Clearance to radius ratio for inner film = C_1/R_1

Clearance to radius ratio for outer film = C_2/R_2

Dimensionless supply pressure to center of bearing = $(P_s/\mu N_1)$ $(C_1/R_1)^2$

Length to inner diameter ratio for bearing = L/D_1

Groove geometry parameters α , β , Γ and \overline{Y}

2. Given this input, the first thing the program does is to calculate and store in tabular form the following performance data for the inner and outer films of the floating ring bearing.

Sommerfeld No.
$$S_1 = \frac{\mu(N_1 + N_2)D_1L}{W} \cdot \left(\frac{R_1}{C_1}\right)^2$$

Dimensionless torque on journal $(\overline{T}_j)_1 = \frac{(T_j)_1}{WC_1}$

Dimensionless torque on inside of ring
$$(\overline{T}_B)_1 = \frac{(T_B)_1}{WC_1}$$

Attitude angle 61

Outer film

Sommerfeld No.
$$s_2 = \frac{\mu N_2 D_2 L}{W} \left(\frac{R_2}{C_2}\right)^2$$

Dimensionless torque on outside of ring
$$(\overline{T}_j)_2 = \frac{(T_j)_2}{WC_2}$$

Dimensionless torque on inside of bearing
$$(\overline{T}_B)_2 = \frac{(T_B)_2}{WC_2}$$

Attitude angle 62

These performance data are stored in tables as functions of the eccentricity ratio and Reynolds number for the film concerned. Values are calculated for three predetermined values of eccentricity ratio and three predetermined values of Reynolds number. Thus, 9 separate calculations of performance characteristics must be made for each film (18 calculations altogether). The Reynolds number for the inner film is defined as

$$Re_{1} = \frac{2\pi\rho(N_{1} - N_{2})R_{1}C_{1}}{\mu}$$
 (14)

while the Reynolds number for the outer film is defined as

$$Re_2 = \frac{2\pi\rho N_2 R_2 C_2}{\mu} \tag{15}$$

Note that since the overall Reynolds number Re is specified, Re $_1$ and Re $_2$ are determined uniquely by the ring speed ratio N_2/N_1 . Typically, the three values of Re $_1$ and Re $_2$ for which film characteristics are calculated are those corresponding to $N_2/N_1 = 0.25$, 0.35 and 0.45. Typical values of eccentricity ratio for which the inner film characteristics are determined are $\epsilon_1 = 0.2$, 0.3 and 0.5. The three values of ϵ_2 selected for calculation of outer film data are chosen in accordance with anticipated operating eccentricities of the outer film.

- 3. Once the tables of inner and outer film characteristics are prepared, the program next considers an initial guess for the ring speed ratio N_2/N_1 . This initial guess is read in as input to the program. From this ring speed ratio, the program then calculates a value for Re_1 . Corresponding to this value for Re_1 , and the value of ϵ_1 read into the program, there will be specific values of S_1 and $(\overline{T}_B)_1$ which the program will determine from the tabular data for the inner film characteristics. The program will interpolate within the tables if necessary.
- 4. The program next determines S₂ from the condition that the load capacities of the inner and outer film must be equal. This condition is expressed by

$$s_2 = s_1 \left(\frac{N_2}{N_1 + N_2}\right) \frac{R_2}{R_1} \left(\frac{R_2}{C_2}\right)^2 \left(\frac{C_1}{R_1}\right)^2$$
 (16)

The program also determines Re_2 corresponding to the guessed value of ring speed ratio.

5. With \mathbf{S}_2 and \mathbf{Re}_2 calculated, the program next determines the corresponding values of, $(\mathbf{T}_j)_2$ and \mathbf{e}_2 from the tabular data for the outer film performance characteristics. The program then checks to see if

$$(\overline{T}_1)_2 - (\overline{T}_2)_1 \frac{c_1}{c_2} \tag{17}$$

i.e. the program checks to see if the torque on the outside of the floating ring matches the torque on the inside. If they match, the solution is complete. If the torque on the outside of the ring is lower (higher), then a slightly higher (lower) value for ring speed is guessed and the process is repeated until a convergent solution is obtained.

When a convergent solution is obtained for the floating ring bearing, the program prints out various performance data for the individual films and for the overall floating ring bearing. This output is described fully in Appendix IV. Detailed instructions for preparing the input for the floating ring program are also provided in this appendix along with a listing of the program.

Stiffness and Bemping Coefficients for Floating Ring Bearing

In order to determine the overall stiffness and damping coefficients for the floating ring bearing, it is necessary to first determine the stiffness and damping coefficients for each individual bearing film. For each steady state solution for the floating ring bearing, the steady state operating conditions for each film are established. Stiffness and damping coefficients for each film can therefore be determined by the single-film, spiral-grooved journal bearing program as described earlier.

Let us denote the stiffness and damping coefficients for the inner film by the subscript 1 and those for the outer film by the subscript 2, i.e., K_{xx1} , K_{xx2} , etc. The overall stiffness and damping coefficients for the floating ring bearing are denoted simply as K_{xx} , K_{xy} , etc. Consider that the shaft moves in sychronous whirl with a frequency $\omega_1 = 2\pi N_1$ radians/sec. and with amplitude components $\overline{\kappa_1} e^{\frac{i\omega_1}{2}t}$. The overall damping and stiffness coefficients are defined by the rollowing relationships.

$$\frac{\mathbf{r} e^{i\omega_1 t}}{\mathbf{w}} = -\left(\frac{\mathbf{c}_1 \mathbf{x}_{xx}}{\mathbf{w}} + \frac{\mathbf{c}_1 \omega_1 \mathbf{s}_{xx}}{\mathbf{w}}\right) \frac{\mathbf{x}_1}{\mathbf{c}_1} e^{i\omega_1 t} - \left(\frac{\mathbf{c}_1 \mathbf{x}_{xy}}{\mathbf{w}} + \frac{\mathbf{c}_1 \omega_1 \mathbf{s}_{xy}}{\mathbf{w}}\right) \frac{\mathbf{y}_1}{\mathbf{c}_1} e^{i\omega_1 t}$$
(18)

$$\frac{\mathbf{r}_{\mathbf{v}}\mathbf{c}^{i\omega_{1}t}}{\mathbf{w}} = -\left(\frac{\mathbf{c}_{1}\mathbf{x}_{\mathbf{y}\mathbf{x}}}{\mathbf{w}} + i\frac{\mathbf{c}_{1}\omega_{1}\mathbf{s}_{\mathbf{y}\mathbf{x}}}{\mathbf{w}}\right)\frac{\mathbf{x}_{1}}{\mathbf{c}_{1}}e^{i\omega_{1}t} - \left(\frac{\mathbf{c}_{1}\mathbf{x}_{\mathbf{y}\mathbf{y}}}{\mathbf{w}} + i\frac{\mathbf{c}_{1}\omega_{1}\mathbf{s}_{\mathbf{y}\mathbf{y}}}{\mathbf{w}}\right)\frac{\mathbf{y}_{1}}{\mathbf{c}_{1}}e^{i\omega_{1}t}$$
(19)

or in short:

$$\left\{\begin{array}{c}
\frac{\mathbf{r}}{\mathbf{x}} \\
\frac{\mathbf{r}}{\mathbf{y}}
\end{array}\right\} = \left\{\begin{array}{c}
\mathbf{z}_{\mathbf{x}\mathbf{x}} & \mathbf{z}_{\mathbf{y}\mathbf{y}} \\
\mathbf{z}_{\mathbf{y}\mathbf{x}} & \mathbf{z}_{\mathbf{y}\mathbf{y}}
\end{array}\right\} \left\{\begin{array}{c}
\mathbf{x}_{1} \\
\mathbf{y}_{1}
\end{array}\right\}$$
(20)

where:

$$z_{xx} = \frac{c_1 k_{xx}}{y} + i \frac{c_1 \omega_1 B_{xx}}{y} \quad \text{(analogous for } z_{xy}, z_{yx}, z_{yy}) \quad (21)$$

$$x_1 = \frac{\overline{x_1}}{\overline{c_1}} \tag{22}$$

$$y_1 = \frac{\overline{y}_1}{\overline{c}_1} \tag{23}$$

Let the center of the ring have whirl amplitudes $x_2e^{i\omega_1t}$ and $y_2e^{i\omega_1t}$ and let:

$$x_2 = \frac{\overline{x_2}}{\overline{c_1}} \tag{24}$$

$$y_2 = \frac{\overline{y}_2}{c_1}$$
 (25)

The dimensionless dynamic coefficients for the inner and outer film are obtained in the form:

Inner film:

$$\frac{C_1 K_{xx1}}{W}, \quad \frac{C_1 (\omega_1 + \omega_2) B_{xx1}}{W}, \text{ etc}$$
 (26)

Outer film:

$$\frac{C_2 K_{XX2}}{W}, \quad \frac{C_2 \omega_2 B_{XX2}}{W}, \text{ etc}$$
 (27)

Define:

Inner film:

$$z_{xx1} = \frac{c_1 x_{xx1}}{w} + i \frac{1}{1+n} \frac{c_1 (\omega_1 + \omega_2) x_{xx1}}{w}$$
 (28)

(similarly for Z xyl, Z yxl, Z yyl)

Outer film:

$$z_{xx2} = \frac{c_1}{c_2} \frac{c_2 K_{xx2}}{W} + i \frac{c_1}{c_2} \frac{1}{n} \frac{c_2 \omega_2 B_{xx2}}{W}$$
 (29)

(similarly for z_{xy2} , z_{yx2} , z_{yy2})

where:

$$n = \frac{N_2}{N_1}$$

Hence, the dynamic forces acting on the shaft become:

$$\left\{\begin{array}{c}
\frac{y}{x} \\
\frac{y}{y}
\end{array}\right\} = - \left\{\begin{array}{c}
z_{xx1} & z_{xy1} \\
z_{yx1} & z_{yy1}
\end{array}\right\} \left\{\begin{array}{c}
x_1 - x_2 \\
y_1 - y_2
\end{array}\right\}.$$
(30)

In order to bring Eq. (30) into the same form as Eq. (20) and thereby determine the overall dynamic coefficients it is necessary to eliminate \mathbf{x}_2 and \mathbf{y}_2 from the equations. This is done by setting up the equations of motion for the ring with mass m:

$$-\frac{c_{1}^{m\omega_{1}^{2}}}{W} \begin{cases} x_{2} \\ y_{2} \end{cases} = -\begin{cases} z_{xx1} & z_{xy1} \\ z_{yx1} & z_{yy1} \end{cases} \begin{cases} x_{1} - x_{2} \\ y_{1} - y_{2} \end{cases} -\begin{cases} z_{xx2} & z_{xy2} \\ z_{yx2} & z_{yy2} \end{cases} \begin{cases} x_{2} \\ y_{2} \end{cases}$$
(31)

or:

$$\begin{cases}
(\mathbf{z}_{xx1} + \mathbf{z}_{xx2} - \frac{\mathbf{c}_{1}^{m\omega_{1}^{2}}}{\mathbf{w}}) & (\mathbf{z}_{xy1} + \mathbf{z}_{xy2}) \\
(\mathbf{z}_{yx1} + \mathbf{z}_{yx2}) & (\mathbf{z}_{yy1} + \mathbf{z}_{yy2} - \frac{\mathbf{c}_{1}^{m\omega_{1}^{2}}}{\mathbf{w}})
\end{cases}
\begin{cases}
\mathbf{x}_{1} - \mathbf{x}_{2} \\
\mathbf{y}_{1} - \mathbf{y}_{2}
\end{cases} -
\begin{cases}
(\mathbf{z}_{-x2} - \frac{\mathbf{c}_{1}^{m\omega_{1}^{2}}}{\mathbf{w}}) & \mathbf{z}_{xy2} \\
\mathbf{z}_{xy2} & (\mathbf{z}_{yy2} - \frac{\mathbf{c}_{1}^{m\omega_{1}^{2}}}{\mathbf{w}})
\end{cases}
\end{cases}$$
(32)

Substitute Eq. (32) into Eq. (30) and compare with Eq. (20) to get:

$$\begin{cases}
z_{xx} & z_{xy} \\
z_{yx} & z_{yy}
\end{cases} = \begin{cases}
z_{xx1} & z_{xy1} \\
z_{yx1} & z_{yy1}
\end{cases} = \begin{cases}
(z_{xx1} + z_{xx2} - \frac{c_1 m \omega_1^2}{W}) & (z_{xy1} + z_{xy2}) \\
(z_{yx1} + z_{yx2}) & (z_{yy1} + z_{yy2} - \frac{c_1 m \omega_1^2}{W})
\end{cases}$$

$$\begin{cases}
(z_{xx2} - \frac{c_1 m \omega_1^2}{W}) & z_{xy2} \\
z_{yx2} & (z_{yy2} - \frac{c_1 m \omega_1^2}{W})
\end{cases}$$
(33)

Solving for z, z, etc. and using Eq. (21) yields the overall dynamic coefficients for the floating-ring bearing.

In general the mess of the ring is relatively small such that:

$$\frac{c_1m\omega_1^2}{v} << \frac{c_2\kappa_{xx}}{v}$$

in which case it can be ignored in the calculations. This condition applies to all the numerical results given in the present report.

Stability Calculation for Floating Ring Bearing

The overall stability of the floating ring journal bearing to self-excited whirl may be calculated from the overall dynamic coefficients described above. In this present study, the stability calculations were performed by means of the computer program developed under USAF contract No. AF 33(615)-3238 and described in part V of the final documentation issued under this contract (Ref. 9). A brief description of the analysis upon which the stability calculations are based is provided below.

At any given rotor speed and with a known static load on the bearing, the journal center occupies a certain unique equilibrium position relative to the bearing center. When the journal whirls around this equilibrium in a small orbit, the dynamic forces $\mathbf{F}_{\mathbf{x}}$ and $\mathbf{F}_{\mathbf{y}}$ generated in the bearing fluid film can be expressed in linearized form as:

$$F_{x} = -K_{xx} \times -B_{xx} \frac{dx}{dt} - K_{xy} y - B_{xy} \frac{dy}{dt}$$
 (34)

$$\mathbf{F}_{\mathbf{y}} = -\mathbf{K}_{\mathbf{y}\mathbf{x}} \times -\mathbf{B}_{\mathbf{y}\mathbf{x}} \frac{\mathbf{d}\mathbf{x}}{\mathbf{d}\mathbf{t}} - \mathbf{K}_{\mathbf{y}\mathbf{y}} \mathbf{y} - \mathbf{B}_{\mathbf{y}\mathbf{y}} \frac{\mathbf{d}\mathbf{y}}{\mathbf{d}\mathbf{t}}$$
 (35)

where x and v are the whirl amplitudes measured from the static equilibrium position, t is time, and the four apring coefficients (the K - coefficients) and the four damping coefficients (the B - coefficients) would be determined for the floating ring bearing from the analysis described above. For a given bearing geometry and known lubricant properties, the 8 coefficients are functions of the bearing lead and the rotor speed and, if the lubricant is compressible like a gas, they are also functions of the whirl frequency. In the latter case, Eqs. (34) and (35) are only valid for harmonic motions such that:

$$x = x_c \cos(vt) - x_s \sin(vt)$$
 (36)

$$y = y_c \cos (vt) - y_s \sin (vt)$$
 (37)

where v is the angular whirl frequency. These equations can also be written:

$$x = Re \left\{ (x_c + ix_s)e^{ivt} \right\}$$
 (38)

$$y = Re \left\{ (y_c + iy_a)e^{i\gamma t} \right\}$$
 (39)

where $i = \sqrt{-1}$ and "Re()" means that only the real part of the bracketed expression applies. For convenience the "Re()" and the e^{1vt} are dropped whereby Eqs. (38) and (39) are written

$$x = x_c + ix_g \tag{40}$$

$$y = y_c + iy_g \tag{41}$$

When these equations are used in the analysis their complete meaning is defined through Eqs. (38) and (39).

With this notation Eqs. (34) and (35) can be written:

$$\mathbf{F}_{\mathbf{x}} = -\overline{\mathbf{Z}}_{\mathbf{x}\mathbf{x}} \times -\overline{\mathbf{Z}}_{\mathbf{x}\mathbf{y}} \quad \mathbf{y} \tag{42}$$

$$\mathbf{F}_{\mathbf{y}} = -\overline{\mathbf{Z}}_{\mathbf{y}\mathbf{x}} \mathbf{x} - \overline{\mathbf{Z}}_{\mathbf{y}\mathbf{y}} \mathbf{y} \tag{43}$$

where:

$$\overline{Z}_{xx} = K_{xx} + i \left(\frac{V}{\omega}\right) \omega B_{xx} = K_{xx} + i \overline{\gamma} \omega B_{xx}$$
 (44)

$$\frac{1}{7} \cdot \frac{y}{m}$$
 (45)

and similarly for Z_{xy} , Z_{yx} and Z_{yy} . Here, ω is the angular speed of rotation and γ gives the ratio between the whirl frequency and the rotational frequency. In this form, the equations are equally valid for an incompressible and a compressible lubricant.

To illustrate the procedure for calculating the threshold of instability, assume for simplicity that the rotor is rigid and symmetric such that the two bearings support an equal mass M which equals half the mass of the rotor. Then the equations of motion for a journal become:

$$M \frac{d^2x}{dt^2} = F_x$$

$$M \frac{d^2y}{dz^2} = F_y \tag{46}$$

By substitution from Eqs. (41) through (43), these equations can be written in matrix form:

$$\begin{cases}
(\overline{z}_{xx} - Mv^2) & \overline{z}_{xy} \\
\overline{z}_{yx} & (\overline{z}_{yy} - Mv^2)
\end{cases}
\begin{cases}
x \\
y
\end{cases} = 0$$
(47)

At the threshold of instability, a non-zero solution of x and y must exist which means that the determinant \triangle of the matrix should be zero:

$$\triangle = \triangle_{c} + i\triangle_{s} = (\overline{z}_{xx} - Mv^{2})(\overline{z}_{yy} - Mv^{2}) - \overline{z}_{xy}\overline{z}_{yx} = 0$$
 (48)

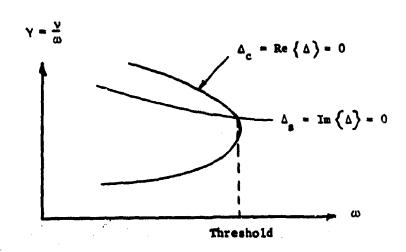
or

$$\Delta_{c} = R_{e} \left(\Delta \right) = (K_{xx} - \overline{\gamma}^{2}M\omega^{2})(K_{yy} - \overline{\gamma}^{2}M\omega^{2}) - K_{xy} K_{yx}$$

$$- \overline{\gamma}^{2} \left[\omega B_{xx} \omega B_{yy} - \omega B_{xy} \omega B_{yx} \right] = 0$$
(49)

$$\Delta_{s} = Im \left(\Delta \right) = \frac{1}{7} \left[(K_{xx} - \frac{1}{7} M\omega^{2}) \omega B_{yy} + (K_{yy} - \frac{1}{7} M\omega^{2}) \omega B_{xx} - K_{xy} \omega B_{yx} - K_{yx} \omega B_{xy} \right] = 0$$
(50)

These two equations must be satisfied simultaneously at the threshold of instability. They contain two unknowns, namely the whirl frequency ratio, $\overline{\gamma}$, and the angular speed of rotation, ω . In the general case, the 8 dynamic fluid film coefficients are functions of both $\overline{\gamma}$ and ω , making a closed form solution impossible, and the solution is most conveniently obtained graphically. For any fixed value of ω , Δ_c and Δ_c can be plotted as functions of $\overline{\gamma}$ to find their zero points. With $\overline{\gamma}>0$ it is seen that Δ_c has one zero point and Δ_c has up to two zero points (only true in this simple case). The calculation is repeated for several values of ω and the results may be plotted as shown:



The intersection of the two curves define the speed at which instability sets in.

RESULTS

Single Film Bearing

Results of calculations of the performance of single film spiral-grooved journal bearings are shown in Figs. 7 through 18. In all cases, the results shown are for bearings having groove geometry optimized for maximum radial component of stiffness at $\epsilon = 0$. These optimum values of groove geometry parameters are given in Tables 1 and 2 presented earlier in the text.

Load capacity of the single film spiral-grooved journal bearing is shown in Figs. 7, 8, 9 and 10, in terms of dimensionless load $W/\mu N_1 LD$ $(G/R)^2$ vs. eccentricity ratio ϵ . Fig. 7 shows results for a bearing of configuration 1 i.e. a bearing having no flow-through of lubricant (see Fig. 2). L/D ratio is taken to be 1.0. It is assumed that only the grooved journal is rotating. In this figure, it can be noted that the existence of turbulence does not significantly effect the linearity of the load vs. eccentricity curve, but only serves to increase the load capacity over that which would be obtained if flow remained laminar.

In Fig. 8 are shown load vs. eccentricity curves for a bearing of configuration 2 with L/D=1.0, in which there is net flow of lubricant pumped through the bearing entirely by action of the spiral grooving ($\mathbf{P}_{\mathbf{g}}=0$). The load capacity of this bearing is seen to be slightly less than that for the configuration 1 bearing. On the other hand, the through-flow of lubricant is useful in removing heat from the bearing.

Fig. 9 shows load capacity of a configuration 2 type bearing with L/D=0.5. As can be seen, unit load capacity, W/LD, decreases significantly with decrease in L/D ratio. As a rough guide, it is found that in the range $0.5 \le L/D \le 2.0$, unit load capacity is very nearly proportional to L/D ratio.

To provide a greater flow of lubricant through a configuration 2 bearing, one can supply the lubricant to the grooved end at an elevated pressure P. The effect of this on load capacity is relatively slight as shown by the curves in

Fig. 10. The results are shown for Re = 5000 but are typical of those obtained at all values of Reynolds number. The degree of pressurization considered is indicated by the dimensionless parameter P_g G_g D/L where P_g is the dimensionless supply pressure defined as $P_g = \left[P_g/\mu(N_i + N_o)\right] (C/R)^2$ and G_g is a turbulent viscosity correction factor corresponding to the mean Reynolds No. $(G_g$ is obtained from Fig. 5). When the supply pressure parameter P_g G_g (D/L) is maintained at 0.35, the net flow of lubricant through the bearing due to pressurization is approximately equal to that due to self-pumping of the grooves, independent of Reynolds number. When this parameter doubles, flow due to pressurization doubles.

In general one may conclude that for values of \overline{P}_{g} G_{g} (D/L) less than 0.7, the effect of pressurisation on load capacity may be neglected. In any case, it is conservative to do so since pressurization tends to increase load capacity*.

Figs. 11, 12, and 13 show curves of attitude angle \$\psi\$ vs. eccentricity ratio for configuration 1 and configuration 2 bearings at different Reynolds numbers and L/D ratios. The effect of pressurization on attitude angle is also shown by the dashed curves in Figs. 12 and 13.

Referring to Fig. 11, which gives attitude angle for a configuration 1 bearing, we see that for laminar flow \$\phi\$ decreases slightly with eccentricity ratio. This decrease is mostly due to effects of cavitation in the bearing film. At higher values of Reynolds number, very little or no cavitation occurs in the bearing film out to \$\epsilon = 0.7\$ and, as a consequence, attitude angle shows very little dependence on \$\epsilon\$. The extent of cavitation that does occur in the bearing will be discussed later in connection with predicted bearing torque.

Pressurization of the grooved end of a spiral-grooved journal bearing produces hydrostatic load capacity whether the journal is rotating or not. Such pressurization will help to promote rotation of the ring in a spiral-grooved floating ring bearing. Getting the ring to rotate can be somewhat of a problem in plain, cylindrical floating ring bearings. Whether this is true for spiral-grooved floating ring bearings remains to be seen.

For configuration 2 bearings, we find again that for laminar flow. 6 decreases with ϵ due to cavitation whereas this effect is less pronounced at higher values of Reynolds number. We also find that pressurization tends to decrease attitude angle. In most instances, this effect is not great, although for laminar flow and L/D = 0.5, a pressurization of \overline{P}_{g} G_{g} D/L = 0.7 produces approximately a 10 degree reduction in attitude angle.

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Comparing Figs. 11 and 12, we see that a configuration 2 bearing of L/D=1.0 has a slightly higher attitude angle than a configuration 1 bearing of the same L/D ratio. Comparing Figs. 12 and 13 we see that for configuration 2 spiral-grooved journal bearings, attitude angle decreases quite substantially as L/D ratio is decreased from 1.0 to 0.5. This latter effect does not occur in plain cylindrical bearings.

In general, we can observe that development of turbulence in spiral-grooved journal bearings reduces the attitude angle by a significant amount i.e. approximately 10 degrees at low eccentricity ratios for both configuration 1 and configuration 2 geometries.

The bearing through-flow, \mathbf{Q}_p , that is generated by the self-pumping of spiral grooving is shown in Fig. 14. Results are plotted in terms of $\mathbf{Q}_p/\mathbb{R}^2C(\mathbf{N}_1-\mathbf{N}_0)$ vs. ϵ . The results shown were obtained neglecting effects of cavitation. This was done because the way in which cavitation is handled in the present analysis does not provide an accurate calculation of flow rate when cavitation appears. This is not a serious deficiency since spiral-grooved bearings usually operate with a full fluid film.

As Fig. 14 indicates, the "self-pumping" flow of an optimized bearing increases as turbulence develops in the bearing film. This is probably due to the fact that the optimum value of groove depth increases as turbulence develops. When turbulence is fully developed (Re = 5000) both flow and optimum pocket depth approach asymptotic values.

It should be kept in mind that the results shown in Fig. 14 pertain to a bearing

with $\overline{Y} = 0.67$ i.e. a bearing with grooving on 67% of its length. Flow through the bearing can be increased by increasing \overline{Y} slightly with very little penalty paid in terms of loss of load.

The flow of lubricant, Q_g , through a spiral-grooved bearing that results from pressurizing either end of the bearing is directly proportional to $P_g C^3 G_g/\mu$ (D/L) for any given eccentricity ratio and Reynolds number. Curves of dimensionless pressure flow, $Q_g \mu/G_g C^3(L/D)$ are plotted vs. ϵ in Fig. 15. Use of the turbulent viscosity correction factor G_g in forming this dimensionless flow takes account of the influence of Reynolds number quite well although some slight dependence on Reynolds number still remains.

The dimensionless torque, T_jC/µN₁R³L, on the journal of a spiral-grooved bearing is plotted in Fig. 16 for a configuration 1 bearing and in Fig. 17 for a configuration 2 bearing. The solid lines show the torque for a bearing with a complete fluid film while the dashed curve shows the torque taking account of cavitation that would be expected to occur. Cavitation is accounted for by assuming that all regions of subambient pressure are cavitated and that shear stresses in these regions are negligible. The discrepencies between the dashed and solid curves in Figs. 16 and 17 provide an indication of the extent of cavitation that develops as eccentricity increases.

Looking at Fig. 16, we see that for a configuration 1 bearing, cavitation does not set in until $\cong 0.3$ for laminar flow, until $e \cong 0.5$ for Re = 1000, and does not occur at all below e = 0.7 for Re = 5000 and 9000. For an unpressurized configuration 2 bearing (Fig. 17), cavitation occurs at lower values of e than for a configuration 1 bearing and does occur at Re = 5000 and 9000. Cavitation can easily be eliminated, however, by modest pressurizing of the bearing.

The solid curves shown in Fig. 17 also apply with reasonable accuracy to bearings with L/D=0.5. The dashed curves do not, however, because there is less tendency for a spiral-growed bearing to cavitate as L/D ratio is decreased. For configuration 2 bearings with L/D=0.5, no cavitation occurs for Re>1000 and $\epsilon<0.7$.

An important quantity to consider is how the dimensionless ratio of friction torque to load, T_i/WC , varies with Reynolds number. This is shown in Fig. 18 for $\epsilon = 0.2$, 0.5 and $\epsilon = 0.7$. As can be seen, torque increases more rapidly than does load when turbulence develops in the bearing film. One can note at this point that one of the advantages of the floating ring bearing is that the Reynolds number in each separate bearing film is less than the Reynolds number that would be obtained if the bearing had only a single film. Hence, due to this effect alone, the floating ring bearing can operate with a more favorable torque to load ratio than an equivalent bearing with only a single film.

Floating Ring Bearing

The floating ring configuration chosen for analysis was one having an overall length to diameter ratio of L/D = 1.0. (See Figure 4). This means that each half of the floating ring bearing had an effective length to diameter ratio of 0.5. Grooving parameters for each half of the floating ring bearing were those presented in Table 2. Grooving on the outside surface of the ring was the same as that on the shaft.

Two values of the ratio of inner clearance to outer clearance were considered i.e. $C_2/C_1 = 1.2$ and 0.8. Results were obtained for no pressurization of the bearing $(\overline{P}_s = 0)$ and for a degree of pressurization corresponding to \overline{P}_s G_z D/L = 0.35.

The static performance data for the floating ring journal bearing are given in Table 3. Dynamic performance data are given in Tables 4 and 5. Much of this data is presented in graphical form in Figs. 19 through 36. These figures are discussed below.

Curves of dimensionless load, W, vs the eccentricity ratio of the inner film ε , are presented in Fig. 19. The curves are for $C_2/C_1=1.2$ although they apply within a few percent accuracy to the case of $C_2/C_1=0.8$. As can be seen the degree of pressurization considered for the floating ring bearing (dashed curves) results in a substantial increase in load capacity over the

unpressurized case (solid curves). For the single film bearing, the same apparent degree of pressurization resulted in only a slight increase in load capacity (See Figure 10). The reasons for the greater apparent effect of pressurization on the floating ring bearing are as follows.

First, the parameter P_g G_gD_1/L for the floating ring bearing is based on the overall L/D_1 . The effective value of this parameter for each half of the floating ring bearing is actually twice the overall value. Second, the value for G_g used in establishing the parameters P_g G_gD_1/L is based on the overall Reynolds number $Re = 2gN_1R_1C_1/v$. Because of rotation of the ring, the individual Reynolds numbers for the inner and outer films are each less than the overall. Hence, the effect of pressurization of each film is greater than is indicated by the parameter P_g G_g D_1/L because, in turbulent flow, the lower the Reynolds number the greater the amount of flow for a given supply pressure. Third, the dimensionless supply pressure P_g is based on the shaft speed N_1 . For spiral-grooved bearings, it turns out that rotation of the ring decreases rather than increases the load capacity of the inner film. Hence pressurization of the inner film becomes relatively more significant with respect to load capacity of the film.

Roughly speaking, the increase in load capacity resulting from pressurization of a floating ring bearing is linearly proportional to the guage supply pressure. One can therefore linearly interpolate between the curves shown in Fig. 19 to determine load capacity at supply pressures different from that considered.

Curves of overall attitude angle ϕ of the floating ring bearing are shown in Figs. 20 and 21. Overall attitude angle is defined in Fig. 4. Values for the attitude angles of the inner and outer films are given in Table 3. Due to rotation of the ring, which decreases the spiral-grooved pumping effect in the inner film, attitude angles for the inner film are considerably greater than for the outer film.

Values of dimensionless journal torque, $T_j : T_j/WC$, are given in Fig. 22 for a floating ring bearing with $C_2/C_1 = 1.2$. Similar curves for a bearing with $C_2/C_1 = 0.8$ would run about 7% higher.

One of the primary advantages of the floating ring bearing is that, for a given eccentricity of the inner film, the ratio of torque to load is much lower than for a comparable single film bearing. This is particularly true for plain bearings for which load capacity of the inner film is proportional to the sum of the speeds of the shaft and ring. In spiral grooved bearings, however, the pumping effect of the grooves is proportional to the difference in speed between the shaft and ring. Load capacity of these bearings is due partly to this pumping effect and partly to the usual hydrodynamic effect which is proportional to the sum of the shaft and ring speed. The net effect is that as ring speed increases, load capacity of the inner film for a spiral-grooved bearing decreases slightly. Consequently, spiral-grooved floating ring bearings do not enjoy the same torque to load advantage possessed by plain floating ring bearings. Nonetheless, the spiral-grooved floating ring bearing does have a torque to load ratio better than that of a single film bearing operating at the same eccentricity ratio. This is evidenced by the curves shown in Fig. 23. The single film bearing used for comparison in this figure is a configuration 2 bearing with L/D = 0.5. This provides a fair comparison because each side of the centrally fed floating ring configuration we are considering consists, essentially, of an isolated bearing with L/D = 0.5.

Total flow pumped through the floating ring bearing by the self-pumping effect of the spiral grooves is plotted in Fig. 24. The increase in lubricant flow that would result from pressurization of the bearing can be calculated from the single film curves plotted in Fig. 15. These single film curves can be applied directly to each individual film of the floating ring bearing on either side of the central feeding groove. In applying these curves to calculate pressure flow, one must be careful to use the appropriate Reynolds number and L/D ratio corresponding to the individual film being considered. The pressure flow that is calculated can be added directly to the self-pumping flow calculated from Fig. 24.

Ring speed ratio, N_2/N_1 , is plotted as a function of inner film eccentricity ϵ_1 in Figs. 25a and 25b. Results for laminar flow and Re = 9000 are shown. Results for Re = 5000 are nearly the same as for Re = 9000 while results for Re = 1000

lie between the Re = 9000 and laminar curves. Ring speed ratio for laminar flow tends to decrease with ϵ_1 while, for turbulent flow, ring speed ratio remains relatively constant with eccentricity. Note that ring speed ratio is not strongly affected by the clearance ratio C_2/C_1 .

 ϵ_2 , the eccentricity ratio for the outer film, is plotted as a function of ϵ_1 in Fig. 25. In general, ϵ_2 increases approximately linearly with ϵ_1 . As would be expected, ϵ_2 is considerably greater than ϵ_1 for $C_2/C_1 = 1.2$ and more nearly equal to ϵ_1 for $C_2/C_1 = 0.8$.

Dynamic data for the floating ring bearing are given in Tables 4 and 5. These data consist mostly of stiffness and damping coefficients for the individual bearing films and for the overall bearing. The data also include values of the dimensionless critical mass for the threshold of whirl instability.

Data for the individual bearing films are given in Table 4. Stiffness and damping for the inner film pertain to the fluid film forces that develop in the inner film due to <u>relative</u> motion between the shaft and the ring. Stiffness and damping for the outer film pertain to fluid film forces developed in that film due to <u>relative</u> motion between the ring and the outer boaring.

Stiffness and damping coefficients for the overall floating ring bearing are given in Table 5. These pertain to the forces developed on the shaft due to a relative motion between the shaft and the outer bearing including the effect of motion of the ring.

Overall stiffness and damping coefficients for the floating ring bearing are plotted vs. ϵ_1 for a number of representative situations in Figs. 27 through 32. Qualitatively, the behavior of the overall stiffness and damping coefficients as eccentricity ratio increases is similar to that for single film bearings.

The stiffness and damping coefficients presented in Tables 4 and 5 may be used to calculate a critical mass at the threshold of whirl instability. The critical masses determined from the inner or outer film damping and stiffness coefficients,

while not of great physical significance, are still of interest to calculate. The critical mass $\rm M_{cl}$, determined from the inner film coefficients, is the critical mass of the shaft within the rotating ring assuming that the ring were restricted from any translational motion i.e. assuming that the outer film were infinitely stiff. $\rm M_{c2}$, the critical mass calculated from the outer film coefficients, is the critical mass for the ring rotating within the bearing neglecting any effect of the inner bearing film. Essentially, $\rm M_{c2}$ represents the critical mass for a single film bearing operating at Reynolds number Re, and eccentricity ratio $\rm \epsilon_2$.

 ${
m M}_{
m C}$, the critical mass determined from the stiffness and damping coefficients for the overall floating ring bearing, represents the critical mass for the shaft rotating within the composite floating ring structure. It is the appropriate value of critical mass for the shaft of the floating ring bearing.

The critical masses M $_{\rm c1}$, M $_{\rm c2}$ and M $_{\rm c}$ are presented in Tables 4 and 5 in the dimensionless form

$$\bar{M}_{c1} = \frac{M_{c1} C_1 (N_1 + N_2)}{\mu (R_1/C_1)^2 LD_1}$$

$$\overline{M}_{c2} = \frac{\frac{M_{c2} C_2 N_2}{\mu (R_2/C_2)^2 LD_2}}$$

$$\overline{N}_{c} = \frac{M_{c} C_{1} N_{1}}{\mu (R_{1}/C_{1})^{2} LD_{1}}$$

In attempting to compare the critical masses in these tables one should keep in mind that each is made non-dimensionless on a slightly different basis.

Values of overall critical mass vs. ϵ_1 are plotted in Figs. 33 and 34 for

C₂/C₁ = 1.2 and 0.8 respectively. In general, critical mass for hydrodynamic bearings increases with eccentricity ratio. However, when operating in the turbulent regime, 'al-grooved bearings exhibit the anomalous characteristic that critical mass accreases with eccentricity in certain ranges. This characteristic may be related to the fact that the attitude angle of spiral-grooved bearings sometimes increases with eccentricity ratio in the turbulent regime. This increase in attitude angle can be qualitatively explained on the basis that as eccentricity increases, the usual plain-bearing-type of hydrodynamic action becomes relatively more significant compared with the self-pressurizing hydrodynamic action of the spiral grooves, particularly in turbulent flow. Hence, there is a tendency for attitude angle to increase with eccentricity in spiral-grooved bearings.

It is interesting to note in Figs. 33 and 34 that pressurization of the floating ring bearing has a more significant effect on bearing stability than it does on bearing load capacity. It is obvious that pressure feeding of the bearings is an effective means of stabilization.

An important point to investigate is whether the spiral-grooved, flusting ring bearing configuration is more or less stable than an equivalent spiral-grooved, single film bearing. Comparisons of the critical masses of the floating ring and single film configurations are shown in Figs. 35 and 36 for laminar and turbulent flow respectively. The single film values of critical mass were taken from the values for $M_{\rm C2}$ calculated for the outer film. The L/D ratio of the outer film is about 20% less than that for the inner film but this fact should not greatly effect the comparison.

For laminar flow, the single film bearing is more stable than the floating ring bearing with $C_2/C_1=0.8$ and, at low eccentricities, is also more stable than the floating ring bearing with $C_2/C_1=1.2$. However, at high eccentricities, the critical mass for the floating ring bearing with $C_2/C_1=1.2$ exceeds that of the single film bearing.

For turbulent flow, the stability of the single film configuration is clearly

superior to that of the floating ring bearing.

The floating ring configuration of spiral-grooved bearings suffers in regard to stability for the following reason. The good stability of spiral-grooved bearings is due principally to the self-pressurizing effect of the spiral grooves. This self-pressurizing effect is proportional to the difference in speeds, $(N_1 - N_2)$. Consequently, in a floating ring configuration, rotation of the ring reduces this self-pressurizing effect in the inner film and, hence, reduces the stability of the inner film. The stability of the overall bearing suffers as a consequence.

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Stability of the spiral-grooved configuration is compared with the stability of a plain floating ring bearing in Fig. 37. At low eccentricities, stability of the spiral-grooved configuration is better but, at high eccentricity, stability of the plain bearing increases rapidly due to the effect of cavitation and begins to surpass that of the spiral-grooved bearing.

An important point to keep in mind when comparing the stability of plain and spiral-grooved bearings is that the plain bearings achieves stability only as a result of cavitation in the bearing film. A plain bearing operating with a full fluid film is inherently unstable for any speed or mass. Often, particularly with liquid metals as lubricants, it is undesirable to operate with cavitated bearing films because of the problem of cavitation damage. If a pressurized supply is used with plain bearings to suppress cavitation, the stability of the bearings suffers drastically.

On the other hand, spiral-grooved bearings, even when unpressurized, operate without cavitation in the bearing film out to quite large eccentricity ratios due to the self-pressurizing action of the spiral grooves. Stability of these bearings is achieved through this self-pressurizing action. Moreover, use of a pressurized lubricant supply further enhances the stability of these bearings as is evidenced by the performance charts presented in this report.

SUMMARY AND CONCLUSIONS

An analysis has been performed of the turbulent, spiral-grooved, journal bearing with incompressible lubricant. Optimum values of groove parameters have been determined to provide maximum radial stiffness. Performance charts are presented for load capacity, attitude angle, lubricant flow rate and bearing frictional torque for both single film and floating ring configurations of the spiral-grooved journal bearing. In addition, stiffness and damping coefficients are presented for the floating ring configuration and values of the critical mass for threshold of whirl instability are determined. Performance data are presented for bearings operating with and without a pressurized supply of lubricant.

The following general conclusions can be drawn concerning the performance of spiral-grooved single film and floating ring journal bearings:

- 1) Compared with plain, cylindrical journal bearings, spiral-grooved bearings offer the following advantages: (a) They possess greater stability under lightly loaded conditions. (b) They tend to operate without cavitation due to the self-pressurizing effect of the spiral-grooving. (This is an important consideration when operating the bearing with liquid metal lubricants where the problem of cavitation damage is significant.) (c) The spiral grooving provides self-pumping of lubricant through the bearing eliminating the need for a pressurized supply. (d) All performance characteristics of spiral-grooved bearings can be easily enhanced by use of a pressurized supply of lubricant.
- 2) The floating ring configuration of spiral-grooved bearing operates with lower torque to load ratio than is achieved with a similarly loaded single film bearing. On the other hand, stability of the single film spiral-grooved bearing is generally better than that for the floating ring bearing.
- 3) In spiral-grooved bearings, development of turbulence results in an increase in frictional torque, an increase in load capacity, an increase in stability and a decrease in attitude angle. In general, the ratio of frictional torque to load capacity increases with development of turbulence.

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G. = Q2 P2 G2 H2	3.53	3.62	3.73	5.73	5.5	5.2	8.21	7.9	7.3	1.7	8	3.	32.6	37.0	9.95	37.8	47.4	63.0	45.0	49.3	1.09	47.9	4.64	57.3
$\overline{Q}_{1} = \frac{Q_{1}}{R_{1}^{2}G_{1}^{2}(M_{1} + M_{2})}$	1.78	1.1%	2.24	2.54	2.57	2.91	3.57	3.57	3.63	3.80	3.74	3.74	14.2	14.8	16.5	15.9	17.5	18.9	20.5	50.9	22.9	22.1	22.3	23.2
Q = 0 R ₁ ² C ₁ ² M ₁	5.13	96.4	4.76	7.42	7.40	6.98	10.8	9.01	0.01	11.5	11.2	4.02	42.4	45.4	, X	8.5	53.2	₹ \$	3.	63.9	2.8	æ.	1.98	71.8
4	37.4	36.6	34.8	31.2	32.0	7.7	26.8	26.9	29.8	26.3	26.5	28.8	20.4	21.0	23.9	16.0	16.7	21.5	14.4	14.3	6.91	14.3	14.6	16.5
* 2	25.4	29.1	28.9	23.1	24.2	30.9	18.5	19.1	23.6	17.8	18.1	22.1	13.1	13.7	18.0	10.1	10.9	18.0	8.7	9.1	17.7	8.6	6.9	11.7
41	57.4	54.3	47.1	49.5	0.67	45.0	1.4	42.9	42.3	43.4	43.0	42.0	35.2	35.3	35.1	27.2	27.7	29.0	24.8	24.1	24.9	24.8	24.7	25.3
$\overline{P}_{02} = \frac{PC_0^2}{\mu N_2 N_2^2}$	•	0	0	0	•	۰	0	•	0	0	•	•	10.5	10.8	12.8	12.6	12.8	4:41	24.5	24.7	25.4	× ×	34.9	35.7
$\overline{P}_{a1} = \frac{PG_1^2}{\mu(H_1 + H_2)R_1^2}$	o	•	0	0	•	•	-	٥	•	•	•	0	9.	3.0	3.16	3.65	3.66	3.78	7.10	7.11	7.18	1.63	10.1	10.2
Tj/NG1	19.3	12.6	7.41	26.9	18.0	9.01	36.3	23.6	13.6	39.4	25.7	14.5	5.3	.9.71	6.42	17.3	11.7	7.7	22.9	14.7	8.97	0.53	16.4	3.6
82 = 10,4478,2 WG2	188.	.514	.222	.874	.525	.236	.463	.2%	.157	338	.217	.112	. zs.	141	.199	.567	386.	.180	Š	195	.107	in.	.147	.079
$\mathbf{a_1} = \mathbf{E}\mathbf{b_1} \frac{\mu(\mathbf{x_1} + \mathbf{x_2})\mathbf{x_1}^2}{\mathbf{w}\mathbf{c_1}^2}$	19.2	3.1	728 .	2-41	1.5	.773	1.33	6.79	\$	ne.	.625	.331	2.06	1.32	ž	1.63	1.06	.572		.562	-316	3.	423	162-
$\theta = \frac{10^{1} \text{Me}^{2}}{\text{Me}^{2}}$	1.88	1.21	.639	1.11	1.10	.577	3.	\$65	.333	35	*	.237	1.47	. *	Ř	1.16	.759	77.	.631	84	-226	.465	8	.165
Reg = 2xH2R2C2	***	3	3	춋	572	169	2938	2913	2829	52.88	5267	sus	Ž	3	14	5 2	578	212	2938	2917	2834	5282	52.75	5159
$Re_1 = \frac{2\pi(N_1 - N_2)R_1C_1}{\nu}$	¥3	3	3	\$	603	629	2960	2977	3135	5327	5342	24.8 24.8	3	3	Ĕ	ž	59%	3	29562	2974	3032	5332	5336	¥17
M ₂ /M ₁	.391	.354	.289	907	.397	.340	907	.405	.393	905.	907.	.395	.399	.388	.329	904.	.401	.356	80%	.405	.3%	408	707	.398
•	.306	7447	769.	.286	.420	.729	.270	.405	.673	.266	.392	.661	.270	.395	.655	.263	.390	8	.256	.388	.655	3.5	376	.637
٠,	607	.587	.870	.370	.540	.929	340	.507	.831	.332	.483	.821	.336	.485	. 795	.320	087	.870	705.	.467	.796	303	446	.758
€1	2.	٤.	i.	-2	ú	٠ż	77	.3	٠.	7.	ņ	ý	.2	ı.	rj	2	e;	ż.	2	۳:	'n	,		λ
$Re = \frac{2\pi N_1 R_1 C_1}{v}$	4			1000			88			8			Š			1000			900			S		
$\overline{P}_0 = \frac{PC_1^2}{\mu N_1 R_1^2}$	0			0			0			0			4.2			5.13			10.0			14.2	!	
c ₂ /c ₁	1.2			1.2			1.2			1.2			1.2	- 		1.2		-	1.2			1	!	

TABLE 4 DYNAMIC PERFORMANCE DATA FOR THE FLOATING RING JOURNAL BEARING

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$[(H_c)_2 = \frac{H_{c2}N_1}{2\mu L} (\frac{C_2}{R_2})^3]$.258 .363 1.24	.270	.605 .557 .869	.880	.748 .895 .750	.756	1.47	22 21 04
$(M_c)_1 = \frac{M_{c1}(M_1 + M_2)}{2\mu L} (\frac{c_1}{R_1})^3$.109	.134 .143 .211	.272.	.403 .415 .471	229	331	.618 .687	. 932 . 967 . 902
(B _{yy}) ₂	2.65 3.28 7.34	2.38 2.70 28.2	3.81 4.09 5.68	5.22 5.66 7.84	2.41 2.67 4.50	2.28	3.74 3.93 5.32	5.12 5.39 6.91
(Byx)2	.225 .670 8.37	.282	.014	.062 .239 3.18	.025	027 .023 4.96	060	051 .01 2 .905
(B _{xy}) ₂	.377 .925 8.29	.507	.240	.342 .624 3.55	.149	.115	.154 .262 1.74	.359
(B ₂₀₂)	3.08 4.43 21.0	2.68 3.49 81.6	4.16 5.00 14.9	5.81 6.90 16.5	2.85 3.72 11.2	2.57 3.18 20.9	4.07	5.69 6.64 13.2
(Kyy) ₂	2.43	3.00	5.95 6.21 6.26	8.93 44.6 47.9	4.08	5.41 5.56 5.27	10.2 10.9 10.5	14.6 14.8 15.5
(Kyk)	-1.32 -1.70 -2.55	-1.37 -1.83 -2.81	-1.93 -2.65 -4.89	-2.98 -3.41 -6.11	-1.09 -1.52 -5.54	-1.13 -1.58 -4.74	-1.75 -2.39 -7.31	-2.49 -3.12 -8.00
(K _{xy}) ₂	1.94 2.90 9.69	1.51	2.44 2.67 5.93	2.97 3.72 7.10	1.15 1.53 3.60	1.04	1.76	2.22 3.09 3.86
(K _{xx}) ₂	3.45 5.15 17.5	3.54 4.20 31.8	7.16	9.30 11.3	5.00 6.31 11.1	5.91 6.46 15.6	11.3 12.2 13.0	15.1 19.7 18.9
(ii _{yy}) ₁	3.27 3.36 3.46	3.14	5.17 5.40 6.26	7.06 7.48 8.76	3.19	3.09 3.21 3.76	5.11	6.99 7.25 8.12
(Byx)	.015 .321 1.05	.023	061 .048 .492	055 .167	.016 .129	040 .026	011	089 .063
(B _{xy}) ₁	.165 .453 1.32	.174	.253 .404 .991	.315	.318	.157 .254 .668	.801	.282 .506 1.19
(Ban')	3.19	3.13	5.18	7.09	3.28	3.18	5.24 5.57 6.85	7.17
(K _{yy})	1.07	1.34 1.39 2.01	2.72 2.92 3.09	3.97	1.96 2.03 2.26	2.69	5.12 5.33 5.44	6.99 7.33 7.42
(K,),	-1.58 -1.52 -1.38	-1.58 -1.65 -1.63	-2.60 -2.56 -3.01	-3.28 -3.76 -4.16	-1.42	-1.44	-2.36 -2.26 -3.34	-2.82
⟨k̄ _{xy} ⟩ ₁	1.72	1.67	3.07	3.96	1.51	1.46	2.45 2.87 3.03	3.75
(K ₁₀₀)	1.10	1.43	3.23	4.15 4.42 6.30	2.15	3.6	85.2 25.3 74.3	8.00 7.73 10.5
4 1	4 6 7	4 45 45	4 4 4	4 4 4	4 4 4	4 4 7	4 4 4	4 4 v
Re = 2xH ₁ R ₁ C ₁	3	0001	800	0006	ă	8	2000	0006
$\overline{P}_{g} = \frac{PG_{1}^{2}}{\mu N_{1}R_{1}^{2}}.$	0	0	0	0	4.2	5.13	10.0	14.2
c ₂ /c ₁	1.2	1.2	1.2	1.2	1.2	1.2	1.2	1.2
	L	L	1	l		L	<u> </u>	

The state of the s

,						
(Ñ _c) ₂	.248	.202 .205	.394	.580 .586 .619	. 514. 544. 586. 404. 388.	.742 .723 .599 .1.54 1.00
ري ^{و)} ا	.125	.149	.357	.396	252 222 124 124 235 235 235 235 235 235 235 235 235 235	. 635 . 766 . 631 . 848 . 1.00
(B _{yy}) ₂	2.36 2.59 3.35	1.97 2.07 2.68	2.83 2.93 3.36	3.96 4.08 4.51	2.31 2.46 3.01 1.96 2.04 2.04	2 81 2 91 3 32 3 96 4 05
(\$ _{yx}) ₂	.186	016 .039	.010	069 016 .267	010 077 034 00	20 20 471. 20 20 30
(ī _{xy}) ₂	.156 .328 1.26	.107 .186 .763	.123 .202 .572	.126 .212 .619	.208 .208 .658 .089	.109 .171 .473 .125 .181
(3 _{xx}) ₂	2.51	2.07	3.22	4.06	2.51 2.91 4.57 2.08 2.34 3.67	2.96 3.29 4.74 4.11 4.42 6.00
(Kyy) 2	2.17 2.36 3.18	2.37	4.41 4.50 4.58	6.56 6.56 6.85	3.15 3.33 3.80 3.62 3.62	6.64 6.75 6.86 9.44 9.66
(Ky2)2	-1.19 -1.28 -1.56	-1.11 -1.22 -1.90	-1.56 -1.70 -2.50	-2.28 -2.33 -3.06	-1.06 -1.20 -1.99 -1.00 -1.17	-1.41 -1.62 -2.76 -1.60 -2.19
(K _{xy}) ₂	1.46 1.84 3.43	1.16 1.31 2.03	1.61 1.77 2.22	2.03	1.17 1.41 2.26 .976 1.08	
(K _{xx}) ₂	2.55 3.26 6.06	2.58 2.85 3.86	4.69 5.09 5.89	6.53 7.13 8.79	3.60 4.28 6.40 3.84 4.12 4.75	6.94 7.41 7.94 11.1 10.1
(i ₂₇) ₁	3.26 3.47 3.57	3.19 3.38 3.79	5.27 5.50 6.31	7.18 7.53 8.62	3.19 3.38 4.10 3.14 3.27	5.23 5.38 5.93 7.13 7.35 8.24
(B _{yx})	.023	021 .068 .618	063 .047 .495	056 .138 .831	.013 .122 .584 .584 .039	089 026 .305 091
(ing)	.179	.176 .297	966° 907° 966°	.321 .574 1.48	.169 .312 .907 .903 .256	.231 .333 .810 .287 .486
(B _{ER})	3.22 3.33 4.03	3.19	5.36 5.56 6.54	7.22	3.28 3.60 4.84 3.24 3.24	5.37 5.68 6.95 7.32 7.84
(<u>K</u> 33) 1	1.26	1.56	2.% 3.37 3.17	3.94 4.39 4.27	2.14 2.30 2.35 2.82 2.85	5.33 5.71 5.57 7.02 7.47
(K ₇₈)	-1.60	-1.61 -1.68 -1.65	-2.66 -2.35 -3.11	-3.59 -3.38 -4.42	-1.49 -1.53 -1.98 -1.48 -1.61	-2.45 -2.19 -3.38 -3.31 -3.06
(g ^{x2})	1.78	1.71	3.30	3.80 4.60 5.09	1.57 1.75 2.50 1.50 1.63	2.53 3.04 3.09 3.44 4.21 4.30
(K ₂₀)	1.36 1.53 2.62	1.60	3.10	4.13 5.11 5.77	2.34 2.63 3.64 3.17	5.60 6.80 6.65 7.38 9.30
•1	4 6 5	4 4 4	44.2	d is d	dun dun	444 444
Re .	3	1000	2000	0006	1000	0005
7 _a	•	•	0	0	5.13	14.2
c ₂ /c ₁	8.0	6.0	8.0	8.0	0.0 0.0	ø. 0 8.

TABLE 5 DYNAMIC PERFORMANCE DATA FOR THE FLOATING RING JOURNAL BEARING

c ₂ /c ₁	$\overline{P}_{\alpha} = \frac{P_{\alpha} C_1^2}{\mu H_1 R_1^2}$	$Re = \frac{2\pi^{N_{1}R_{1}C_{1}}}{v}$	٠1	r x	K _X y	K _{yx}	X _{yy}) XX	B Ny	B y'x	997 197	$\overline{\overline{\mathbf{H}}}_{c} = \frac{\frac{\mathbf{H}_{c} C_{1} \mathbf{H}_{1}}{c_{1}} \left(\frac{C_{1}}{\mathbf{E}_{1}}\right)}{\mu \mathbf{L} \mathbf{D}_{1}} \left(\frac{C_{1}}{\mathbf{E}_{1}}\right)$	(·//æ) _c
1.2	0	LAN	.2	. 785	.762		.637	1.32	.629	- 0	1.41	.084	.50
			.3 .5	1.00 2.69	.928 2.05	653 33	.745 1.28	1.52 2.09	.990 2.61	.123	1.64 2.23	.102	.50 .29
			.,	1.,,	2.05								
1.2	0	1000	•2	.909	.652	592	.782	1.29	.541	041	1.31	.106	.48
			.3	1.06 3.18	.790 2.42	676 .006	.799 1.58	1.51	.743 2.82	.020 .859	1.46 2.43	.113	.49 .57
			••	3.10	2.42	.500		,	2.02	.039	2.43		.,,
1.2	0	5000	.2	1.81	1.04	928	1.58	2.10	.842	087	2.16	.223	.46
			.3	1.97	1.15	985	1.62	2.40	1.03	021	2.28	.244	.45
		. :	.5	3.44	2.07	-1.27	1.71	3.84	2.40	.555	2.92	.356	.44
1.2	0	9000	.2	2.44	1.38	-1.19	2.23	2.97	1.09	089	2.93	.337	.43
]			.3	2.85	1.58	-1.45	2.34	3.33	1.40	016	3.20	.236	.46
			.5	4.88	2.91	-1.72	2.49	5.38	3.15	.697	4.10	.538	-42
1.2	4.2	LAN	.2	1.26	.528	492	1.06	1.44	.431	039	1.36	.243	.36
{			.3	1.51	.655	588	1.11	1.73	.607	.004	1.48	.258	.37
			.5	2.72	1.34	965	1.20	3.30	1,60	.417	2.19	.453	.33
1.2	5.13	1000	.2	1.54	.473	482	1.42	1.38	.392	051	1.31	.315	.35
			.3	1.68	.542	582	1.44	1.62	.506	038	1.39	.308	.36
			.5	3.71	1.47	688	1.44	3.18	1.96	.514	1.98	-1.33	.21
1.2	10	5000	.2	2.97	.802	784	2.74	2.25	.637	097	2.18	.595	.35
}			.3	3.17	.869	814	2.76	2.53	.744	063	2.20	.649	. 34
			.5	4.11	1.32	-1.63	2.80	4.83	1.65	.312	2.88	.693	.36
1.2	14.2	9000	.2	4.00	1.08	938	3.69	3.10	.808	098	2.88	.907	.33
			.3	4.84	1.28	-1.34	3.99	3.51	1.14	067	3.18	.830	.37
}	1		.5	5.77	1.80	-2.05	3.95	6.18	2.09	.261	3.77	.999	.35

TABLE 5 (continued)

c ₂ /c ₁	a**I	*	L ₃	g ^{ra}	K Ky	¥ ¥	אָצ	ğ	жу	В Ух	в	oI	(<i>\uldalaha</i>) _c
													
0.8	0	LAH	.2	1.21	1.31	-1.15	1.09	2.04	. 794	096	2.25	.105	.57
			.3	1.39	1.43	-1.12	1.24	2.18	1.08	.016	2.46	.127	.56
			.5	2.43	2.12	-1.07	1.77	2.88	2.26	.572	2.79	.179	.57
0.8	0	1000	.2	1.41	1.19	-1.13	1.31	1.94	. 799	120	2.11	.122	.58
			.3	1.56	1.32	-1.18	1.33	2.08	.956	067	2.23	.127	.58
			.5	2.16	1.77	-1.21	1.62	2.76	1.82	.294	2.72	.178	.55
0.8	0	5000	.2	2.67	1.82	-1.73	2.52	3.11	1.19	179	3.33	.241	.55
1			.3	3.03	2.06	-1.54	2.72	3.42	1.50	105	3.49	.301	.52
			5	3.53	2.44	-2.15	2.65	4.14	2.09	.148	4.00	.278	.57
0.8	0	9000	.2	3.59	2.45	-2.38	3.48	4.24	1.44	201	4.49	.322	.55
			.3	4.31	2.91	-2.27	3.77	4.67	1.92	125	4.78	.382	.54
			.5	5.06	3.37	-3.01	3.71	5.58	2.73	-243	5.44	.376	.58
0.8	4.2	LAN	.2	1.90	1.03	95	1.71	2.28	.781	138	2.31	.266	.43
į			.3	2.18	1.19	-1.03	1.77	2.52	.982	075	2.44	.278	.44
			.5	3.15	1.79	-1.40	1.90	3.46	1.74	-202	2.95	.318	.47
0.8	5.13	1000	.2	2.35	.946	939	2.21	2.19	. 794	153	2.20	.337	.43
		ŀ	.3	2.51	1.03	-1.03	2.23	2.40	-925	123	2.28	.335	.44
			.5	3.06	1.38	-1.47	2.22	3.20	1.45	.048	2.66	.328	.47
0.8	10.0	5000	.2	4.32	1.48	.1.45	4.11	3.43	1.16	210	3.44	.615	.43
		1	.3	4.94	1.68	-1.33	4.25	3.87	1.41	147	3.56	.781	.39
			, 5	5.26	1.92	-2.19	4.27	4.88	1.95	025	3.97	.614	.46
0.8	14.2	9000	.2	6.14	2.16	-1.98	5.60	4.50	1.62	255	4.69	.781	.45
			.3	6.86	2.39	-1.90	5.87	5.26	1.82	180	4.83	.990	.41
			.5	7.34	2.64	-2.97	5.97	6.43	2.51	003	5.36	.819	.47

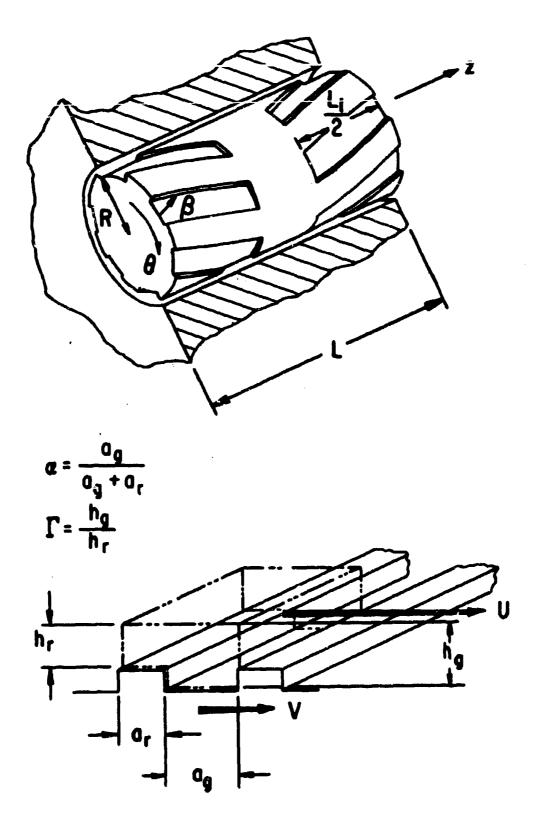
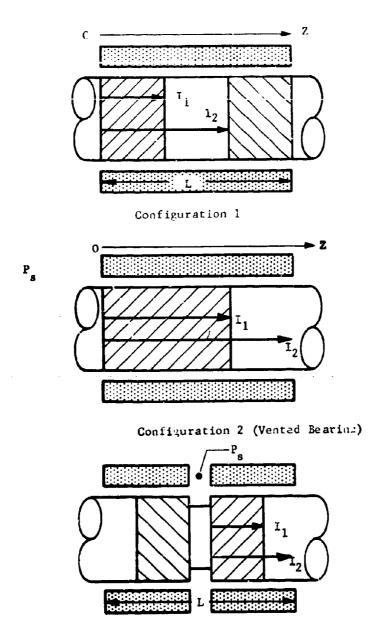


Figure 1. Schematic of Spiral-Grooved Journal Bearing



Configuration 3 (Vented Bearing)

Figure 2. Various Configurations of Spiral-Grooved Journal Bearings

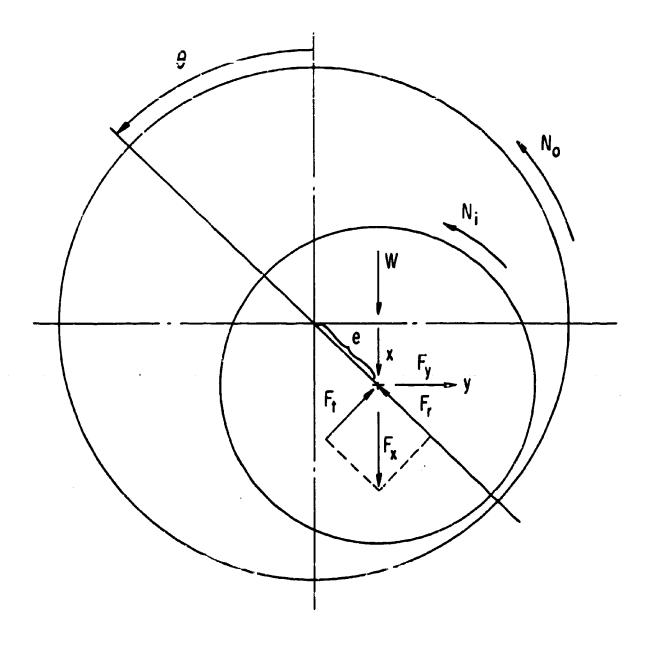


Figure 3. Coordinate System for Forces and Displacements

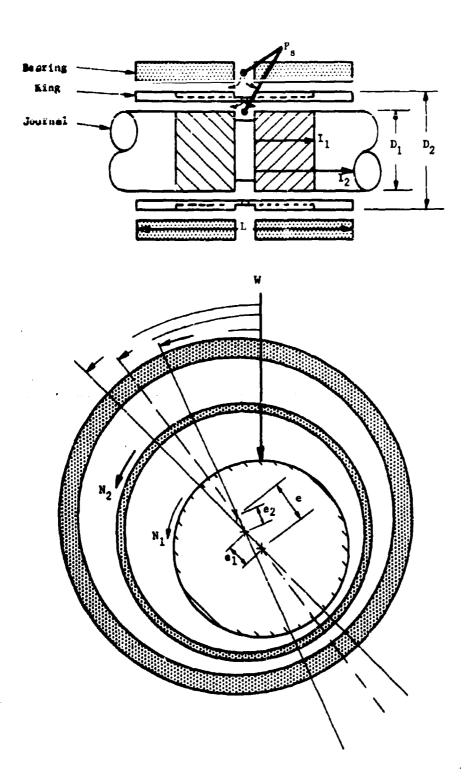


Figure 4. Geometry of Floating Ring Bearing

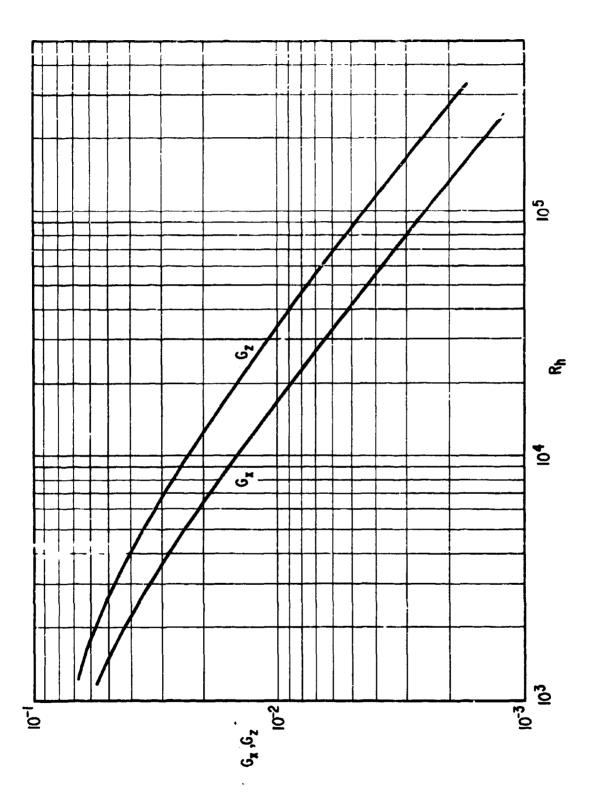


Figure 5. G_x and G_z vs. Local Reynolds Number R_h

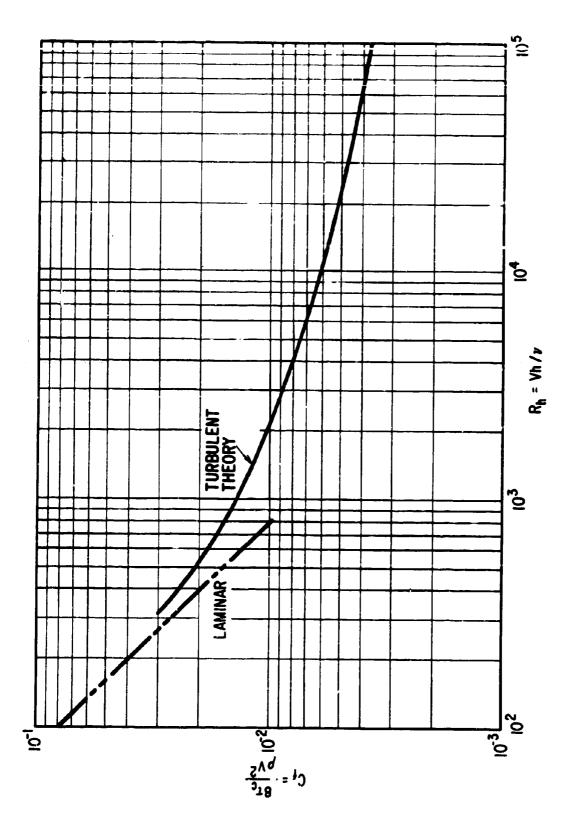


Figure 6. Coefficient of Friction vs. Local Reynolds Number ${\tt R}_{\sf h}$

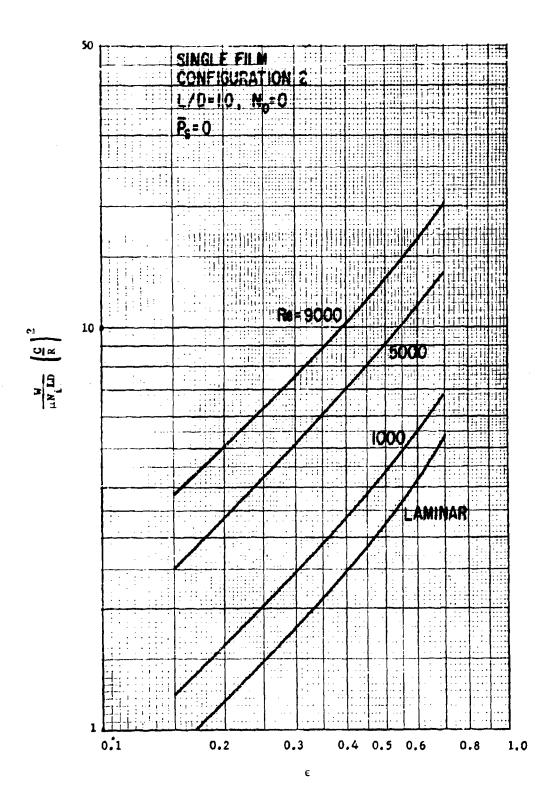


Figure 7. Load vs. Eccentricity, Single Film Bearing

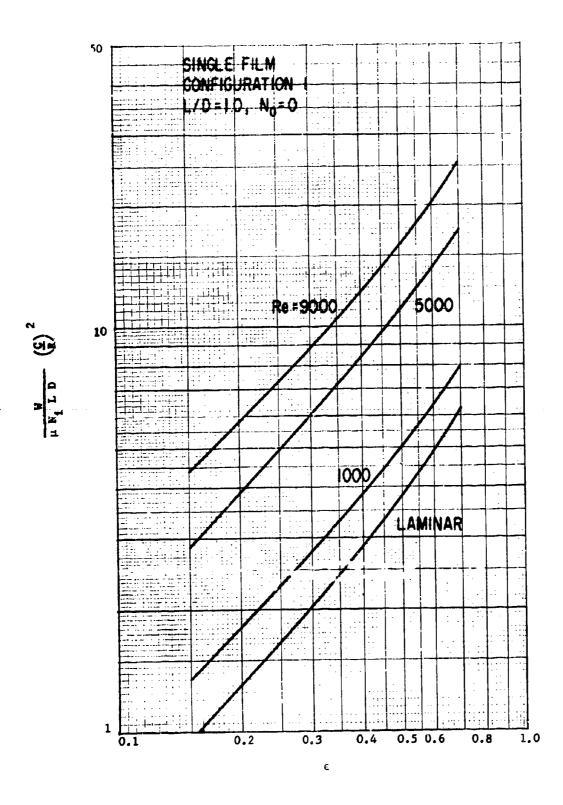


Figure 8. Load vs. Eccentricity, Single Film Bearing

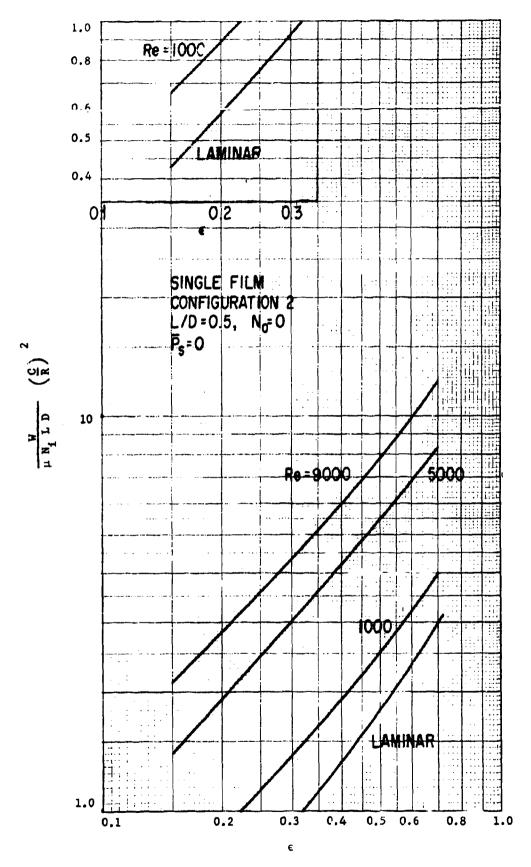


Figure 9. Load vs. Eccentricity, Single Film Bearing

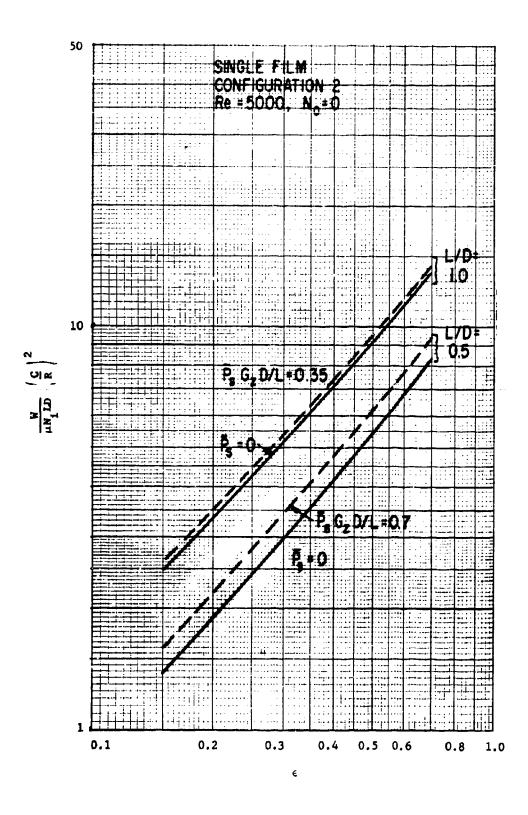


Figure 10. Load vs. Eccentricity, Effect of Pressurization

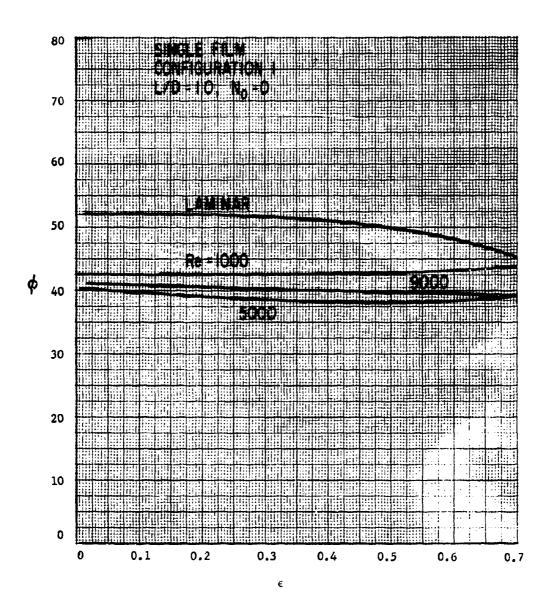


Figure 11. Attitude Angle vs. Eccentricity, Single Film Bearing

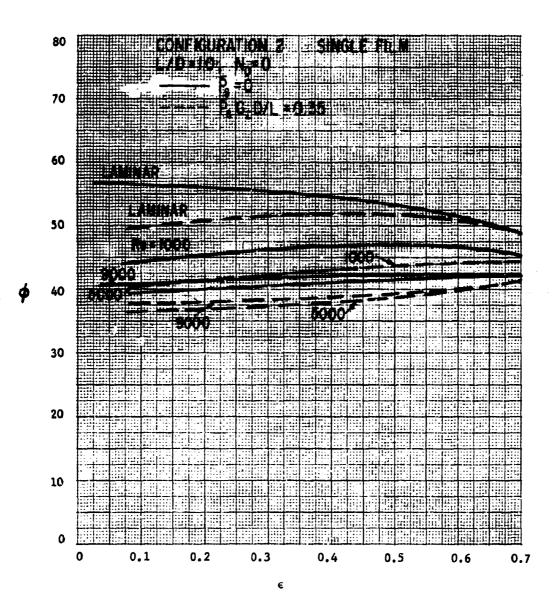


Figure 12. Attitude Angle vs. Eccentricity, Single Film Bearing

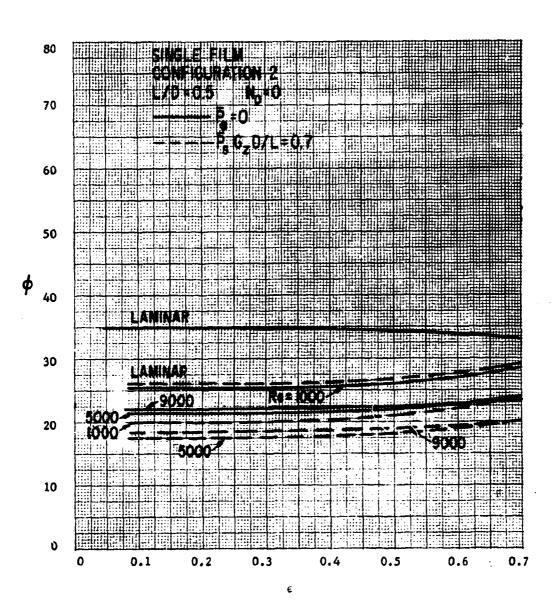


Figure 13. Attitude Angle vs. Eccentricity, Single Film Bearing

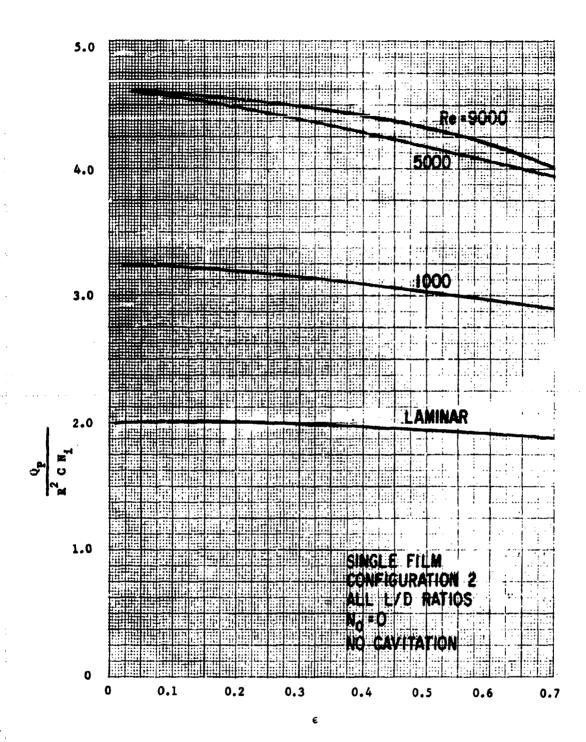


Figure 14. Single Film Bearing Flow Due to Self Pumping Effect of Spiral Grooves

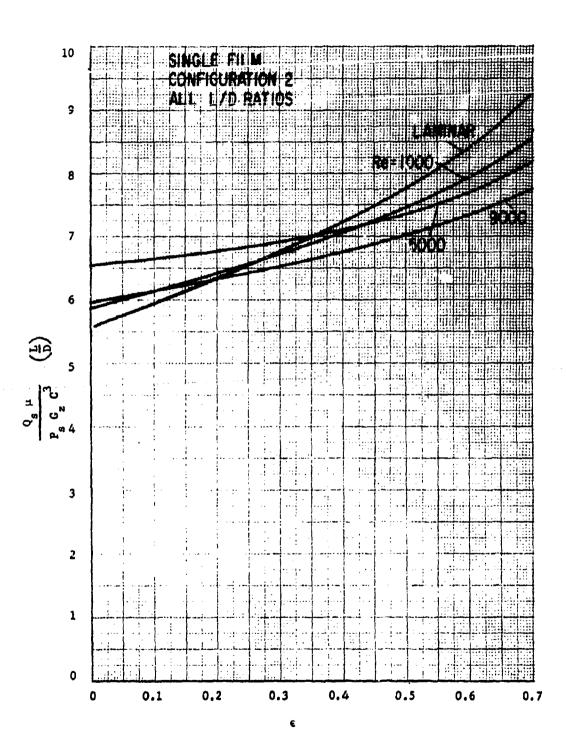


Figure 15. Single Film Bearing Flow Due to Pressurized Supply

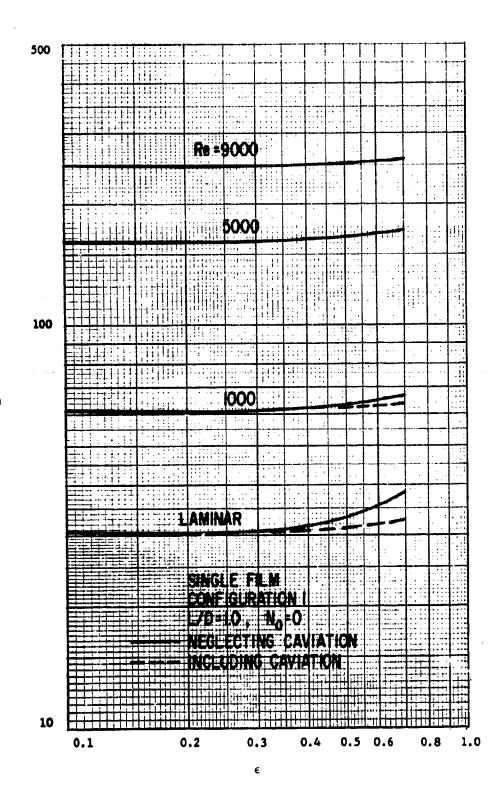


Figure 16. Torque vs. Eccentricity, Single Film Bearing

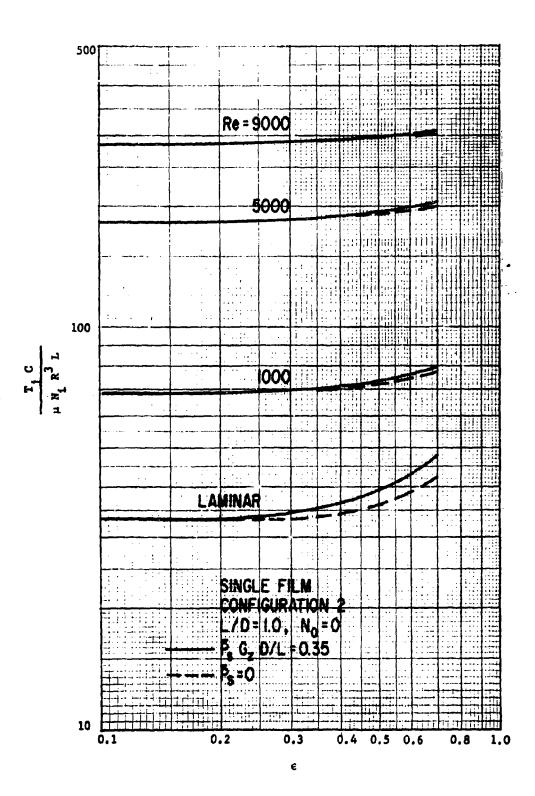


Figure 17. Torque vs. Eccentricity, Single Film Bearing

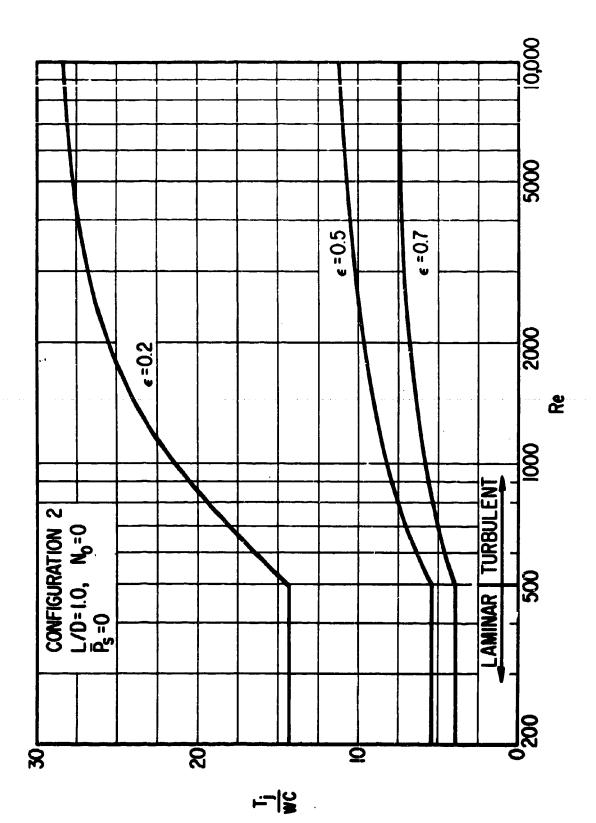


Figure 18. Torque to Load Ratio vs. Reynolds Number, Single Film Bearing

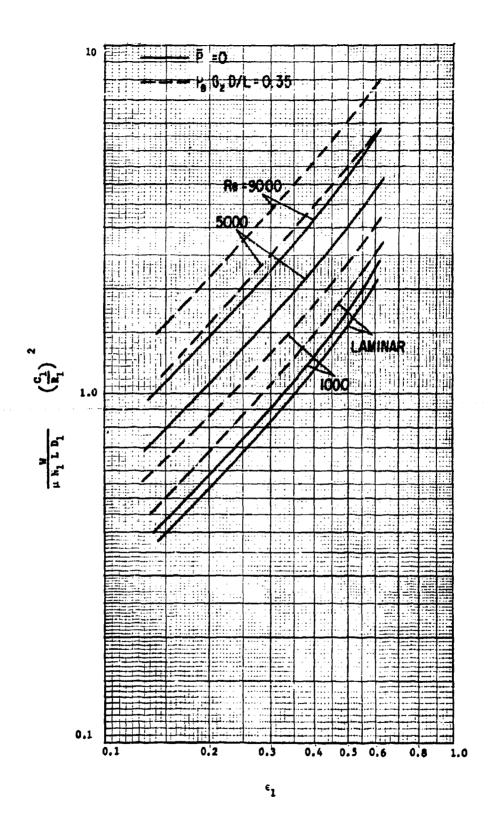


Figure 19. Load vs. Inner Film Eccentricity Ratio, Floating Ring Bearing

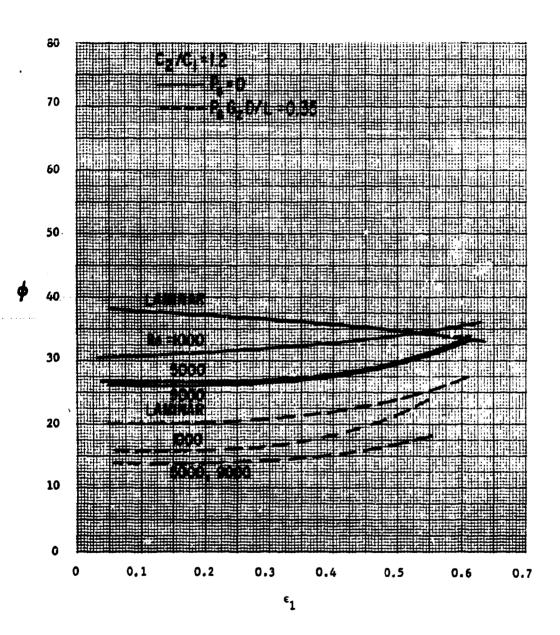


Figure 20. Attitude Angle vs. Inner Film Eccentricity Ratio, Floating Ring Bearing

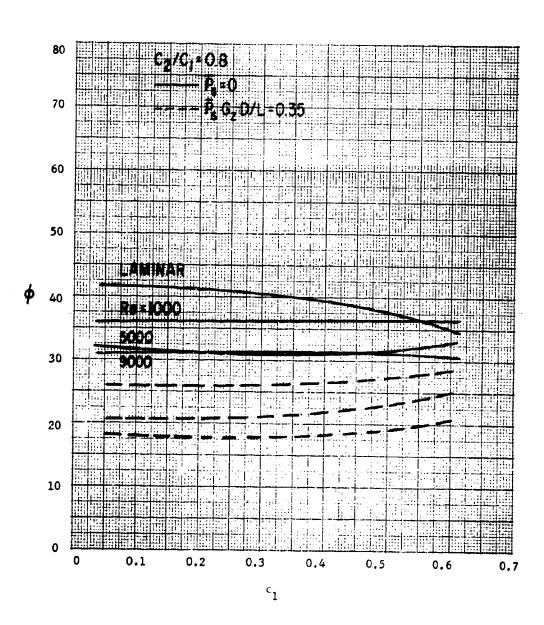


Figure 21. Attitude Angle vs. Inner Film Eccentricity Ratio, Floating Ring Bearing



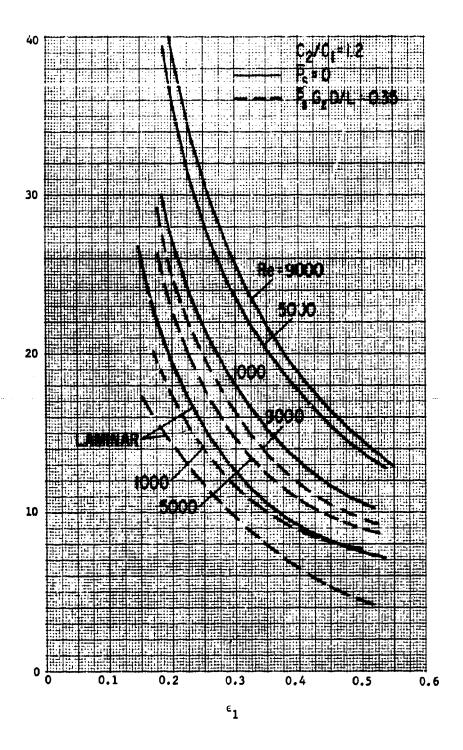


Figure 22. Torque to Load Ratio vs. Inner Film Eccentricity, Floating Ring Bearing

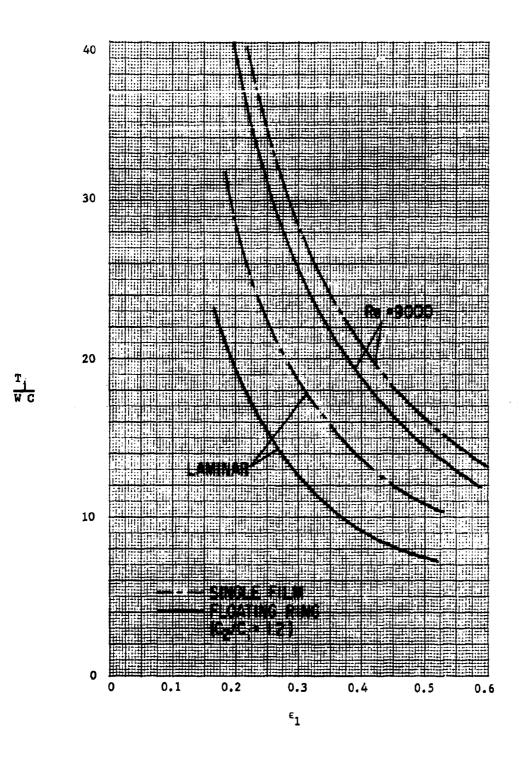


Figure 23. Torque to Load Ratio, Comparison between Single Film and Floating Ring Bearing

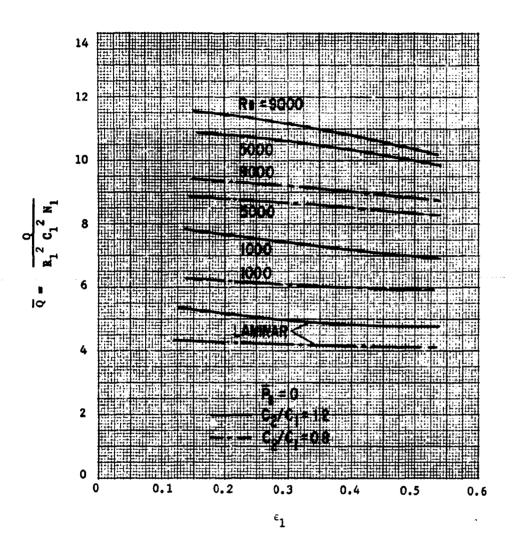


Figure 24. Floating Ring Bearing Flow due to Self-Pumping Effect of Spiral Grooves

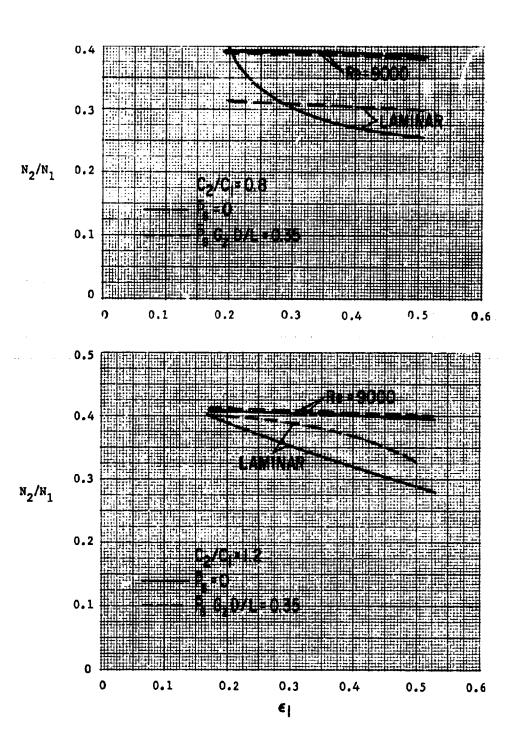


Figure 25. Ring Speed Ratio vs. Inner Film Eccentricity Ratio, Floating Ring Bearing

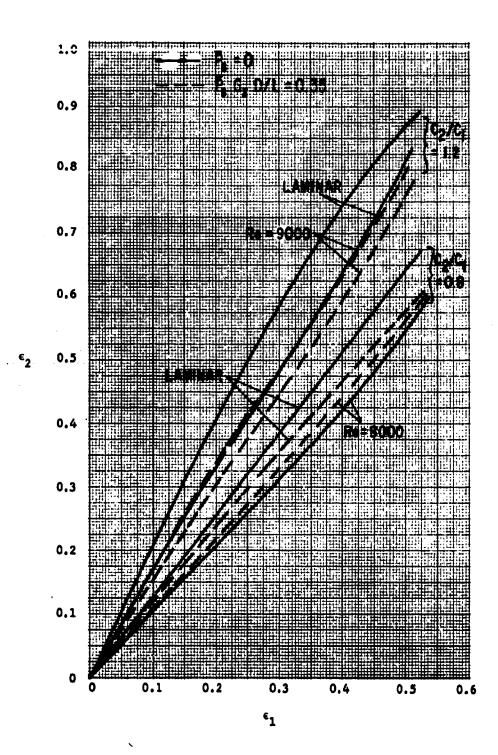


Figure 26. Outer Film Eccentricity Ratio vs. Inner Film Eccentricity Ratio, Floating Ring Bearing

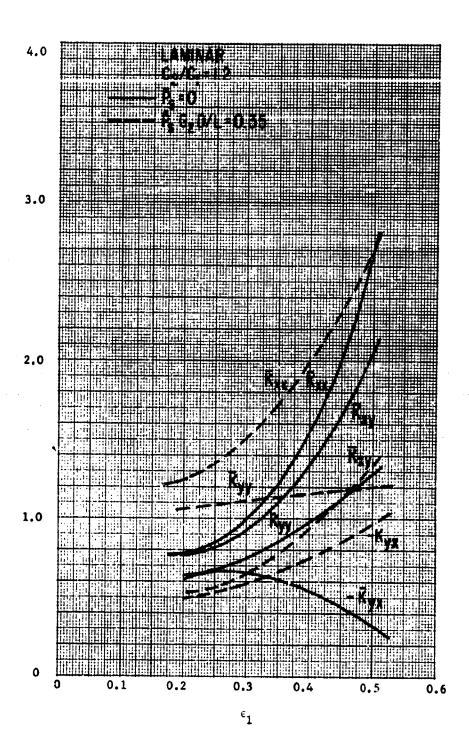


Figure 27. Stiffness Coefficients, Floating Ring Bearing

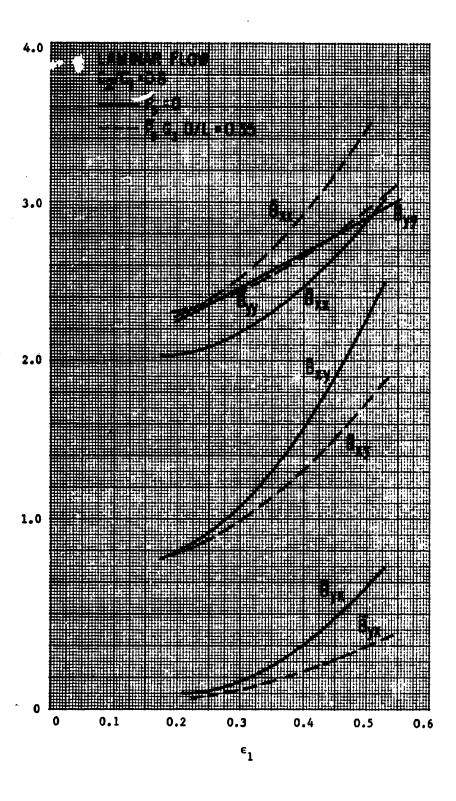


Figure 28. Damping Coefficients, Floating Ring Bearing

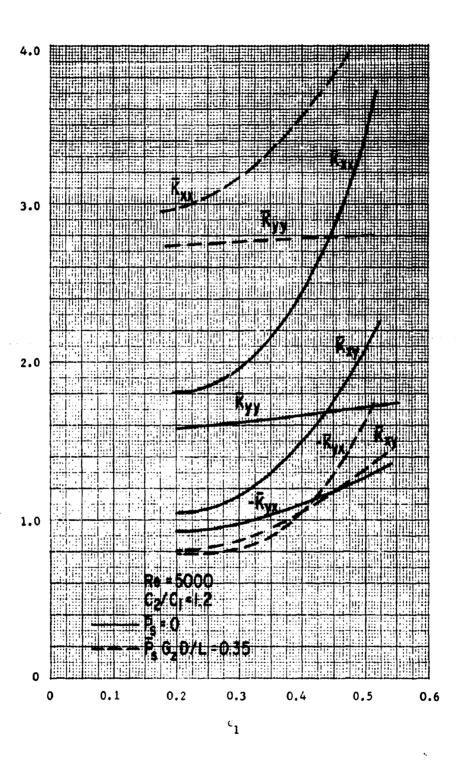


Figure 29. Stiffness Coefficients, Floating Ring Bearing

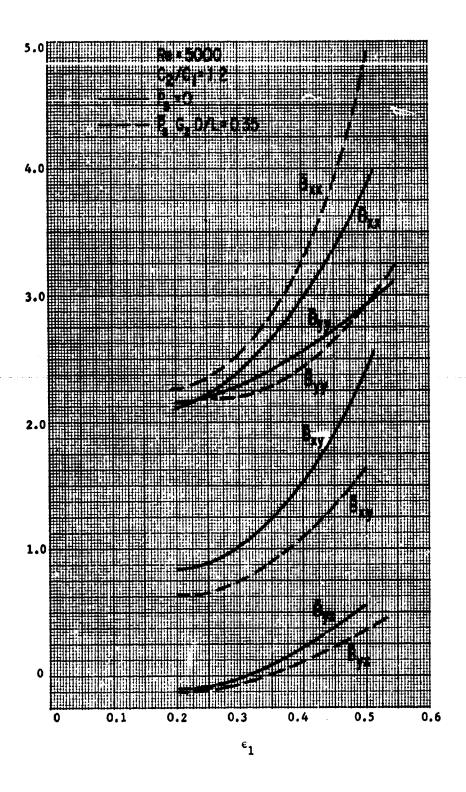


Figure 30. Damping Coefficients, Floating Ring Bearing

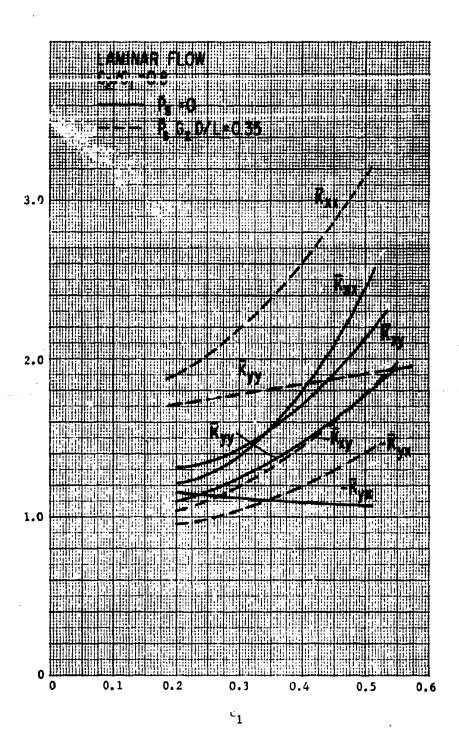


Figure 31. Stiffness Coefficients, Floating Ring Bearing

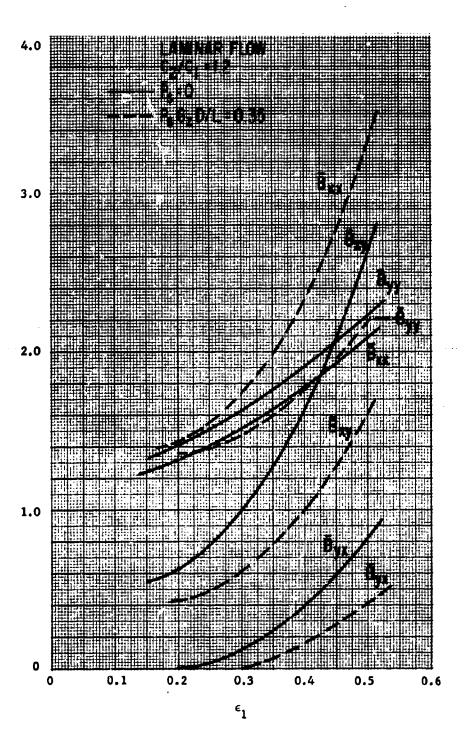


Figure 32. Damping Coefficients, Floating Ring Bearing

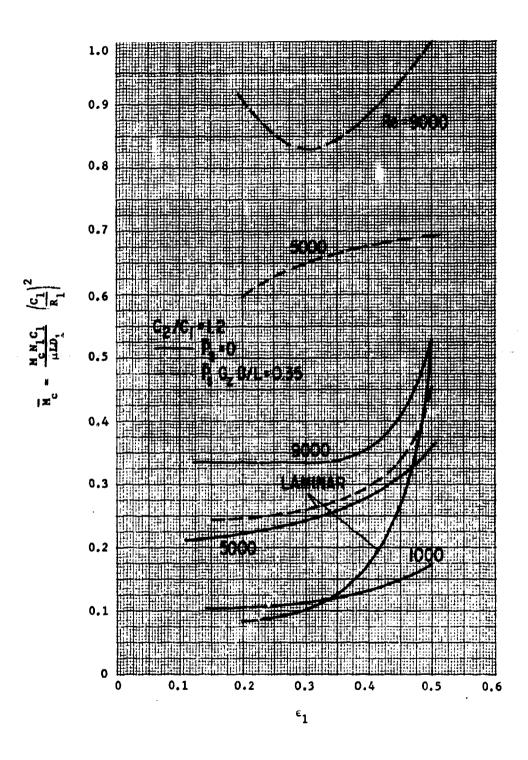


Figure 33. Critical Journal Mass, Floating Ring Bearing

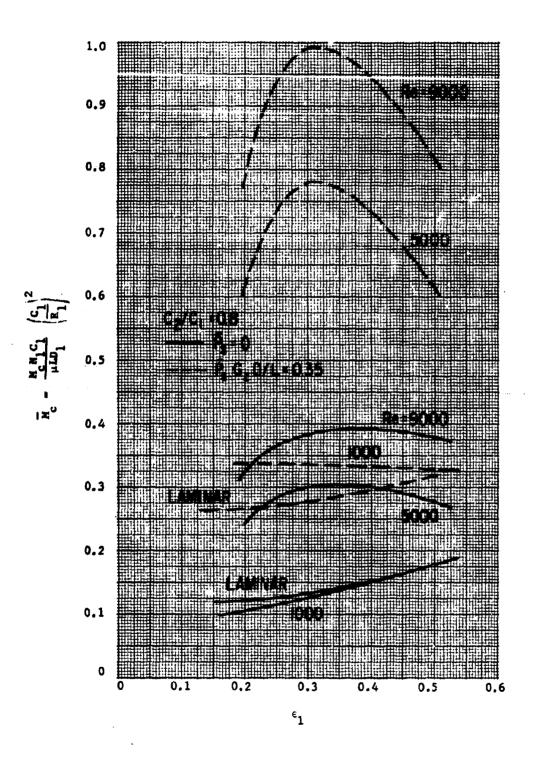


Figure 34. Critical Journal Mass, Floating Ring Bearing

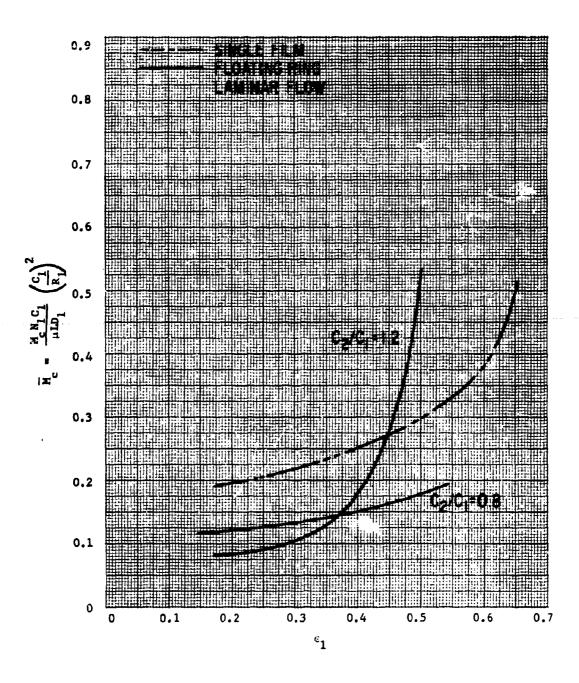


Figure 35. Critical Journal Mass, Comparison between Plain and Spiral-Grooved Floating Ring Bearings

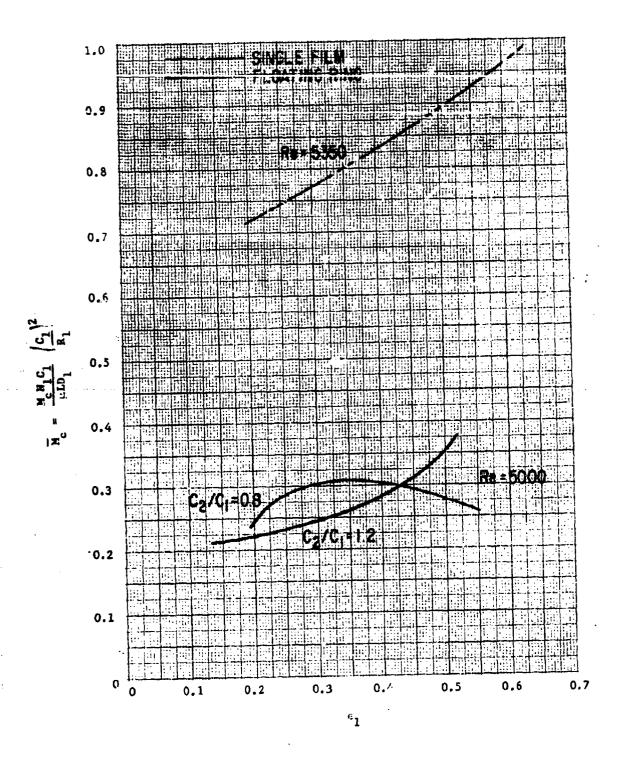


Figure 36. Gritical Journal Mass, Comparison between Plain and Spiral-Grooved Floating King Bearings

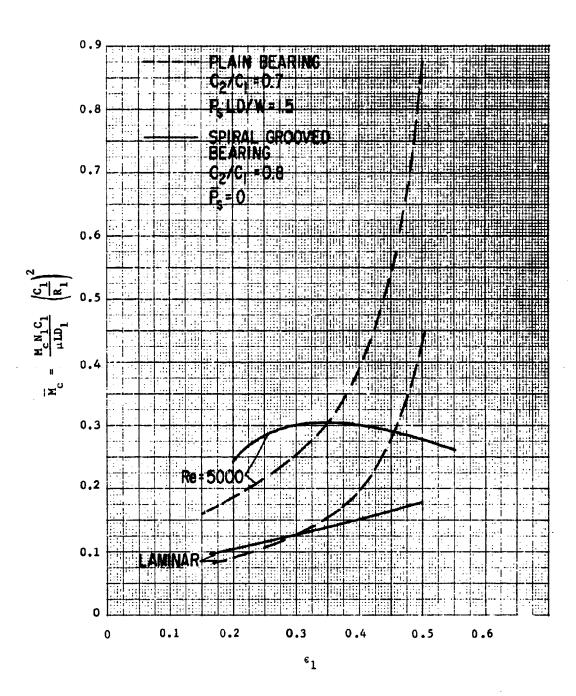


Figure 37. Critical Journal Mass, Comparison between Single Film and Floating Ring Spiral-Grooved Bearings

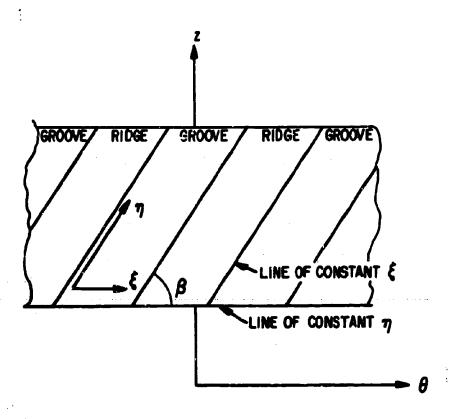


Figure 38. η and ξ Coordinates for Grooved Surface

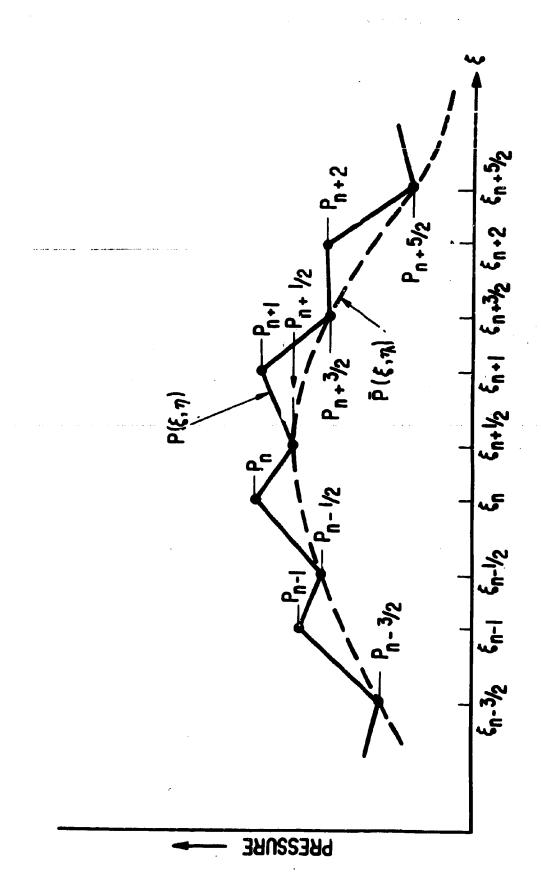


Figure 39. Pressure Distribution around Spiral-Grooved Journal Bearing

MT1-6612

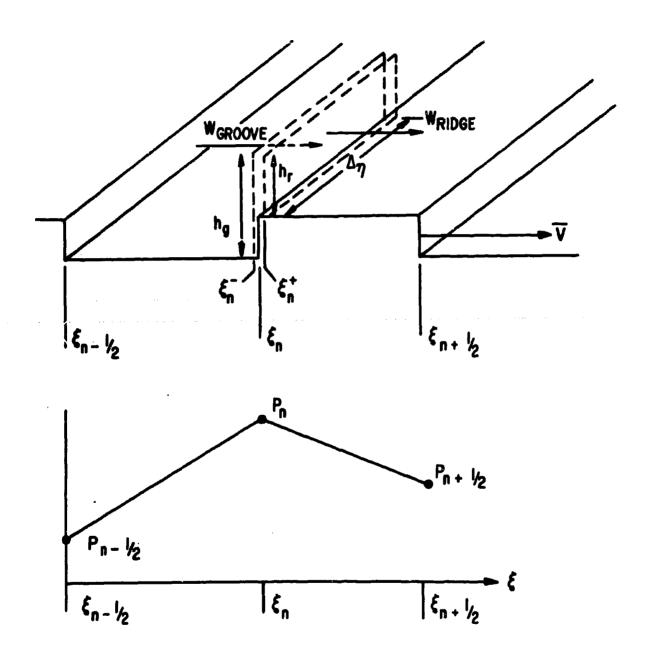


Figure 40. Continuity of Mass Flow across Groove-Ridge Interface and Pressure Variation across Groove-Ridge Pair

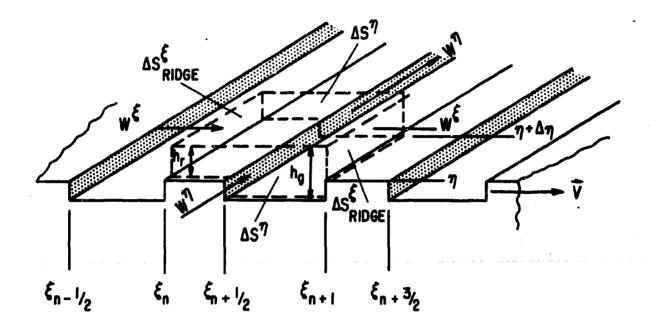


Figure 41. Control Volume for Mass Flow Continuity Analysis

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APPENDIX I

DERIVATION AND SOLUTION OF EQUATION FOR TURBULENT SPIRAL-GROOVED JOURNAL BEARING

The differential equation for the pressure distribution around a spiral-grooved journal bearing has been derived previously by the present authors for the case of laminar flow (Ref. 1). In this appendix will be presented a re-derivation of this equation in which the effects of turbulence in the bearing film will be accounted for by means of the linearized turbulent lubrication theory developed by Ng and Pan (Ref. 4). The derivation will involve four major steps:

- 1. Express the local mass flows in the ridge and groove regions in terms of the local pressure gradients in those two regions.
- Define an "overall" pressure profile around the bearing neglecting the zig-zag ripples in the profile which arise due to the discountinuous groove-ridge geometry.
- 3. Use the requirement that the flow normal to a groove-ridge interface be continuous across the interface in order to solve for local groove-ridge pressure gradients in terms of the "overall" pressure gradient.
- 4. Apply the principle of conservation of mass to obtain a differential equation for the overall pressure profile.

According to the linearized turbulent lubrication theory of Ng and Pan, the local turbulent mass flows in a bearing film can be expressed as

$$\rho = -\frac{\rho h^3 G_x}{\mu} \frac{\partial P}{\partial x} + \rho \frac{(U+V)}{2} h \qquad (51)$$

$$\rho_{Wh} = -\frac{\rho h^3 G_z}{\mu} \frac{\partial P}{\partial z}$$
 (52)

where x and z are the coordinates in the direction of rotation and the axial direction respectively and where U and V are the surface velocities of the bearing and journal respectively. The factors $G_{\rm x}$ and $G_{\rm z}$ can be considered, essentially, to be turbulent viscosity correction factors. In the linearized turbulent lubrication theory $G_{\rm x}$ and $G_{\rm z}$ are considered to be functions of the local Reynolds number, $R_{\rm h}$, in the bearing film where $R_{\rm h} = \rho(V-U)h/\mu$. A plot of $G_{\rm x}$ and $G_{\rm z}$ vs. $R_{\rm h}$ is shown in Fig. 5.

Next, we introduce the "skewed" ξ , η coordinate system shown in Fig. 38 in which lines parallel to groove-ridge interfaces are lines of constant ξ while planes perpendicular to the axis of the bearing are planes of constant η . The relationships between ξ and η and the cylindrical coordinates θ and z are given below

$$\xi = 0 - \frac{z \cot \theta}{R}$$
 (53)

$$\eta = z/\sin\beta$$
 (54)

$$\Theta = \xi + \frac{\eta \cos \theta}{2} \tag{55}$$

$$z = \eta \sin \beta$$
 (56)

note also that

$$\frac{\partial P}{\partial \theta} = \frac{\partial P}{\partial E} \tag{57}$$

$$\frac{\partial P}{\partial z} = \frac{\partial P}{\partial \eta} = \frac{1}{\sin \beta} = \frac{\partial P}{\partial \xi} = \frac{\cot \beta}{1}$$
 (58)

$$\frac{\partial P}{\partial P} = \frac{\partial P}{\partial \theta} \tag{59}$$

$$\frac{\partial P}{\partial \eta} = \frac{\partial P}{\partial \theta} \frac{\cos \theta}{R} + \frac{\partial P}{\partial z} \sin \theta \tag{60}$$

In the ξ , η coordinate system, the pressure gradient $\partial P/\partial \eta$ is continuous everywhere in the bearing film because the geometry has no discontinuities in the η direction. On the other hand, the gradient $\partial P/\partial \xi$ is discontinuous at groove-ridge interfaces due to the discontinuity in (ilm height. Consequently the pressure profile in the & (circumferential)direction will have the "zig-zag" appearance as shown schematically by the solid line in Fig. 39. In this figure the symbols ξ_n , ξ_{n+1} , etc., denote the interfaces at the beginning of ridge region while $\xi_{n+1/2}$, $\xi_{n+3/2}$, etc. denote the interfaces at the beginning of groove regions. Now, by neglecting the saw-toothed ripples in the actual pressure distribution, one can conceive of an approximate, smoothed "overall" pressure distribution around the journal shown in Fig. 39 as the dashed line through the pressures $P_{n-3/2}$, $P_{n-1/2}$, etc., at $\xi_{n-3/2}$, $\xi_{n-1/2}$, etc. Since the local pressure gradients within each groove and ridge region are bounded in magnitude the saw-toothed fluctuations in pressure due to alternating groove and ridge regions will reduce to a negligible magnitude as the width of the groove-ridge pair becomes very small, i.e., as the number of grooves becomes very large. In the limit, as the width of each groove-ridge pair becomes very small, the smooth "overall" pressure distribution through the discrete points $P_{n-3/2}$, $P_{n-1/2}$, etc., will approach ρ continuous distribution $P(\xi,\eta)$ which should provide a very good approximation to the actual "saw-toothed" pressure distribution around the journal. Formally, one can define the slope of $P(\xi,\eta)$ in the ξ direction at the point ξ_n , as

$$\frac{\partial \overline{P}(\xi,\eta)}{\partial \xi} \bigg|_{\xi_n} = \lim_{\Delta \xi \to 0} \frac{P_{n+1/2} - P_{n-1/2}}{\Delta \xi} = \lim_{\Delta \xi \to 0} \left[\alpha \frac{\partial P_g}{\partial \xi} + (1-\alpha) \frac{\partial P_g}{\partial \xi} \right]$$
(61)

where $\Delta \xi = \xi_{n+1/2} - \xi_{n-1/2}$ and where $\partial P_g/\partial \xi$ and $\partial P_r/\partial \xi$ refer to the local pressure gradients within the groove and ridge region respectively.

Having defined the overall gradient $\partial P/\partial \xi$, we next consider writing an expression for the mass flux W^{ξ} normal to a moving groove-ridge interface (see Fig. 39). In terms of the mass fluxes puh and ρ wh, W^{ξ} is expressed as

$$\mathbf{W}^{\xi} = \rho \left[(\mathbf{u} - \mathbf{V}) \sin \beta - \mathbf{w} \cos \beta \right] \mathbf{h}$$
 (62)

Substituting for u and w in Eq. (62) by means of Eqs. (51) and (52) and noting that $\partial P/\partial x = \partial P/R\partial \theta$ we obtain

Wgroove region =
$$-\rho \left\{ \frac{h_g^3 G_{xg}}{\mu} \frac{\partial P_g}{\partial \theta} - \frac{(U-V)}{2} h_g \right\} \sin \beta$$

$$- \frac{h_g^3 G_{gg}}{\mu} \frac{\partial P_g}{\partial \theta} \cos \beta$$
(63)

Wridge region =
$$-\rho \left(\frac{h_x^3 G_{xx}}{\mu} \frac{\partial P_x}{R\partial \theta} - \frac{(U-V)}{2} h_x \right) \sin \beta$$

$$-\frac{h_{r}^{3}G_{r}}{\mu}\frac{\partial P_{r}}{\partial z}\cos\beta$$
(64)

Note that the factors G_{χ} and G_{g} are subscripted r and g because they have different values in the ridge and groove regions.

Next we make the following useful definitions

$$G_1 = 12(G_x + G_z \cot^2 \beta)/R^2$$
 (65)

$$G_2 = -\frac{12G_2 \cos \beta}{R \sin^2 \beta} \tag{66}$$

$$G_3 = -\frac{12 G_2}{e^{4n^2 R}} \tag{67}$$

If, in Eqs. (63) and (64), we transform the derivatives of P with respect to 9 and z into derivatives with respect to ξ and η (see Eqs. (57) and (58)) and collect terms, we obtain

$$\mathbf{w}_{\text{groove region}}^{\xi} = \mathbf{R} \sin \beta \left\{ -\frac{\rho}{12\mu} h_{\mathbf{g}}^{3} \left[G_{1\mathbf{g}} \frac{\partial \mathbf{P}_{\mathbf{g}}}{\partial \xi} + G_{2\mathbf{g}} \frac{\partial \mathbf{P}}{\partial \eta} \right] + \rho h_{\mathbf{g}} \frac{(\mathbf{U} - \mathbf{V})}{2\mathbf{R}} \right\}$$
(68)

$$\psi_{\text{ridge region}}^{\xi} = \mathbb{R} \sin \beta \left\{ -\frac{\rho}{12\mu} h_r^3 \left[G_{1r} \frac{\partial P_r}{\partial \xi} + G_{2r} \frac{\partial P}{\partial \eta} \right] + \rho h_r \frac{(U-V)}{2R} \right\}$$
(69)

Note that the derivative $\partial P/\partial \eta$ does not have to be identified by a subscript g or r since it is continuous everywhere within the bearing film.

Next we note that by continuity of mass flow

Eqs. (61) and (70) constitute two linear equations in the "unknowns" $\partial P_g/\partial \xi$ and $\partial P_p/\partial \xi$. Eqs. (61) and (70) may therefore be solved to yield

$$\frac{\partial P}{\partial \xi} = (1-\alpha) \, \overline{B}_1 \, \frac{\partial P}{\partial \eta} + (1-\alpha) \, \overline{B}_2 \, - \, \overline{A}_1 \, \frac{\partial \overline{P}}{\partial \xi} \tag{71}$$

$$\frac{\sum_{\mathbf{r}}^{\mathbf{p}}}{\partial \xi} = -\alpha \overline{B}_{1} \frac{\partial \mathbf{p}}{\partial \eta} - \alpha \overline{B}_{2} + \overline{A}_{2} \frac{\partial \overline{\mathbf{p}}}{\partial \xi}$$
 (72)

where

$$A_{1} = G_{1r} h_{r}^{3}$$

$$A_{2} = G_{1g} h_{g}^{3}$$

$$A_{3} = A_{2} - \alpha(A_{2} + A_{1})$$

$$B_{1} = G_{2g} h_{g}^{3} - G_{2r} h_{r}^{3}$$

$$B_{2} = \frac{6\mu(h_{r} - h_{g})}{R} (U - V)$$

$$\overline{A}_{1} = A_{1}/A_{3}$$

$$\overline{B}_{1} = B_{1}/A_{3}$$

$$(73)$$

Eqs. (71) and (72) may be substituted in either Eq. (68) or (67) to yield an expression for the mass flux \mathbf{W}^{ξ} in terms of the overall pressure gradients $\partial P/\partial \xi$ and $\partial P/\partial \eta$ (note that $\partial P/\partial \eta$ may be written as $\partial P/\partial \eta$ because of the continuous nature of this derivative). The expression obtained is

$$w^{\xi} = R \sin \beta \left\{ -\frac{\rho}{12\mu} h_{r}^{3} \left[G_{1r} \left(\overline{A}_{2} \frac{\partial \overline{P}}{\partial \xi} - \alpha \overline{B}_{1} \frac{\partial \overline{P}}{\partial \eta} - \alpha \overline{B}_{2} \right) + G_{2r} \frac{\partial \overline{P}}{\partial \eta} \right] + \rho h_{r} \frac{(U-V)}{2R} \right\}$$

$$(74)$$

Next, consider the control volume ΔV , for one ridge-groove pair shown in Fig. 41. We take the control volume to move with the grooved surface at velocity \vec{V} and we consider that, at the instant shown in Fig. 41, the various ridge-groove interfaces are located at ξ_n , $\xi_{n+1/2}$, ξ_{n+1} etc., as depicted. The mass flows entering and leaving the moving control volume through the surfaces ΔS_{ridge}^{ξ} we denote as V_{ridge}^{ξ} whereas the mass flows entering and leaving the control volume through the surfaces ΔS_{ridge}^{η} we denote as V_{ridge}^{η} . The total time rate of change of the mass, ΔM contained in ΔV is given by

$$\frac{\partial}{\partial t} (\Delta M) + V \cdot \nabla (\Delta M)$$
 (75)

By the conservation of mass we obtain that

$$\begin{bmatrix} w_{\text{ridge}}^{\xi} \Big|_{\xi_{n+1}} - w_{\text{ridge}}^{\xi} \Big|_{\xi_{n}} \end{bmatrix} \Delta \eta + \begin{bmatrix} w^{\eta} \Big|_{\eta + \Delta \eta} - w^{\eta} \Big|_{\eta} \end{bmatrix} \begin{pmatrix} \xi_{n+1} - \xi_{n} \end{pmatrix} + \frac{\partial}{\partial t} (\Delta M) + \vec{v} \cdot \vec{\nabla} (\Delta M) = 0$$
 (76)

Dividing Eq. (76) through by $\Delta \xi \Delta \eta$ where $\Delta \xi = \xi_{n+1} - \xi_n$, and taking the limit as $\Delta \xi$ and $\Delta \eta$ go to zero we have

$$\frac{\partial w^{\xi}}{\partial \xi} + \frac{\partial w^{\eta}}{\partial \eta} + \frac{\partial}{\partial t} \frac{(\Delta M)}{\Delta \xi} + \vec{V} \cdot \vec{\nabla} \frac{(\Delta M)}{\Delta \xi} = 0$$
 (77)

where W5/8 is defined to be

$$\frac{\partial \mathbf{w}^{\xi}}{\partial \xi} = \lim_{\substack{\Lambda \xi = 0}} \frac{\mathbf{w}^{\xi} \left| \xi_{n+1} - \mathbf{w}^{\xi} \right| \xi_{n}}{\Delta \xi} \tag{78}$$

The subscript <u>ridge</u> has been dropped from W^{ξ} because of the equality condition expressed by Eq. (70). The expression for W^{ξ} is given by equation (74).

The expression for the mass flux W^{η} is

$$\mathbf{W}^{\eta} = -\rho \left[\frac{(1-\alpha)h_x^3}{\mu} \frac{\partial P_x}{\partial z} \mathbf{G}_{zx} + \frac{\alpha h_x^3}{\mu} \frac{\partial P_g}{\partial z} \mathbf{G}_{zg} \right]$$
 (79)

If we transform $\partial P_{\chi}/\partial z$ and $\partial P_{g}/\partial z$ into $\xi = \eta$ coordinates by means of Eq. (58) we will obtain an expression for W^{η} in terms of $\partial P/\partial \eta$, $\partial P_{\chi}/\partial \xi$ and $\partial P_{g}/\partial \xi$. We then can substitute for $\partial P_{\chi}/\partial \xi$ and $\partial P_{g}/\partial \xi$ by means of Eqs. (71) and (72) to obtain, finally

$$W^{\eta} = \mathbf{R} \sin \beta \frac{\alpha}{12\mu} \left\{ \alpha h_g^{3} \left[G_{3g} \frac{\partial \overline{P}}{\partial \eta} - G_{2g} \left(-\overline{A}_{1} \frac{\partial \overline{P}}{\partial \xi} + (1-\alpha) \overline{B}_{1} \frac{\partial \overline{P}}{\partial \eta} + (1-\alpha) \overline{B}_{2} \right) \right] + (1-\alpha)h_g^{3} \left[G_{3g} \frac{\partial \overline{P}}{\partial \eta} - G_{2g} \left(\overline{A}_{2} \frac{\partial \overline{P}}{\partial \xi} - \alpha \overline{B}_{1} \frac{\partial \overline{P}}{\partial \eta} - \alpha \overline{B}_{2} \right) \right] \right\}$$
(80)

where \overline{A}_2 , \overline{B}_1 and \overline{B}_2 were defined previously by Eqs. (73)

The quantity AM/AEAn in Eq. (77) is

$$\frac{\Delta M}{\Delta \xi \Delta \eta} = \rho R \sin \beta \left[(1-\alpha)h_x + \alpha h_g \right]$$
 (61)

while

$$\vec{V} \cdot \vec{\nabla} = \frac{V}{R} \frac{\partial}{\partial \xi} \tag{82}$$

Substitution of Eqs. (74), (80), (81) and (82) into Eq. (77) yields a second-order differential equation in $P(\xi,\eta)$ the overall pressure distribution around the spiral-grooved journal. To solve this equation, we must first transform it back into the orthogonal 9-z coordinate system. This is done by means of Eqs. (59) and (60). The result is

$$\frac{\partial \mathbf{w}^{\xi}}{\partial \theta} + \frac{\cos \beta}{R} \frac{\partial \mathbf{w}^{\eta}}{\partial \theta} + \sin \beta \frac{\partial \mathbf{w}^{\eta}}{\partial z}$$

$$+ \left(\frac{\partial}{\partial t} + \frac{\mathbf{v}}{R} \frac{\partial}{\partial \theta} \right) \left(R \rho \sin \beta \left[\alpha \, h_g + (1-\alpha) h_g \right] \right) = 0$$
(83)

Expressions for W^{ξ} and W^{η} in the 0-z coordinate system may be obtained by substituting Eqs. (59) and (60) into Eqs. (74) and (80).

The Numerical Solution

Eq. (83) is solved for any combination of groove and seal arrangement with or without feed or vent in the middle of the journal (Fig. 2). Thus, it can provide the solution for a seal-groove, groove-seal, fully grooved or herringbone journal containing up to three distinct sections. The basic technique is first to divide the bearing into a numerical grid with dimensions man. Then write the differential equation into a finite difference form of three columns. Thus, each point in concern is related to the five neighboring points. At the boundaries, the pressures are given. Therefore man equations are established for man unknowns. By means of the columnwise matrix inversion solution routine developed by Castelli, Pirvics and Shapiro, the pressure field is obtained.

This technique is fully discussed in References 6 and 7.

Once the pressure field is obtained, loads, moments, torques, etc. are obtained by numerically evaluating the following expressions.

Radial component of force (cosine component)

$$\mathbf{F}_{\mathbf{r}} = -\int_{0}^{\mathbf{I}} \int_{0}^{2\pi} (\overline{\mathbf{P}} - \mathbf{P}_{\mathbf{g}}) \mathbf{R} \cos \theta \, d\theta \, dz \qquad (84)$$

Tangential component of force (sine component)

$$P_{t} = \int_{0}^{L} \int_{0}^{2\pi} (\overline{P} - P_{a}) R \sin \theta d\theta ds \qquad (85)$$

Redial component of moment (cosine component)

$$M_{r} = -\int_{0}^{L} \int_{0}^{2\pi} (\overline{P} - P_{\underline{a}}) \operatorname{Re} \cos \theta \, d\theta \, dz \qquad (86)$$

Tangential component of moment (sine component)

$$M_{t} = \int_{0}^{L} \int_{0}^{2\pi} (\widetilde{P} - P_{a}) \operatorname{Rz sin } \theta \ d\theta \ dz$$
 (87)

Attitude angles

$$\phi = \tan^{-1} \frac{F_{r}}{F_{t}}, \quad \phi' = \tan^{-1} \frac{M_{r}}{M_{t}}$$
 (88)

Bearing torque

$$T_{B} = \frac{Ro(U-V)^{2}}{8} \int_{0}^{z} \int_{0}^{2\pi} C_{f} Rd\theta dz + \frac{R}{2} \int_{0}^{z} \int_{0}^{2\pi} h \frac{\partial P}{\partial \theta} d\theta dz \qquad (89)$$

where C_f is the Couette friction factor which is plotted in Fig. 6 sgainst $R_{h\,e}$ $\partial P/\partial \theta$ is the local pressure gradient. By Eqs. (71), (72), (59) and (60) the second term of Equation (89), the Poissuille torque, can be written in terms of the overall pressure gradients.

$$\frac{R}{2} \int_{0}^{\pi} \int_{0}^{2\pi} d\theta d\theta dz = \frac{R}{2} \int_{0}^{\pi} \left\{ \alpha h_{g} \left[(1-\alpha)\overline{B}_{1} \left(\frac{\partial \overline{P}}{\partial z} + \frac{\cot \beta}{R} \frac{\partial \overline{P}}{\partial \theta} \right) \sin \beta + (1-\alpha)\overline{B}_{2} - \overline{A}_{1} \frac{\partial \overline{P}}{\partial \theta} \right] + (1-\alpha)h_{r} \left[\overline{A}_{2} \frac{\partial \overline{P}}{\partial \theta} - \alpha \overline{B}_{1} \left(\frac{\partial \overline{P}}{\partial z} + \frac{\cot \beta}{R} \frac{\partial \overline{P}}{\partial \theta} \right) \sin \beta \right]$$

$$- \alpha \overline{B}_{2} \right] dz \qquad (90)$$

Journal torque

$$T_1 = T_B + \epsilon C W \sin \epsilon$$

(91)

Where W = load =
$$\sqrt{\mathbf{F}_{r}^{2} + \mathbf{F}_{t}^{2}}$$

Flow

$$Q = R \int_{0}^{2\pi} W^{\eta} d\theta$$

(92)

where \mathbf{W}^{η} is defined by Eq. (80).

APPENULA LL

DERIVATION OF RELATIONSHIPS FOR

CALCULATING STIFFNESS AND DAMPING COEFFICIENTS

Consider the reference axes shown in Fig. 3. The relationship between the forces $\mathbf{F}_{\mathbf{x}}$ and $\mathbf{F}_{\mathbf{y}}$ and the forces $\mathbf{F}_{\mathbf{r}}$ and $\mathbf{F}_{\mathbf{t}}$ can be written in matrix form as

For an infinitesimally small motion around the steady state position the dynamic forces become

The infinitesimal dynamic motion of the journal center is described by the coordinates (x,y):

$$x = d(e \cos \phi)$$
 $y = d(e \sin \phi)$

or

$$\begin{pmatrix}
de \\
ed\phi
\end{pmatrix} = \begin{pmatrix}
\cos \phi & \sin \phi \\
-\sin \phi & \cos \phi
\end{pmatrix} \cdot \begin{pmatrix}
\pi \\
y
\end{pmatrix}$$
(95)

The velocities transform similarly:

If, in the differential equation for pressure P obtained in Appendix I, we introduce the following dimensionless variables

we obtain the result that the dimensionless pressure P in a spiral-grooved bearing of fixed geometry is a function only of the dimensionless variables ϵ , ϵ/ω and δ/ω i.e.

$$\overline{P} = \overline{P} \left(\epsilon, \frac{\epsilon}{60}, \frac{\epsilon}{60} \right). \tag{98}$$

The resulting fluid film forces in radial and tangential directions are:

$$F_{r} = -\lambda \omega \iint \overline{P} \cos \theta \, dx' \, dz'$$

$$= \lambda \omega \overline{F}_{r} \left(\varepsilon, \frac{\dot{\varepsilon}}{\omega}, \frac{\dot{\theta}}{\omega} \right)$$

$$F_{t} = \lambda \omega \iint \overline{P} \sin \theta \, dx' \, dz'$$

$$= \lambda \omega \overline{F}_{t} \left(\varepsilon, \frac{\dot{\varepsilon}}{\omega}, \frac{\dot{\theta}}{\omega} \right)$$
(100)

where:

$$\lambda = \frac{\mu R L}{\pi} \left(\frac{R}{C} \right)^{2}$$

$$\overline{F}_{r} = \frac{F_{r}}{\mu NDL} \left(\frac{C}{R} \right)^{2}$$

$$(101)$$

$$\overline{F}_{t} = \frac{F_{t}}{\mu NDL} \left(\frac{C}{R} \right)^{2}$$

Differentiating Eqs. (99) and (100) we obtain

$$dF_{r} = \frac{\lambda \omega}{C} \left[\frac{\partial \overline{F}_{r}}{\partial \varepsilon} de + \frac{1}{\omega} \frac{\partial \overline{F}_{r}}{\partial (\frac{\varepsilon}{\omega})} d\dot{e} + \frac{1}{\varepsilon \omega} \frac{\partial \overline{F}_{r}}{\partial (\frac{\varepsilon}{\omega})} e d\dot{e} \right]$$
(102)

$$dF_{t} = \frac{\lambda m}{C} \left[\frac{\partial F}{\partial \epsilon} de + \frac{1}{\omega} \frac{\partial F}{\partial \epsilon} de + \frac{1}{\omega} \frac{\partial F}{\partial \epsilon} de + \frac{1}{\omega} \frac{\partial F}{\partial \epsilon} e de \right]$$
(103)

By substitution of Eqs. (102 and (103) into Eq. (94)

$$\begin{pmatrix}
dF_{x} \\
dF_{y}
\end{pmatrix} = -\frac{1}{C}\lambda\omega
\begin{pmatrix}
\cos \phi & \sin \phi \\
\sin \phi - \cos \phi
\end{pmatrix}$$

$$\begin{pmatrix}
\frac{\partial F_{x}}{\partial \varepsilon} & \frac{F_{x}}{\varepsilon} \\
\frac{\partial F_{x}}{\partial \varepsilon} & \frac{F_{x}}{\varepsilon}
\end{pmatrix}
\begin{pmatrix}
de \\
\frac{\partial F_{x}}{\partial \varepsilon} & \frac{\partial F_{x}}{\partial \varepsilon} & \frac{\partial F_{x}}{\partial \varepsilon} \\
\frac{\partial F_{x}}{\partial \varepsilon} & \frac{\partial F_{x}}{\partial \varepsilon} & \frac{\partial F_{x}}{\partial \varepsilon}
\end{pmatrix}
\begin{pmatrix}
\frac{\partial F_{x}}{\partial \varepsilon} & \frac{\partial F_{x}}{\partial \varepsilon} \\
\frac{\partial F_{x}}{\partial \varepsilon} & \frac{\partial F_{x}}{\partial \varepsilon} & \frac{\partial F_{x}}{\partial \varepsilon}
\end{pmatrix}
\begin{pmatrix}
\frac{\partial F_{x}}{\partial \varepsilon} & \frac{\partial F_{x}}{\partial \varepsilon} \\
\frac{\partial F_{x}}{\partial \varepsilon} & \frac{\partial F_{x}}{\partial \varepsilon} & \frac{\partial F_{x}}{\partial \varepsilon}
\end{pmatrix}
\begin{pmatrix}
\frac{\partial F_{x}}{\partial \varepsilon} & \frac{\partial F_{x}}{\partial \varepsilon} \\
\frac{\partial F_{x}}{\partial \varepsilon} & \frac{\partial F_{x}}{\partial \varepsilon} & \frac{\partial F_{x}}{\partial \varepsilon}
\end{pmatrix}
\begin{pmatrix}
\frac{\partial F_{x}}{\partial \varepsilon} & \frac{\partial F_{x}}{\partial \varepsilon} & \frac{\partial F_{x}}{\partial \varepsilon} \\
\frac{\partial F_{x}}{\partial \varepsilon} & \frac{\partial F_{x}}{\partial \varepsilon} & \frac{\partial F_{x}}{\partial \varepsilon}
\end{pmatrix}
\begin{pmatrix}
\frac{\partial F_{x}}{\partial \varepsilon} & \frac{\partial F_{x}}{\partial \varepsilon} & \frac{\partial F_{x}}{\partial \varepsilon} \\
\frac{\partial F_{x}}{\partial \varepsilon} & \frac{\partial F_{x}}{\partial \varepsilon} & \frac{\partial F_{x}}{\partial \varepsilon} & \frac{\partial F_{x}}{\partial \varepsilon}
\end{pmatrix}
\begin{pmatrix}
\frac{\partial F_{x}}{\partial \varepsilon} & \frac{\partial F$$

The stiffness and damping coefficients are defined by:

$$dF_{x} = -K_{xx} - B_{xx} - K_{xy} - B_{xy}$$

$$dF_{y} = -K_{yx} - K_{yx} - K_{yy} - B_{yy}$$
(105)

To determine the 8 coefficients, substitute Eq. (95) and (96) into Eq. (104) and collect the terms in accordance with Eq. (105) to get:

$$K_{XX} = \frac{1}{C} \lambda \omega \left[\frac{\partial \overline{F}_{x}}{\partial c} \cos^{2} \phi + \frac{\partial \overline{F}_{y}}{\partial c} \cos \phi \sin \phi - \frac{\overline{F}_{y}}{c} \sin \phi \right]$$

$$\omega B_{XX} = \frac{1}{C} \lambda \omega \left[\frac{\partial \overline{F}_{x}}{\partial (\frac{c}{\omega})} \cos^{2} \phi + \frac{\partial \overline{F}_{y}}{\partial (\frac{c}{\omega})} \cos \phi \sin \phi \right]$$

$$= \frac{1}{C} \lambda \omega \left[\frac{\partial \overline{F}_{x}}{\partial (\frac{c}{\omega})} \cos^{2} \phi + \frac{\partial \overline{F}_{y}}{\partial (\frac{c}{\omega})} \cos \phi \sin \phi \right]$$

$$= \frac{1}{C} \lambda \omega \left[\frac{\partial \overline{F}_{x}}{\partial (\frac{c}{\omega})} \cos^{2} \phi + \frac{\partial \overline{F}_{y}}{\partial (\frac{c}{\omega})} \cos \phi \sin \phi \right]$$

$$= \frac{1}{C} \lambda \omega \left[\frac{\partial \overline{F}_{x}}{\partial (\frac{c}{\omega})} \cos^{2} \phi + \frac{\partial \overline{F}_{y}}{\partial (\frac{c}{\omega})} \cos \phi \sin \phi \right]$$

$$= \frac{1}{C} \lambda \omega \left[\frac{\partial \overline{F}_{x}}{\partial (\frac{c}{\omega})} \cos^{2} \phi + \frac{\partial \overline{F}_{y}}{\partial (\frac{c}{\omega})} \cos \phi + \frac{\partial \overline{F}_{y}}{\partial (\frac{c}{\omega})} \sin \phi \right]$$

$$= \frac{1}{C} \lambda \omega \left[\frac{\partial \overline{F}_{x}}{\partial (\frac{c}{\omega})} \cos^{2} \phi + \frac{\partial \overline{F}_{y}}{\partial (\frac{c}{\omega})} \sin \phi \right]$$

$$= \frac{1}{C} \lambda \omega \left[\frac{\partial \overline{F}_{x}}{\partial (\frac{c}{\omega})} \cos^{2} \phi + \frac{\partial \overline{F}_{y}}{\partial (\frac{c}{\omega})} \sin \phi \right]$$

$$= \frac{1}{C} \lambda \omega \left[\frac{\partial \overline{F}_{x}}{\partial (\frac{c}{\omega})} \cos^{2} \phi + \frac{\partial \overline{F}_{y}}{\partial (\frac{c}{\omega})} \sin \phi \right]$$

$$= \frac{1}{C} \lambda \omega \left[\frac{\partial \overline{F}_{x}}{\partial (\frac{c}{\omega})} \cos^{2} \phi + \frac{\partial \overline{F}_{y}}{\partial (\frac{c}{\omega})} \sin \phi \right]$$

$$= \frac{1}{C} \lambda \omega \left[\frac{\partial \overline{F}_{x}}{\partial (\frac{c}{\omega})} \cos^{2} \phi + \frac{\partial \overline{F}_{y}}{\partial (\frac{c}{\omega})} \sin \phi \right]$$

$$= \frac{1}{C} \lambda \omega \left[\frac{\partial \overline{F}_{x}}{\partial (\frac{c}{\omega})} \cos^{2} \phi + \frac{\partial \overline{F}_{y}}{\partial (\frac{c}{\omega})} \sin \phi \right]$$

$$= \frac{1}{C} \lambda \omega \left[\frac{\partial \overline{F}_{x}}{\partial (\frac{c}{\omega})} \cos^{2} \phi + \frac{\partial \overline{F}_{y}}{\partial (\frac{c}{\omega})} \sin \phi \right]$$

$$= \frac{1}{C} \lambda \omega \left[\frac{\partial \overline{F}_{x}}{\partial (\frac{c}{\omega})} \cos^{2} \phi + \frac{\partial \overline{F}_{y}}{\partial (\frac{c}{\omega})} \sin \phi \right]$$

$$K_{xy} = \frac{1}{C} \lambda \omega \left[\frac{\partial \overline{F}_{t}}{\partial \epsilon} \sin^{2} \phi + \frac{\partial \overline{F}_{r}}{\partial \epsilon} \cos \phi \sin \phi + \frac{\overline{F}_{v}}{\epsilon} \cos \phi \right]$$

$$\omega B_{xy} = \frac{1}{C} \lambda \omega \left[\frac{\partial \overline{F}_{t}}{\partial \epsilon} \sin^{2} \phi + \frac{\partial \overline{F}_{r}}{\partial \epsilon} \cos \phi \sin \phi + \frac{\overline{F}_{v}}{\epsilon} \cos \phi \sin \phi \right]$$

$$(108)$$

$$K_{yx} = \frac{1}{C} \lambda x \left[-\frac{\partial \overline{F}_{t}}{\partial \epsilon} \cos^{2} \phi + \frac{\partial \overline{F}_{x}}{\partial \epsilon} \cos \phi \sin \phi + \frac{\overline{F}_{x}}{\epsilon} \sin \phi \right]$$
 (110)

$$\omega \delta_{yx} = \frac{1}{C} \lambda m \left[-\frac{\partial \overline{F}_{t}}{\partial (\frac{E}{m})} \cos^{2} \phi + \frac{\partial \overline{F}_{t}}{\partial (\frac{E}{m})} \cos \phi \sin \phi \right]$$

$$-\frac{\sin \phi}{\epsilon} \left(\frac{\partial \overline{F}_{r}}{\partial \frac{\phi}{m}} \right) = \frac{\partial \overline{F}_{r}}{\partial \frac{\phi}{m}} \cos \phi$$
(111)

$$K_{yy} = \frac{1}{C} \lambda \omega \left[\frac{\partial \overline{F}_r}{\partial \epsilon} \sin^2 \phi - \frac{\partial \overline{F}_r}{\partial \epsilon} \cos \phi \sin \phi - \frac{\overline{F}_r}{\epsilon} \cos \phi \right]$$
 (112)

$$\omega B_{yy} = \frac{1}{C} \lambda \omega \left[\frac{\partial \overline{F}_{x}}{\partial \frac{\mathcal{E}}{\omega}} \sin^{2} \phi - \frac{\partial \overline{F}_{z}}{\partial \frac{\mathcal{E}}{\omega}} \cos \phi \sin \phi \right]$$

$$+ \frac{\cos \phi}{\delta} \left(\frac{\partial \overline{F}_r}{\partial \dot{\phi}} \sin \phi - \frac{\partial \overline{F}_t}{\partial \dot{\phi}} \cos \phi \right)$$
(113)

where, in the coordinate system selected,

$$\bar{r}_{x} = \frac{-v}{\mu NLD} \left(\frac{R}{C}\right)^{2} \tag{114}$$

$$\overline{P}_{v} = 0 \tag{115}$$

and all forces and derivatives are calculated for the given steady state position, defined by (ϵ_0, ϕ_0) .

APPENDIK III - COMPUTER PROGRAM PN 412 PERFORMANCE OF A HERRINGBONE JOURNAL BEARING UPERATED IN THE TURBULENT REGIME

Input

All input data appears in the form of name list. A full description of name list can be found in Ref. 10. The input are contained in the namelist "INPUT". The input data are:

- 1. REM = Reynolds number
 - = 2 π N₁ N₀ RC

where N, and N are the rotational velocities of the journal and bearing in cycles/sec., respectively.

- R = Radius of journal, in.
- C = Nominal radial clearance, in.
- V Rinematic viscosity, in /sec.
- 2. ALOVD = Length-diameter ratio
 - = L/D

where L = Length of journal, in.

D = Diameter of journal, in.

- 3. COR Film clearance ratio
 - C/R
- 4. PFIX - Dimensionless gage pressures at the ends and the middle of the bearing.
 - = $\frac{P \text{ (Pressure, PSIC)}}{\mu \left(\frac{R}{C}\right) \left(N_1 + N_0\right)}$

$$\mu \left(\frac{R}{C}\right)^{2} \left(N_{1} + N_{0}\right)$$

where μ = dynamic viscosity, lb-sec/in².

The pressure at the initial end appears first, then at the middle and finally at the final end.

5. Il - Number of axial grid points in the first region of the bearing counted from the initial end of journal (see Fig. 2). An odd number is required and also it must be at least 2 less than I2. The minimum permissible value for Il is 3.

- 6. I2 Number of axial grid points counted from the initial end of the journal to the end of the second region. For a vented bearing, 12 represents the grid points of one half of a bearing. For a thre gion, non-vented bearing, I2 represents the grid points for the initial end up to the interface of the second and third region (see Fig. 2). The minimum permissible value for I2 is 5 and the maximum is 17. Again, I2 must be an odd number.
- 7. MORE Indicator to specify whether or not there is another set of input cards to follow the present set. MORE = F, last set of input MORE = T, another set of input to follow
- $= \frac{N_0 N_1}{N_1 + N_2}$
- Number of grid points in the circumferential direction. maximum permissible value for N is 19.
- $= \frac{1}{2\pi} (N_1 + N_2)$ 10 EDOT where & = time rate change of accentricity ratio of the journal.
- 11. PHDOT = Dimensionless whirl velocity ratio $= \frac{1}{2\pi} (N_1 + N_2)$ where 0 = journal whirl velocity, rad/sec.
- 12. GAMDOT = $\frac{7}{2}\pi (N_1 + N_2)$ where $\dot{\gamma}$ = time rate change of angular misalignment.
- = Eccentricity ratio 13. EPS = e/cwhere e = eccentricity of journal, in.
- 14. GAM = Misalignment of journal, degrees.
- = Indicator to specify whether or not the middle of bearing is 15. VENT vented. Set VENT = T only for a bearing vented at the middle. For non-vented bearings, set VENT = F.

- 16. BETA Groove angle in degrees. Beta must be specified for the first region of the bearing (first value) and the second region of the bearing (second value). If VENT = F, the value of BETA in the third region must be specified. For a pump-in design, with grooving in the first region, and a smooth seal in the second region. BETA should be read in as an obtuse angle, the same value for BETA being read in for the second region as the first region. For a pump-out design, with grooving in the second region of the bearing and a seal in the first region, BETA should be read in as acute angle with the same value of BETA being read in for the first region as for the second region. If VENT = F, the value of BETA in the third region should be given. The third value of BETA should be a conjugate of the first value of BETA, i.e. BETA(3)=180°-BETA(1). Never set BETA = 0.
- 17. DEP = Groove recess ratios in two or three regions of the journal with the first value referring to the first region, etc. = 5/c where 5 = groove recess, in.

 To impose the condition of a smooth bearing (no grooving) in either region, set DEP = 0 for that region.
- 18. ALPHA = Fractional groove width in two or three regions of the journal with the first value referring to the first region, etc.

where a_g and a_r are the widths in inches in the groove and ridge portion respectively. To impose the conditions of a smooth portion in either region, set ALPHA = 0 for that region.

Output

- 1. Under the heading of INPUT, the complete set of input in the namelist "INPUT" is printed out. Each quantity is identified by the same symbol as used in the namelist "INPUT".
- 2. In the case of PFOUT = T, a heading of "Final Pressure Distribution" is printed out. Below the heading, if VENT = T, there are a total of I2 number of lines of pressures with the first line referring to the initial end of the bearing. If N is less or equal to 10, each line contains N number of pressures starting at = 0 (see Fig. 1). For the case of N > 10, the number of lines are double. If VENT = F, there are a total of (I2 + I1-1) lines when N ≤ 10. The number of lines will be double for the case of N > 10.
- 3. Regular Output:

There are a total of nine quantities in one line under the heading of REN NO., ECC., TORQUE J., TORQUE B., RADIAL LOAD, TANG. LOAD, FLOW, COS. MOMENT, SIN MOMENT, which are defined below.

- a. REN NO. Same as the input.
- b. EPS = Same as the input.
- c. TORQUE J. = Dimensionless torque on bearing

 T
 WC

 Where T = torque on journal, in-

where T_j = torque on journal, in-1b. W = total load, 1b.

d. TORQUE B. = Dimensionless torque on bearing

Tb

WC

where T_b = torque on bearing, in-lb.

e. RADIAL LOAD = Dimensionless radial component of load $= \frac{F_r}{\mu \ (N_i + N_o) \ (\frac{R}{C}) \ R^2}$ where F_r = radial component of load, lb.

f. TANG. LOAD - Dimensionless tangential component of load

$$= \frac{\mathbf{F_t}}{\mu \left(\mathbf{N_i} + \mathbf{N_o} \right) \left(\frac{\mathbf{R}}{\mathbf{C}} \right)^2 \mathbf{R}^2}$$

where F = tangential component of load, 1b.

g. FLOW = Dimensionless flow

$$= \frac{Q}{R^2C (N_1 + N_0)}$$

where Q = flow, cu. in/sec.

h. COS. MOMENT = Dimensionless radial (cosine) component of moment, about the initial end of journal.

$$= \frac{M_r}{\mu (N_i + N_o) (\frac{R}{C})^2 R^3}$$

where Mr = radial component of moment, 1b-in.

Ö

i. SIN MOMENT - Dimensionless tangential (sin) component of moment, about the initial end of journal.

$$= \frac{M_t}{\mu (N_i + N_o) (\frac{R}{C})^2 R^3}$$

where M = tangential component of moment, 1b-in.

A Fortran listing of Program PN 406 is provided in the next few pages. Typical listings of input and output are also given.

```
MERKINGBUNE JUURNAL
          WITH LARGE ECCENTRICITY AND MISALIGNMENT
    IN TURBULENCE REGIME
    COMMON MDIAG.DELX.DELZ.DELZS.M.MS.MG1.MG2.N.NP(17.19).A1(2.5.1
   19),B1(2,19),CC(2,19),AF1(17,19),AF2(17,19),AF3(17,19),AF4(17,19),A
   2F6(17,19),AF7(17,19),AF5(17,19),PHI(17,19)
    DIMENSION BETA(3).DEP(3).ALPHA(3).PFIX(3).
                                                            QQQ(19),H9(17
   1,19),QQQQ(19),PP(17),PPP(17),PPX(17),PPPX(17),AX1(17,19),AX2(17,19
                                                                                34
   2),AX3(17,19),AX6(17,19),AX7(17,19),AX8(17,19),AX9(17,19),WS11(17,1
                                                                                35
   39).WS12(17.19).WS13(17.19).WS14(17.19).XX(17).AXL(2.19).CZ(2.19)
    DIMENSION KUPT(17,19)
    LOGICAL PPOUT . VENT . TORU . MORE
    NAMELIST/INPUT/REN, ALOVD, COR, PFIX, 11, 12,
   IMORE . SIGN .
                    No EDOT . PHOOT . GAMDOT . EPS . GAM . VENT . BETA . DEP . ALPHA .
   1PPOUT
 2 FORMAT(7E14.7)
   FORMAT(/10(1X+F11+7))
 9 FORMAT(29HOFINAL PRESSURE DISTRIBUTION. //)
 11 FORMAT (6H1 INPUT)
 10 READ(5.INPUT)
    WRITE(6.11)
    WRITE(6.INPUT)
      MDIAG=0
     MD=0
    RATLD=2.*ALOVD
    MG1=11-1
    AMG=MG1
    MS=12-11
    IF(VENT) GO TO 102
    M=12+11-1
    BMM1=M-1
    MG2=MG1
GO TO 101
102 M=12
      RATLD=2.*RATLD
    BMM1= M-1
    BMM1=BMM1+2.
    MG2=0
                                                                                 65
101 DO 30 I=1.M
    DO 30 J=1.N
 30 NP(1,J)=0
      DO 20 J=1+N
     NP(1,J)=1
    1=(L+M)9A
20
35 KK*1
100 AN=N
    PI=3.14159265358979
    DTHETA=2.#PI/AN
    DTHE2=0.5/DTHETA
    TPS=2.*PI*SIGN
    CON1=6.*TPS
    RADIAN=.017453292519943
    GA1=GAM=RADIAN
    EDT=0.0
    CON2=CON1/REN
    TORQ=.FALSE.
    TPS1=TPS/8.0
    TRQ=TPS1+REN
   DELX=DTHETA
   DELZ=RATLD/BMM1
    TPS1=(2.*P1) ++2+8.
```

C

č

	AMS-MS		8.J
	AMS=MS DELZS=DELZ		8
	ANG=0.0		9
	PHIMC=PHDOT-(1SIGN)#0.5		9
	IND=1		9
	ERO2=1.		9
	L1=1		9
	L2=I1		9
3.8	DO 40 J=1.N		96
	CC(L1+J)=0+0		9
	AXL(L1,J)=0.		91
	CZ(L1,J)=0.		99
	A1(L1,2,J)=0.0		100
	A1(L1.3.J)=0.0		10:
40	AF7(L2.J)=0.0	·	102
	IF(IND.EQ.2)GO TO 48		10:
	IF(VENT) GO TO 48	<u> </u>	104
	L1=2		10
	L2=12		100
	IND=2	·	10
	GO TO 38		10
48	NR=1		10'
	MN=MG1	The second secon	11(
	MM= I1	•	11
	ISS=1		11: 11:
	DEL=DELZ		
	DZ=0.5/DELZ		11. 11:
	IS=1 2=0•0		11
200			11
200	BET=BETA(NR)*RADIAN DEPH=DEP(NR)		11.
	ALPH=ALPHA(NR)	· · · · · · · · · · · · · · · · · · ·	11
	ALM1=1ALPH		12
	ALTAL1=ALPH#ALM1		12
	SINB=SIN(BET)		12.
	COSB=COS(BET)		12
	SINB2=SINB*SINB		12.
	COSB2#COSB#COSB		12
	COT2=COSB2/SINB2		12
	DLZ=DEL*DTHETA		12
	IF(TORG) GO TO 1001		12.
	DO 2000 I=IS:MM		12
	XX(I)=Z	, and the second	13
	ZCOR#Z/COR		13
	EPZGH=EPS+GA1*ZCOR		13 13
	EDZR=EDOT+GAMDOT*ZCOR		13
	EPZG=EPZGH+PHIMC		13
	DO 2001 J=1+N SI=SIN(ANG)		13
	CO=COS(ANG)		13
	H=1.+CO*EPZGH		13
	H9(I,J)=H		13
	H3=H*H*H	•	14
	HG=H+DEPH		14
	HGHR=HG/H		14
	AX9(I+J)=(EDZR*CO+EPZG*SI)	*SINB*P!*24.0	14
	HG3=HG**3°		14
	HGHR3=HG3/H3		14
	S1=1./SINB2		14
	S2=-COSB/SINB2		14

	RENG=REN+HG GXR=GTCF(RENR)+12.	
	GXG=GTCF(RENG)+12.	
	GZR=GZCF(RENR)+12.	
	GZG=GZCF(RENG)+12.	
	S5=(GKR+GZR#COT2)	
	S6=(GXG+GZG*COT2)	
	57-62G+52	
	· · · · · · · · · · · · · · · · · · ·	
	58=GZR+52	
	\$9=GZG#\$1	
	\$10=GZR*\$1	
	\$11=-\$5/\$6/HGHR3	
	\$12#1 _F -\$11#ALPH-ALPH	
	S13=(S7-S8/HGHR3)/S6/S12	
	\$14=RENR/HG3/\$12*(1HGHR)/\$6	
	ALH3=ALPH*HG3	
	Als=SINB*(ALH3*S6*S11-ALM1*S5*H3)/S12	
	A2=-ALM1*(ALPH*55*S13+S8)*H3	
	A2=(A2+ALH3+(ALM1*S6*S13-S7))*SINB	
	A3*ALTAL1*S14*(S6*HG3*S5*H3)/REN	
	A3=CON1*(A3+H#ALM1+HG*ALPH)*SINB	
	the define the manage of the true define	
	DMY=H3*ALM1	
	S7H=HGHR3+S7	
	B1S=-H3/S12*(S8*ALM1-S7H*ALPH*S11)*SINB	
	B2=ALH3+(S9-S7+S13+ALM1)+DMY+(S10+ALPH+S8+S13)	
	B3=C0N1+ALTAL1+S14+(S8-S7H)	
	B2=-B2#SINB	
	AX1(I.J)=A1S+A2*COSB	
	B3=-B3*H3*SINB/REN	
	HIZ+SA=(L.1)SXA	
	WS11(I+J)=511/512	
	WS12(I,J)=1./S12 ~	
	W\$13(I.J)=\$13	
	WS14(I+J)=514	
	EA=(L+1)EXA	
	AX6(I+J)=B1S+B2*COSB	
	BAIZ#SBE(Lel)7XA	
	EB=(L-I)BXA	
	IF(MD.NE.2) GO TO 2001	
	IF (I.EQ.IS. AND.J.EQ.1)	
1	<pre>PXAe(Uel)6XAe(Uel)8XAe(Uel)2XAe(Uel)1XA (2e6)3TIRW</pre>	
_	1 •J) •AXB((1•J) •AX9(1•J)	
	ANG=ANG+DTHETA	
	Z=Z+DEL '	
	CONTINUE	
-		
	[F(NR-EQ-1) GO TO 2010	
	IF(NR-EQ-3) GO TO 2014	
	IF(VENT) GO TO 2014	
	GO TO 2020	
	IK=1	
	GO_TO_3800	
	I K = MM	
	GO TO 3800	
	COMPUTE THE DIFFERENCES IN XS AND COEFFICIENT	
	1_14	
	DO 4010 J=1.N	
	AE141. 11-0.0	
	AF1(I+J)=0+0 AF2(I+J)=0+0	''
	AF2(I+J)=0+0	
	AF3(1,J)=0.0	
	AF4(I+J)=0+0 AF5(I+J)=0+0	

	AF6(I,J)=1.0				210
	AF7(1))=-PF[X(NR)				211
4010	CONTINUE				212
2020	IST=IS+1				213
	MM1=MM-1				214
	DO 4000 I=IST •MM1				215
	IO=I-1				216
	17=1+1			·	
					217
	DO 4000 J=1,N				216
	DTH=DTHE2				215
	IF(J.EQ.1.OR.J.EQ.N) GO TO 4004				220
	JU=J-1				221
	J1≠J+1				222
	GO TO 4008				22:
4004	IF(J.EQ.1) GO TO 4006				224
	JO=N-1				225
	J1=1				226
	GO TO 4008				227
4006	JU=N				228
	J1=2		• • • • • • • • • • • • • • • • • • • •	•	229
4008	AF1(I,)=SINB*AX7(I,)				230
	AF2(1,J)=(AX2(1,J1)-AX2(1,J0)+COSB*(AX7(1,J1)-AX7(1,J0)))	#DTH			231
		-0111			-
	1 +SINB*(AX7(I7,J)-AX7(I0,J))*DZ				232
	AF3(1,J)=AX2(1,J)+COSB*AX7(1,J)+SINB*AX6(1,J)				233
	AF4(I.J)=(AX1(I.J1)~AX1(I.J0)+COSH*(AX6(I.J1)-AX6(I.J0)))	#DTH			234
•	1 +SINB*(AX6(I7.J)-AX6(I0.J))*DZ		•		235
	AF5(1.J)=AX1(1.J)+COSB*AX6(1.J)				236
	AF6(1+J)=0+0	_			237
	AF7(I,J)=(AX3(I,J1)~AX3(I,J0)+CUSH*(AX8(I,J1)-AX8(I,J0)))	*DTH			238
	1 +SIND*(AX8(I7.J)~AXA(I0.J))#DZ+AX9(I.J)		· · · · · ·	•	239
	IF (MD.EQ.2 .AND. J. EQ. 1)				24C
	WRITE(6.2) AF1(I.J).AF2(I.J).AF3(I.J).AF4(t . 11 -	AFEI		241
		11311	AFDI		
	1I,J),AF7(I,J)				242
4000	CONTINUE				243
	IF(NR.EG.1) GO TO 4020				244
	IF (NR.EQ.2) GO TO 4040				245
	The state of the s				
	II=2				246
	IE=12 !				247
	GO TO 4090				248
4020	II=1				249
	1E*MM				250
					_
	GO TO 4090				251
4040	11=1				252
	IE=IS				25:
4090	DO 4100 J=1,N				254
	$A1(11 \cdot 1 \cdot J) = 0 \cdot 0$				255
	A1(I1,5,J)=0.0				
					256
	TRS=AX7(IE+J)				257
	TRSZ=TRS+DZ*2•0				258
	A1(11,4,J)=-TRSZ				255
	A1(II+2+J)=A1(II+2+J)-TRSZ*ERO2				260
	DUT=AX6(IE+J)+DTHE2				261
	CC(II.))=CZ(II.)-DDT				262
	CZ(II+J)=DDT				263
	81(II,J)=-CC(II,J)				264
	A1(II+3+J)=A1(II+3+J)+TRSZ				265
	AF7(IE,J)=AXL(II,J)=AXB(IE,J)				
	•				266
	AXL(II,J)=AXB(IE,J)		•		267
	AF1(IE,J)=0.0				268
	AF2(IE,J)=0.0	-			265
	AEGITE II-O O				

The second secon

•	AE4.15 11-0 0	27.
	AF4(IF4)=0.0	
	AF5(1E.J)=0.0	214
	AF6(1E.J)=0.0 1F(MD.EQ.Z.AND.J.EQ.N)	273
	IF(MO.EG.Z.AND.J.EQ.N)	274
	1 WRITE(6.2) A1(!!.2.J):A1(!:.4.J).A1(!!.3.J):B1(!!.J	275
	1) • CC(11 • J) • AF7(1E • J)	276
4100	CONTINUE	277
		211
	GO TO 4130	279
4102	IS=11	280
	NR=2	281
	NR=2 MM=12	282
		283
	DEL=DELZS	284
	DZ=0.5/DELZS	285
	60 to 200	286
4160	IF(VENT) GO TO 4190	287
	IF(KK.EQ.1) GO TO 4180	268
	11 IVVAPATI DO 10 ATOD	
	15*12	289
	MM=M	290
	MM=M NR=3 ERO2=0.	291
	ERO2=0.	292
	DEL -DEL 7	293
	DEL=DELZ	
	DZ=0.5/DELZ	294
	GO TO 200	29
4180	IE=12	296
	ERO2=1.	297
	KK=2	278
		299
		_
	GO TO 4090	300
4150	IF(NR.EQ.2) GO TC 4160	301
	MTSR=MD	302
	MD =MTSR	303
	CALL CICL (MD)	304
	MAN AND AND AND AND AND AND AND AND AND A	
	MD=0 IF(PPOUT) WRITE(6.9) DO 575 I=1.M	305
	IF(PPOUL) WELLE(0.9)	306
-	DO 575 I=1.M	307
	IF(PPOUT) WRITE(6,4)(PHI(I,J),J=1,N)	308
		309
	DO 5/5 J=1*N	310
	!F(PH1(1.J).GE.0.0) GO TO 575	311
	0+0=(1+J)=0+0	312
	KUPT(I.J)*1	31:
575	CONTINUE	314
C	DIMENSIONLESS FLOW Q/C(N1+N2)R#R	319
•	[P=[]-1	310
	· · · · · · · · · · · · · · · · · · ·	
9209	AFLOW=0.0	31
	DO 4200 J=1,N	316
	IF(J.EQ.1.OR.J.EQ.N) GO TO 4220	319
	YF1=(PHI(IP+J+1)-PMI(IP+J-1))*DTHE2	320
4210	AFLOW=(YF1+AX6(IP+J))+AX8(IP+J)+AX7(IP+J)+(PHI(IP+1+J)-PHI(IP-1+J)	
		32
4	I) +DZ+AFLOW	
	IF(MDIAG.EQ.2) WRITE(6.2)YF1.AFLOW	32
	90 10 4200	74.
4220	IF(J.EQ.N) GO TO 4230	329
	IF(J.EQ.N) GO TO 4230 YF1=(PHI(IP,2)-PHI(IP,N))+DTHE2	320
	GO TO 4210	32
1000	YF1=(PHI(IP,1)-PHI(IP,N-1))+DTHE2	326
W420	laa aaaa	
-	60 TO 4210	329
	CONTINUE	330
	AFLOW-AFLOW-DTHETA/12.	33

Ċ	TÖRĞÜE DİVIDED BI MUXNXRXKXKXK/C		35
•	NR=1		33
	TORQ=•TRUE•		334
	TQ=0.0		33
	IT1=1		336
	172=11	-	33
	7C1=0.0		338
	GO TO 200		339
1001	DO 1000 1=1T1+1T2		340
1001	DO 1000 J=1+N		34
	IF(KUPT(I,J).EQ.1) GO TO 1000		342
	IF(I.EQ.ITI.OR.I.EQ.IT2) GO TO 1800		343
	DPDZ=(PHI(I+1,J)-PHI(I-1,J))/DZ		344
	AFTR=1.0		345
1200	IF(J.EQ.1.OR.J.EQ.N) GO TO 1600		346
1200	DPDT=(PHI(I,J+1)-PHI(I,J-1))*DTHE2		347
1 240	H=H9(I,J)		348
1240	BQ=H#ALTAL1*DEPH		349
	AQ=(+BQ*COSB*WS13(I+J)-H*ALM1*WS12(I+J)-ALPH*WS11(I+J)*(H+DEPH))	. *	350
,	AG=(~DG*CO3D*#3[5([*J]***********************************		351
	AQ=AQ+BQ*(-CON2*W514(I.J)-W513(I.J)*DPDZ*51NB)		352
	TQ=TQ+AQ+DLZ+0.5*AFTR		353
	GO TO 1010		354
1.660	IF(J.EQ.N) GO TO 1610		355
1000	DPDT=(PHI(I,2)-PHI(I,N))*DTHE2		356
	GC TO 1240		357
1410	DPDT=(PHI(I,1)-PHI(I,N-1))*DTHE2		358
1010	GO TO 1240		359
1900	AFTR=.5	•	360
1000	IF(I.EQ.IT2) GO TO 1810		361
	DPDZ=(PHI(!T1+1,J)-PHI(!T1,J))/DELZ		362
	GO TO 1200		36
1810	DPDZ=(PHI(IT2,J)-PHI(IT2-1,J))/DELZ		364
1010	GO TO 1200		36
1010	RE=REN#H		366
1.10	TC2=TCC(RE)#ALM1	· . -	36
	RE=REN#(H+DEPH)		368
	TC1=TC1+(TC2+TCC(RE)*ALPH)*TRQ*DLZ*AFTR		369
	IF (J.NE.1) GO TO 1000		370
	IF(MD.EQ.2.AND.I.EQ.IT1)		37
,	WRITE(6,2)AQ,TQ,RE,TC1,TC2		37
	CONTINUE		373
* (1/1/2)	IF(MD.EQ.2)WRITE(6.2)WS11(I.J).WS12(I.J).WS13(I.J).WS14(I.J)		374
	IF(NR.EQ.1) GO TO 1400		37
	IF(NR.EQ.2) GO TO 1410		376
	GO TO 578		37
1400	NR=2		371
	IT1=I1		373
	IT2=12		380
	GO TO 200	•	38
1410	1F(VENT) GO TO 578		38
1410	NR=3		38
	IT1=12		384
	172=M		38
	GO TO 200		384
578	TQO= TQ+TC1		38
	IF (SIGN.LT.0.) TQ0=-TQ0		38
	THE=0.0		38
	DO 580 J=1+N		3.9
	QQQ(J)=SIN(THE)		39
	0000111=0001THE		20

589 THE=DTHETA+THE	393
DO 590 [=1+M	394
PP(I)=0.0	395
PPP(I)=0.0	396
000 J=1*N	397
DUM=PHI(I+J)	398
PP(I)=PP(I)+QQQ(J)*DUM	399
BUO PPP(I)=PPP(I)+QUQQ(J)*DUM	40C
PP(I)=PP(I)+DTHETA	401
PPP(I) =PPP(I) +DTHETA	402
PPX(I) *PP(I) *XX(I)	403
590 PPPX(I)=PPP(I)*XX(I)	404
FSIN=SUM(PP+M+DELZ)	405
FCOS=SUM(PPP+M+DELZ)	406
FMSIN=SUM(PPX+M+DELZ)	407
FMCOS=SUM(PPPX:M:DELZ)	408
FMCOS=FMCOS	409
FCOS==FCOS	41d
	411
WLOAD=SQRT(WLOAD)	412
TQO=TQO/WLOAD	413
TQ1=TQ0+EPS*FSIN/WLOAD	414
	415
WRITE (6.6)	416
WRITE (6.7) REN, EPS, TQI, TQO, FCOS, FSIN, AFLOW, FMCOS, FMSIN	417
6 FORMAT (112H REN NO. EPS. TORQUE J. TORQUE B. RADIAL LOA	418
1D TANG. LOAD FLOW COS. MOMENT SIN. MOMENT)	410
7 FORMAT (F9.2,1X,F6.3,7(1XE13.6))	
599 IF(MORE) GO TO 10	420
<u> STOP.</u>	
END	422

	SUBROUTINE CICL(MD)		2
		LZS+M+MS+MG1+MG2+N+NP(17+19)+A1(2+5+1	3
		17.191.AF2(17.191.AF3(17.191.AF4(17.19).A	/
			5
	2Fo(17,1y),AF7(17,17),AF5(_
		7) •C(17•17) •D(17•17) •F(20•17) •AK(17•17) •G	6
	-).BD(17.17).BF(17).DD(17:17).DS(17).G(17	···· 4
•	217),GI(17,17),E(17,17)		8
	AN=1.0/DELX	The state of the s	
	NC = 0		10
	M=MS+MG1+MG2+1		
	MN1=MG1+1		12
	MN2=MN1+M5	process and the second company	
	DX1=AN+0.5		14
	DX2= AN**2		
203	DO 205 I=1.M		16
	DO 204 II=1.M		-1.7
	E(I.II)=0.		18
204	D([,[],0)		19
	F(1:1)=0.		20
205	$D(I \bullet I) = 1 \bullet$		_
	DO 300 J=1.N		22
	WRITE(7)((E(I,I/),D(I,I))		-23
	IF (MD.NE.2) GO TO 240		24
	WRITE (6.103) AF1(1.J).AF	2(1,J),AF3(1,J),AF4(1,J),AF5(1,J),AF6(1,J	
	l) •AF7(1•J)		26
	WRITE (6:103)	The second secon	
	1 Al(1+1+J)+Al(1+2		28
	lJ) •CC(MN1•J)	and the second s	
	WRITE (6+103)		30
		(2,2,4),A1(2,3,J),A1(2,4,J),A1(2,5,J),	
	1B1 (MN2+J)+CC (MN2+J)		32
240	DZ1=U.5/(DELZ)	a de la companya del la companya de	33
	DZ2=1./(DELZ)**2		34
241	DO242 I=1.M	t and the temperature and	-35
	DO 242 II=1•M		36
	B(I,II)=0.	A CONTRACTOR OF THE PROPERTY O	
	A(I,II)=0.		38
242	C(I,II)=0.		
	DO 250 I=1+M		40
	IF(I-MG1-1) 212,210,212		41
209	AFJI(I) =-AF7(I+J)	The state of the s	42
	A(I,I)=1.		_
210	GO TO 250		44 45-
	IF(MS) 211+212+211 DZ1=∪+5/DELZS		46 46
211	DZ2=1./(DELZS)**2		47
	• =		48
222	1F(NP(I+J))209+232+209		
	1F(MG1) 233:212:233		49 50
233	IF(NC+EQ+2) GO TO 600		50 -51
	A(î,I-2)=A1(1,1,J)	. se - s year market year year and a second of the second	
	A(I,I-1)=A1(1,2,J)		52 53
	A(I,I)=A1(1,3,J)		-54 54
	A(I,I+1)=A1(1,4,J)		54 55
	A(I,I+2)=A1(1,5,J)	A CONTRACTOR OF THE PROPERTY O	
	B(I,I)=B1(1,J)		56
2 ~ ~	C([,[]=CC([,J)	والمنظم والمراجع والمنطقة والم	57
500	AFJI(1)=-AF7(1,J)		58
	GO TO 250	and the second of the second o	- 59
	IF(NP(!+J))209+234+209	<u>.</u>	60
	IF(I-MG1-MS-1) 215,213,21	5 <u></u>	
213	IF(MS) 214,215,214		62

214	DZ1=0.5/DELZ	63
	DZ2=(1-/DELZ)##2	64
	1F(NC+EU+2) GO TO 601	65
	A(1+1+2)=A1(2+1+J)	
	A([.[-1]*A](2.2.J)	66
		57
	A(1+1'=A1(2+3+J)	68
	$A(I_0I+1)=A1(2_04_0J)$	69
-	A([,[+2]=A1(2,5,J)	70
	B(l+l)=B1(2+J)	71
	C(1•1)=CC(2•J)	7.2
601	AFJ1(1)=-AF7(1,J)	73
001	GO TO 250	
~		74
215	IF(NC.EQ.2) GO TO 602	75
	B(I+I-1)=AF3(I+J)*DX1*DZ1	16
	B(I+I)=AF5(I+J)+DX;-AF4(I+J)+DX1	7.7
	B(I+I+1)=-AF3(I+J)+DX1+DZ1	78
	A(I+I-1)=AF1(I+J)+DZ2-AF2(I+J)+DZ1	79
	A(I+I)=AF6(I+J)-2+0*(AF1(I+J)*DZ2 +AF5(I+J)*DX2)	ဗိဝ
	A(I+1)=AF1(I+J)+DZ2+AF2(I+J)+DZ1	_
		81
	C(I+I-1)=-AF3(I+J)+DX1+DZ1	82
	C(I,I)=AF4(I,J)+DX1+AF5(I,J)+DX2	83
	C(I ₀ I+1)=AF3(I ₀ J)+DX1+DZ1	54
602	AFJI(I)=-AF7(I=J)	. ď5
250	CONTINUE	86
	IF(NC+EQ+2) GO TO 603	87
	DO 260 I=1+M	
	DO 260 II=1.M	88
		89
	AK(I+II)=A(I+II)	90
	DO 260 III=1:M	91
260	AK([+II)=AK(I+II)+U(1+III)+E(III+II)	92
	IF(MDIAGeLTe2) GO TO 262	93
	WRITE(6+101)J	94
	DO 261 I=1.M	95
261	WRITE(6+100) (AK(1+11)+11=1+M)	
		96
	CALL MATINY(AK+M+DUM+O+DUM1)	97
603	CONTINUE	98
	DO 404 I=1.M	99
	BF(I)=AFJI(I)	100
	F(J+1+1)=0.	101
	DO 404 II=1.m	102
	E(1,11)=0.	103
	BD(1.11)=0.	_
	·	104
	DO 403 III=1.0M	105
	E(IoII)=E(IoII)-AK(IoIII)+C(IIIoII)	106
403	BD([+II)=BD(I+II)+B(I+III)+D(III+II)	107
404	BF(I)=BF(I)-B(I:II) +F(J:II)	108
	DO 406 I=1:M	109
	DO 406 II wlam	110
	D(I+II)=0.	•
	* · · · · · · · · · · · · · · · · · · ·	111
	DO. 405 . I I I R 1 . M	112
	D([,1])=D([,1])-AK([,1]])+BD([]],1])	113
	.FtJ+1+11#FtJ+1+11+AKt1+111#BEtill	- 114
	CONTINUE	115
	-00-505-1=1+M	اهدد
	DO 504 11=1.M	117
504	00(1=111=-0(1=11)	110
	DD([al]=1.+DD([al])	
747		119
	IF(MDIAGOLTO2) GO TO 264	
	WRITE (6.101)	121
	.00 263 In1 H	122
Z)		123
	The state of the s	1

```
266 CALL MATINY(00+M+DOM+0+DOMI)
DO 507 I=1+M
                                                                                  124
                                                                                  125
                                                                                  126
    S(N.1)=0.
                                                                                  127
    00 507 11=1:M
                                                                                  128
    GN(1.11)=C.
                                                                                  129
    DO 506 III=1.M
                                                                                  130
    GN(1+11)=GN(1+11)+DD(1+111)*E(111+11)
                                                                                  131
500 0(1,11)=GN(1,11)
                                                                                  132
507 5(N,1)=S(N,1)+UD(1,11)*F(N+1,11)
    J=N+1
                                                                                  133
    DO 512 K#2+N
                                                                                  134
                                                                                  135
    WRITE(8) ((G(1,11),1=1,M),11=1,M)
    BACKSPACE 7
                                                                                  136
    READ(7) = ((L(1.11).D(1.11).1=1.M).1=1.M)
                                                                                  137
    BACKSPACE 7
                                                                                  138
    IF (MUIAG-EQ-2) WRITE (6-100) ((E(I-II) + U(I-II) + I-1 + K) + II = 1 + M)
                                                                                  139
    J=J-1
                                                                                  140
    DO 509 I=1+M
                                                                                  141
    S(J-1+1)=+(J+1)
                                                                                  142
    00 509 II=1.M
                                                                                  143
                                                                                  144
    G1(1+11)=0.
    DO 508 111=1.M
                                                                                  145
    G1(1+11) = G1(1+11) + D(1+111) + GN(111+11) + E(1+111) + O(111+11)
                                                                                  146
    IF (MD1AG.NE.2) GO TO 508
                                                                                  147
                                                                                  148
508 CONTINUL
509 S(J-1*[)=S(J-1*[)+E(1*[1]*S(J*[1])+D(1*[1])*S(N*[1])
                                                                                  149
                                                                                  150
    DO 512 I=1.M
    DO 512 II=1.M
                                                                                  151
                                                                                  152
512 G(I.II) = GI(I.II)
                                                                                  153
280 DO 511 I=1.M
                                                                                  154
    DO 510 II=1.M
510 DD(1.11)=-01(1.11)
                                                                                  155
                                                                                  156
511 UD(1.11=1.+0U(1.1)
    18 (NOTAG . ( T. 2 ) GO TO 200
                                                                                  157
                                                                                  158
    WRITE (6+101)
                                                                                  159
    DO 265 1-1•M
26% WRITE (0.10.1 (DO(1.11).11=1.M)
                                                                                  160
4 IPUC . CALL MATINVIPE . M . DUM . J. DUM1 .
                                                                                  161
    IF (MDIAGOLIO2) GO TO 270
                                                                                  162
                                                                                  163
    1:0
    WRITE (6.101);
                                                                                  164
                                                                                  165
    DO 273 1=1.M
2/3 WRITE (6.100) (DD(1.11).11=1.M)
                                                                                  166
270 DO 515 I=1.M
                                                                                  167
    PHI(1.1)=0
                                                                                  168
                                                                                  169
    DU 515 II=1.M
515 PHI(I+1)=DU(I+II)*S(1+II)+PHI(I+1)
                                                                                  170
                                                                                  171
    DO 516 J=2+N
    BACK SPACE 8
                                                                                  172
    READ(8) ((G(1+11)+1=1+N)+11=1+N)
                                                                                  1/3
                                                                                  174
    BACKSPACE B
                                                                                  175
    DO 516 I=1.M
    11.L)2=(L.1)1HQ
                                                                                  176
    DO 516 II=1.M
                                                                                  177
516 PHI(I,J)=PHI(I,J)+G(I,II)+PHI(II,1)
                                                                                  178
    REWIND 7
                                                                                  179
    REWIND 8 ...
                                                                                  180
                                                                               ... . 181
        IF (MD-EQ-2) GO TO 110
    IF(MDIAG.LT.21 GO TO 268
                                                                                  182
                                                                                  183
110 WRITE (6.102)
    DU 267 1=1+M
                                                                                  184
```

(N. [xt. Col. o) (N. [xt. L. o) L. o)	185
266-ASTURN	100
100 FORMAT(1X:1P10E11.4)	186
101 FORMAT (SHOCLC1-15)	188
IOZ FORMATCIHO.30X10HFTNAL PHI /1HO)	189
103 FORMAT (1X+1P7E11-4)	190
END	191

c	SUBROUTINE MATINY(A+N+B+M+DETER) MATRIX INVERSION WITH ACCOMPANYING SOLUTION OF LINEAR DIMENSION IPIVO(17+4+117+B+17+B+17+1+1+1+1+1+1+1+1+1+1+1+1+1	VOT(17) 4
1 5 2 0	DETER =1.0 DO 2U J=1.N IPIVO (J)=0 DO 550 I=1.N	1c
Ċ	SEARCH FOR PIVOT ELEMENT	, 1: 14
45) AMAX=0.C) DO 105 J#1.N	1: 16
60	: IF (IPIVO (J)-1) 60. 105. 60 : DO 100 K=1.N	17 18
80) IF (IPIVO (K)-1) 80+ 100+ 740) IF (ABS (AMAX)-ABS (A(J+K))) 85+ 100+ 100 ; IROW=J	15 20 21
90) ICOLU =K • AMAX=A(J+K)	22
109	CONTINUE CONTINUE	24
Ç	IPIVO (ICOLU)=IPIVO (ICOLU)+1	26 21
C 130	INTERCHANGE ROWS TO PUT PIVOT ELEMENT ON DIAGONAL IF (IROW-ICOLU) 140, 260, 140	2E 25
140	DETER =-DETER DO 200 L=1.N	31 32
170	SWAP=A(IROW+L) A(IROW+L)=A(ICOLU +L)	32 34
205) A(ICULU •L)=5WAP) IF(M) 26U• 26U• 210	3: 36
220) DO 250 L=1, M SWAP=B(IROW+L) B(IROW+L)=B(ICOLU +L)	37 36 39
250	B(ICOLU_+L)=SWAP) INDEX(I,1)=IROW	4C
310	INDEX(I+2)=ICOLU	42
C C	DETER =DETER *PIVQT(I) DIVIDE PIVOT ROW BY PIVOT ELEMENT	46
C	A(1COLU +1COLU)=1.0	4 <u>6</u> 41 48
340 350 355) DO 350 L=1.N) A(ICOLU .L)=A(ICOLU .L)/PIVOT(I) ; IF(M) 380. 380. 360	45 50 51
370) DO 370 L=1.M) B(ICOLU .L)=B(ICOLU .L)/PIVOT(I)	52 53
, , ,	REDUCE NON-PIVOT ROWS	54 55 56
38(39() DO 550 LP=1.N) IF(L1-ICOLU) 400. 550. 400	57 58
400) T=A(L1+ICOLU)) A(L1+ICOLU)=0+0	5 ; 6 (
) DO 450 L=1.N) A(L1.L)=A(L1.L)-A(ICOLU .L)+T	R5 E1

		184W EEO EFO 440	4
		IF(M) 550. 550. 460	0.2
		DO 500 L=1.M	64
	500	B(L1.L)=B(L1.L)-B(ICOLU .L)*T	64
	550	CONTINUE	66
C			67
c		INTERCHANGE COLUMNS	68
č		V. 1. 2. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1.	69
<u>-</u> -	600	DO 710 I=1.N	70
	610	L=N+1-I	71
			72
		JROW=INDEX(L • 1)	73
		JCOLU =INDEX(L+2)	74
		DO 705 K#1.N	75
		SWAP=A(K.JROW)	76
		•	
	· .	A(K,JROW)=A(K,JCOLU)	75
	700	A(K,JCOLU)=SWAP	76
	705	CONTINUE	75
	710	CONTINUE	ಕರ
	_	RETURN	ខរិ
	<u> </u>	END	82

	FUNCTION TOCIRE!	
	1F(RE.GT.100.0) GO TO 10	/
	TCC=8./RE	
	GO TO 100	· · · · · · · · · · · · · · · · · · ·
10	1F(RE.GT.400.0) GO TO 20	
	TCC=4.175/(RE)**.86	·
	GO TO 100	
20	IF(RE.GT.1000.0) GO TO 30	
	TCC=+547/(RE)**+521	10
	GO TO 100	1
30	IF(RE.GT.4000.0) GO TO 40	12
	TCC=+342/(RE)+++453	13
	GO TO 100	14
40	TCC=+064/(RE)**+25	1
100	RETURN	16
	END	17

	FUNCTION SUM(P+M+DX)	
	DIMENSION P(17)	
	X=2	
	KX=M-1	
	KK#2	
•	SUM=0 - 0	
10	DO 20 1=K+KK+KK	
20	SUM=SUM+P(I)	7
	GO TO (30.40.50).K	1
30	SUM=SUM+DX/3.C	1
	RETURN	1
	<=3	1
45	5UM=SUM=2.0	1
	30 TO 10	1
50	(=)	_1
	(K=M	1
	(KK=M-1	1
	50 TO 45	1
	END	20

		3
	FUNCTION GZCF (REYN)	
	RE=REYN	
	IF(RE.LE.70.0)GO TO 20	
	IF((RE.GT.70.0).AND.(RE.LE.4000.0))GO TO 30	
10	IF((RE.GT.4000.0).AND.(RE.LE.7.0E+03)) GO TO 40	<u> </u>
	IF((RE.GT.7000.0).AND.(RE.LE.2.0E+04)) GO TO 50	
	GZCF=25.6/(RE)**.756	
	RETURN	
20	GZCF=1.0/12.0	10
	RETURN	T.
30	GZCF=1.858 E-09*(RE)**2-1.878E-05*RE+.0846	172
	RETURN	T
40	GZCF=9.62/(RE)**.652	14
	RETURN	i:
50	GZCF=11.3/(RE)#*.674	1€
	RETURN	I
	FND	1.6

	FUNCTION GTCF(REYN)	
	RE=REYN	
	IF(RE+LE+70+01GO TO 20	
	IF((RE+GT+70+0)+AND+(RE+LE+2000+0)) GO TO 30	
10	IF(PRE . GT . 2000 . 0) . AND . (RE . LE . 5 . 5E+03)) GO TO 40	
	IF((RE.GT.5500.0).AND.(RE.LE.2.0E+04) GO TO 50	
	GTCF=20.5/(RE)**0.784	·
	RETURN	
20	GTCF=1.0/12.0	10
,	RETURN	1
30	GTCF=+619E-08*(RE)**2-3+465E-05*RE++08569	12
	RÉTURN	13
40	GTCF=4.9Q/(RE)++.628	14
	RETURN	1
50	GTCF=10+35/{RE}**+716	16
	RETURN	1
	END	16

0.10	100000F 02	ALOUD	A 486668	5 00 5					
1 0.	3 1	.0.	<u>0-</u>						
ME T		• 							
10T 0.	12	PHOOT	0.50000000	E 00 0	AMDOT U.			0.9000000	1-01
NT T									
TA (1)	00000E 03	9.31000000E	12 6.3160	0000E 02					
P (1)		U.24000000E							
PHA 1120.			-	****				···	
OUT T		0,55000000	0,5500	0000E 00			_		
D NAMEL 18	TUBLETELD BE	10N							
D NAMEL 18		10n	0,		0,	0.	0.	5.	. 0,
0. NAMELIS JNAL PRESSUI 0. 0.	E DISTRIBUT		0,	0,7761385	0.7924057	0.	U. U.7760784	8. 0.7489701	
NAMELIS JNAL PRESSUI 8. 9.	G. G. G.	0.							
0. NAMELIS JNAL PRESSUI 0. 0.	G. Q. 0.6427785	0.							0.7186
0 NAMELIS JNAL PRESSUI 0. 0. 0.4037008 1.3563977 1.3883323 1.0100076	0. 0. 0. 0. 0.6927785 0.6702456 1.3814361 1.3812372	0.	0,7485889	0,7761385	0.7924057	0.7923074	g.7760784	0.7489701	0,7100 1,4370
0 NAMELIS JNAL PRESSUI 0. 0. 0.4037008 1.3543577 1.3883323 1.0180078 1.0521661	0. 0. 0. 0.6927785 0.6702956 1.3854361 1.3872372 1.0821377 1.0821377	0. 0.7180269 2.4337954	1,4953438	0.7761305 1.5513639 1.1513494	0.7924057	0,7923074 1,5862470 1,1892059	0.7760784 1.5946936 1.1724800	0.7489701 1.90063V8 1.1367066	1,4371
0 NAMELIS JNAL PRESSUI 0. 0. 0.4070010 0.4037000 1.3543577 1.3683323 1.0100074 1.0521461 0.4799845	0. 0. 0. 0. 0.6927785 0.6702475 1.3814361 1.3812377 1.0821377 1.0821377	0. 0.7180269 2.4337954	1,4953438	0.7761385	0.7924057	0,7923074	1.5546936	0.7469701	1,4371
0 NAMELIS JNAL PRESSUI 0. 0. 0.4037008 1.3563377 1.3683323 1.0100076 1.0521661 0.679849 0.7008211	0. 0. 0. 0.6927785 0.6702956 1.3854361 1.3872372 1.0821377 1.0821377	0. U.7180269 L.4337954 L.0647648	0,7485889 1.4993438 1.1085963 0.7308586	0.7761305 1.5513639 1.1513494	0.7924097 1.5851544 1.1814016	0,7923074 1,5862470 1,1892059	0,7760784 1.5546936 1.1724800 0.7848128	0.7489701 1.90083V8 1.1367066 0.7646212	0.7186 1.4391 1.0926
0 NAMELIS JNAL PRESSUI 0. 0. 0.4070010 0.4037000 1.3543577 1.3683323 1.0100074 1.0521461 0.4799845	0. 0. 0. 0. 0.6927785 0.6702956 1.3834361 1.3872372 1.0821377 1.08252619	0. U.7180269 2.4337994 1.0647648 0.7037073	0,7485889 1,4993438 1,1083063	0,7761385 1,5513639 1,1513494 0,7594683	0.7924057 1.5851544 1,1814016 0.7819976	0.7923074 1.5862498 1.1892059 0.7914188	0,7760784 1.5546936 1.1724800 0.7848128	0.7489701 1.90083V8 1.1367066 0.7646212	0.7186 1.4398 1.0926

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APPENDIX IV

COMPUTER PROGRAM PN 406

STATIC PERFORMANCE OF A SPIRAL-GROOVED, PLOATING-KING JOURNAL BEARING OPERATED IN THE TURBULENT REGIME

Input

All input data appear in the form of name list except when the characteristics of inner and outer film are known and need not be computed within the program. In that case, two sets of data, each containing 9 cards in a specified form as explained in detail below, are required to provide the information on the film characteristics.

For the readers who would like to be familiar with the format of namelist, it is recommended that he read pages 14 and 19 of Ref. (10).

The choice of whether to provide or to compute the film characteristics is indicated by the first word of the namelist "NGPUT". The preparation of input for each case is shown below:

- Case I: The film data generated within the program the namelist contains two listings; these are "NGPUT" and "INPUT".
 - A. "NGPUT" includes the following input:
 - INPRD, INPRD # 1: The film characteristics will be generated within the program and the information in the namelist "INPUT" must be provided.
 - 2. NEPS Number of (inner film) eccentricities ratios to be examined (maximum 10).
 - 3. NCASE, NCASE = 0: Last set of input.
 NCASE ≠ 0: More input follows, starting from the namelisting "NGPUT".
 - 4. NN = Number of iterations to be allowed to achieve an equilibrium condition in the floating-ring system (recommend 10).
 - 5. R2R1 = Radius ratio of ring and journal.
 - $= R_2/R_1$, $R_1 = radius$ of journal, in.; $R_2 = radius$ of ring, in.
 - 6. ANTT = Initial guess, on the speed ratio; ω_2/ω_1 , ω_2 = speed of ring, rad/sec.; ω_1 = speed of journal, rad/sec.

- 7. DN = Incremental value of the ring speed ratio during the iteration (recommend. -15).
- 8. REY = Overall Reynolds number under which the bearing is to be operated.
 - $= \frac{\omega_1 R_1 C_1}{V}; \quad C_1 = \text{inner film thickness, in.,}$
 - $v = \text{kinematic viscosity in}^2/\text{sec.}$
- 9.EPIS = Eccentricity ratios of inner film to be examined. There are

 NEPS number of eccentricity ratios to be provided (maximum 10).
- 10.COR1 = Inner film clearance ratio
 - $= c_1/R_1$
- 11.COR2 = Outer film clearance ratio
 - $= c_2/R_2$
- 12.PRES = Overall dimensionless gauge pressure measures at the end and the middle of the bearing.
 - = $2\pi P$ (pressure, psig) / $\mu \omega_1 (\frac{R_1}{C_1})$

where μ is the dynamic viscosity, $\frac{1b\text{-sec}}{\text{in}^2}$

The pressure at the end appears first.

- B. "INPUT" includes the following input:
 - 1. PINSP = The starting value of ring-speed ratio under which the film data will be generated. It is noted that 0 ≤ RINSP ≤1. Since the film data of each film covers three different speeds, a small number for RINSP, say .25, is recommended.
 - 2. DELSP = The incremental ring-speed ratio, DELSP, should be sufficiently small such that RINSP + 2 x DELSP ≤1. The recommended value for DELSP is 0.15.
 - 3. BLOVD = Length diameter ratio, $L/2R_1$, where L is the length of journal.
 - 4. Il = Number of axial grid points in the first region of the bearing counted from the initial end of journal (see Fig. 2). An odd number is required and also it must be at least 2 less than I2.

 The minimum permissible value for I1 is 3.

- B. 5. I2 = Number of axial grid points counted from the initial end of the journal to the middle of the journal. The minimum permissible value for I2 is 5 and the maximum is 17. Again, I2 must be an odd number. The number of grid points in the second region is I2-I1+1 which gives (I2-I1) intervals.
 - 6. N9 = Number of grid points in the circumferential direction, maximum permissible value for N9 is 19.
 - 7. EPS1 = An array of three values of ϵ_1 for which inner bearing film data are to be generated. The range of EPS1 should be wide enough to cover anticipated operating eccentricities.
 - 8. BETA = Groove angle in degrees. BETA must be specified for the first region of the bearing (first value) and the second region of the bearing (second value). For a pump-in design, with grooving in the first region, and a smooth seal in the second region, BETA should be read in as an obtuse angle, the same value for BETA being read in for the second region as for the first region. For a pump out design, with grooving in the second region of the bearing and a seal in the first region, BETA should be read in as acute angle with the same value of BETA being read in for the first region as for the second region.

 Never set BETA = 0.
 - DEP = Groove recess ratios in the two regions of journal with the first value referring to the first region, etc.
 - = 8/c, where 8 = groove recess. in.

 and c = nominal, radial clearance, in.

 To impose the condition of a smooth bearing (no grooving) in either region, set DEP = 0 for that region.
 - 10. ALPHA=Fractional groove width in the two regions of a journal with the first value referring to the first region = a / (a + a r), where a and a are the widths in inches in the groove and ridge portion respectively. To impose the condition of a smooth bearing in either region, set ALPHA = 0 for that region.
 - 11. EPS2= An array of three values of ϵ_2 for which outer bearing film data are to be generated. The range of EPS2 should be wide enough to cover anticipated operating eccentricity.

Case II: In the case of known film characteristics, only the namelisting "NGPUT" is required. In addition to that, 18 cards must be followed which contain the film data.

The content of namelisting "NGPUT" is essentially the same as those of Case I. provided INPRD must be equal to 1.

The inner film data appear first corresponding to three eccentricity ratios at three different inner film Reynolds numbers.

The data include (these symbols are defined below)

Re,
$$\epsilon$$
, $\overline{\mathbf{T}}_{\mathbf{j}}$, $\overline{\mathbf{T}}_{\mathbf{B}}$, \mathbf{S} , ϕ

which are punched on one card with the format of (1X, F8.1, F5.2, 4E13.6). The first three cards are for the same Reynolds number, the smallest of the three values. Each card refers to a different eccentricity ratio. Again, the order of the eccentricity ratio is ascending. The next three cards correspond to a higher Reynolds number but with the same set of eccentricity ratios. In total, there are 9 cards for the inner film.

Following the inner film data, there are 9 cards for outer film data arranged in an order similar to that for the inner film.

The six quantities used as input for the inner and outer film are defined below.

- 1. Re = Reynolds number $= \frac{(\omega_1 \omega_2) R_1 C_1}{\nu}$ (for inner film) $= \frac{\omega_2 R_2 C_2}{\nu}$ (for outer film)
- 2. $\epsilon = \text{Eccentricity (see Fig. 3)}$ $= e_1/c_1 \qquad \text{(for inner film)}$ $= e_2/c_2 \qquad \text{(for outer film)}$
- 3. \overline{T}_j = Dimensionless Torque of Journal $= \frac{T_j}{WC_1}$ (for inner film), where W = load, pounds $= \frac{T_j}{WC_2}$ (for outer film)

Case II:

4.
$$\overline{T}_B$$
 = Dimensionless Torque of Bearing
$$= \frac{T_B}{WC_1} \quad \text{(for inner film)}$$

$$= \frac{T_B}{WC_2} \quad \text{(for outer film)}$$

5. S = Sommerfeld Number

$$= \frac{LD_1\mu(N_1+N_2)}{W} \frac{\left(\frac{R_1}{C_1}\right)^2}{W}$$
 (for inner film)

$$LD_2 \mu N_2 = \frac{R_2 \cdot 2}{C_2}$$
(for outer film)

where N₁ and N₂ are speed of journal and ring in rev./sec., respectively.

= ϕ_1 (for inner film)
= ϕ_2 (for outer film)

Output

The output appears under the title of "Floating-Ring with herringbone journal".

- Main program input: it prints out the title of "Main program input".
 Immediately, there follows the title of "Namelist NGPUT" and the entire contents in that namelist. At the end, it prints out "end namelist NGPUT".
- 2. Input for subroutine "HERNB": it prints out the title of "Herringbone Bearing Input" and a title of "Namelist INPUT". Then, the entire contents of that namelist are printed out. At the end, it prints out "end namelist INPUT".
- 3. Single film data
 - A. For Inner Film:

There are three eccentricity ratios at three different Reynolds numbers corresponding to three different speed ratios. The output starts with a title of "inner film data" and then the headings REYNOLDS NO., ECCENTRICITY, INNER TORQUE, OUTER TORQUE, SOMMERFELD

NO., ATT. ANGLE, FLOW, on one line. Immediately, there follows 9 lines of data. Each line contains seven quantities under the appropriate heading. The first six of these seven quantities are defined above in the input list for NGPUT, Case II. The flow is defined as

Q - dimensionless flow

$$= \frac{C}{R_1^2 C_1(N_1 + N_2)}$$
 (for inner film)

Q = Flow, cu. in/sec.

B. For Outer Film:

After the output of the inner film, there are a set of output referring to the outer film just like those for the inner film. The output comprises the title of "Outer Film Data", the heading and 9 lines of data.

4. Final performance characteristics of the floating ring bearing at the steady state equilibrium condition. Under the title of output, there are four values in a line. These are:

ECCENTR/C₁ = e/C_1 = the overall eccentricity of the journal at equilibrium position divided by the nominal clearance of the inner film (see Fig. 4).

 ${\rm N_2/N_1},~{\rm C_2/C_1}$ and ${\rm R_2/R_1}$ as previously explained.

Next, there is a table of output referring to the inner film, the outer film, and the overall bearing. There are seven values in a line and a total of 3 lines. Each line contains

REYNOLDS NO. =
$$\frac{(\omega_1 - \omega_2)R_1C_1}{\alpha_1 + \alpha_2}$$
 (for inner film)

$$= \frac{\omega_2 R_2 C_2}{v}$$
 (for outer film)

$$= \frac{\omega_1 R_1 C_1}{v} \qquad \text{(for overall)}$$

ECCENTRICITY =
$$e_1/c_1$$
 (for inner film) = e_1

(see Figs. 3 and 4)

$$\epsilon_2 = \epsilon_2/c_2$$
 (for outer film)

$$\epsilon = e/c_1 + c_2$$
 (for overall)

TORQUE = Dimensionless form defined as

$$= \left[\frac{T_1}{WC_1}\right] - \frac{1}{2} S_1 \epsilon_1 \overline{F}_{t1} \qquad \text{(for inner film)}$$

$$= \left[\frac{T_B}{WC_2}\right] + \frac{1}{2} S_2 \epsilon_2 \overline{F}_{t2} \qquad \text{(for outer film)}$$

$$= \left[\frac{\mathbf{T}_{1}}{\mathbf{WC}_{1}} \right]$$
 (for overall)

where \overline{F}_{t1} and \overline{F}_{t2} are defined on page 139.

SUPPLY PRES = Dimensionless supply pressure

$$= \frac{\frac{P}{R_{\frac{1}{2}}}}{\frac{R_{\frac{1}{2}}}{C_{1}}} \quad \text{(for inner film)}$$

$$= \frac{P}{\mu N_2 \left(\frac{R_2}{C_2}\right)}$$
 (for outer film)

$$= \frac{P}{\mu N_1} \frac{\left(\frac{R_1}{C_1}\right)}{\left(\frac{C_1}{C_1}\right)}$$
 (for overall)

SOMMFD NO. - Sommerfeld Number

$$\mathbf{s}_{1} = \frac{LD_{1}^{\mu} (N_{1}+N_{2}) \left(\frac{R_{1}}{C_{1}}\right)^{2}}{W} \text{(for inner film)}$$

$$S_2 = \frac{LD_2 \mu N_2}{W} \frac{\left(\frac{R_2}{C_2}\right)}{W} \qquad \text{(for outer film)}$$

$$S = \frac{LD_1 \mu N_1 \left(\frac{R_1}{C_1}\right)}{W} \qquad \text{(for overall)}$$

ATT. ANGLE = Attitude angle in deg. (see Fig. 3)

- Ø₁ (for inner film)
- Ø₂ (for outer film)
- = Ø (for cverall)

TANG. FORCE = Dimensionless form of tangential force

$$\overline{F}_{t1} = \frac{F_{t1}}{WS_1}$$
 (for inner film)
$$\overline{F}_{t2} = \frac{F_{t2}}{WS_2}$$
 (for outer film)

where F_{t1} = Tangential force of the inner film, pound F_{t2} = Tangential force of the outer film, pound

A Fortran listing of program PN 406 is provided in the next few pages. Typical listings of input and output are also given.

03	/04/69	
MAAN - EIP GOUNCE STATEMENT - TENES -	V4/ 07	
C FLOATING-RING IN CONJUNCTION WITH HERRINGBONE JOURNAL IN TURBULENT		
C REGIME DIMENSION P(6,3,3),Q(6,3,3),A(4,3,3),B(4,3,3),AP(4,3,3),BP(4,3,3)		
DIMENSICH REY(1).C2C1(1).EPIS(10).BA(6).BC(6).AA(4.3).BB(4.3)	53 54	
DIMENSICH AP1(4,3),8P1(4,3),81(4,3),81(4,3),\$A(4),\$B(4)	55	
CIMENSICA EPS1(3), BETA(3), DEP(3), ALPHA(3), PRES(3), EPS2(3)	56	
500 FORMAT(1x, F8.1, F5.2, 4E12.6)	57	
525 FORMAT(6(1PE12.51)	58	
C INPRO-1, CATA FOR HERRINGBONE BEARING READ IN	62	
NAMELIST/NGPUT/INPRC, NEPS, NCASE, MN, R2R1, ANTT, DN, REY,	63	
1EPIS, CUR1, COR2, PRES/ INPUT/R INSP, DELSP, BLOVD, 11, 12, N9.		
1EPS1, BETA, DEP, ALPHA, EPS2	65	
52 NRE~1	66	
GAM-U.O	67	
EDOT=0.0	68	
HUST=0		
PHDOT=0.0	69	
KDIAG=0 NSES1=0	70	
N9652=0	72	
READ (5 INCPUT)	80	4
IF (MUST-NE-1) GO TO 53	73	•
KDIAG=1	74	
NSES1=1	75	
NSES 2=1	76	
33 NCC=1 1000 1000 1000 1000 1000 1000 1000	17	
WRITE(6,505)	78	14
505 FORMAT(41H) FLCATING-RING WITH HERRINGBONE JOURNAL)		
C2C1(1)=COR2/CCR1+R2R1	61	
WR ITE (6, 210)	82	15
FCS=FRES(2)	83	
210 FORMAT(20H MAIN PROGRAM INPUT)	84	
WRITL(6, NGPUT)	85	16
IF(INPRC.EQ.1) GO TO 202	86	•
READ(5,INPUT) WRITE(6,212)	87	20
212 FURMAT(27H HERRINGBONE EGARING INPUT)	88 89	21
WRITE(6. INPUT)	90	22
PPAS=1	91	
REO=REY(1)	92	
CALL HERNB (BLCVO, COR1, COR2, PRES, II, 12, N9, EOOT, FHCOT, EPS1, GAM, BETA,	93	••
10EP. ALPHA, RINSP, REC. RZR1, DELSP, MPAS, KC TAG)	94	25
REWIND 9	95	26
00 1213 K=1.3	96	
00 1213 J=1,3	97	
READ(9) (P(1,J,K),P(2,J,K),P(3,J,K),P(4,J,K),P(5,J,K),P(6,J,K))	98	31
ERRCR MESSAGE NUMBER 1		
1213 CONTINUE	99	
REWING 9	غامانه	41
GO TO 304	100	
202 READ (5,500) ((P(1,J,K),P(2,J,K),P(3,J,K),P(4,J,K),P(5,J,K),P(6,J,K	101	4.9
11,J=1,3),K=1,3) 304 IF(MUST-EQ-1)%RITE(6,5GG)((P(1,J,K),P(2,J,K),P(3,J,K),P(4,J,K),P(5	102 103	43
1.J.K).P(6.J.K).J=1.3).K=1.3)	104	59
4101111 10101011041110411104111	107	27

MATE _ CEN COUNCE STATEMONT .	03/04/69
MAIN - EFN SOURCE STATEMENT - I	FN(S) -
204 IK=1	105
DO 1 I=1,6	106
DO 1 J-1;3	107
DO 1 K=1,3	108
1 C(I, J,K)=P(I, J,K)	109
2 DO 5 J=1,3	110
00 5 I=3,6	111
- A(1-2,J,1)=0.C	112
A(I-2,J.3)=0.C	113
B(1-2,J,1)=0.C	114
B(I=2,J,3)=0.C	115
AP(I-2, J, 1)=0.0	116
AP(I-2, J, 3)=0.0	117
8P(1-2, J, 1) = 0.C	118
8P(I=2, J, 3)=0.0	119
Y2=Q(1, J,1)	120
Y3=Q([, J, 2)	121
X2=U(1, J, 1)	izz
X3×4(1, J, 2)	123
DO 5 K=2,2	124
Y1=Y2	125
Y2*Y3	128
X1=X2	127
X2*X3	
Y3=Q(I, J, K+1)	128
X3=Q(1,J,K+1)	130
0T1=X2~X1 CT2=X3~X2	131 mg
	132
C1=Y2=Y1	133
C2=Y3=Y2	134
C3=X3-X1	
C4=DT1/CT2	136
C24=C2+C4	137
4(1-2,J,K)=(C24-C1)/(CT1+C3)	138
8(1··2·J·K)=(C24+C1/C4)/C3	139
GO TC (3,5),IK	140
3 AP(I-2, I,K)=A(I-2, J,K)	141
BP(1-2, J, K)=B(1-2, J, K)	142
5 CONTINUE	143
GO TC (7,9),1K	144
7 IF(INPRC.EQ.1) GO TO 208	145
MPAS=2	146
CALL HERNB(BLCVD.CCR1,CGR2,PRES,I1,I2,N9,EDOT,P	HCOT, EPS2, GAM, BETA, 147
ICEP, ALPHA, RINSP, REU, RZRI, DELSP, MPAS, KCIAG)	148
REWIND 10	149
DO 1228 K=1,3	150
00 1228 J=1.3	151
PEAD(13) (Q(1,J,K),Q(2,J,K),Q(3,J,K),Q(4,J,K),Q	
· with the contraction of the co	
RCR PESSAGE NUMBER 2	THE CONTRACTOR OF THE CONTRACT
228 CONTINUE	169
REWING 10	153
GO TO 309	154
208 READ(5,500)((C(1,J,K),Q(2,J,K),Q(3,J,K),Q(4,J,K),Q(5,J,K),C(6,J,K) 135
1,J71,3),K=1,3)	156
309 IF(MUST.EQ.1)kRITE(6,50C)	157

	037	04/69	
	MAIN - EFN SOURCE STATEMENT - IFN(S) -		
	((C(1,J,K),Q(2,J,K),Q(3,J,K),Q(4,J,K),Q(5,J,K),C(6,J,K)	158	
	1.J=1.3).K=1.3)	159	165
9	1K=2	160	
	GO TC 2	161	
9	DO 201 I##1,NRE	162	
	RE=REY(IA)	163	
	00 201 1E=1,NCC CC=C2C((1B) 00 201 1C=1,NEPS EP=EPIS(EC)	164 165	
	60 201 16-1 MEDS	166	
	20 201 1(-1)NEPS 2PagPIS(IC)	167	
	ANRT-ANTT	168	
	N=U	169	
	C=AN	170	
Ĵ	RE1=RE+(1ANRT)	171	
	RE2=R2R1+GC+RE1/(1.0/ANPT-1.C)	172	
	C1=P(1,1,3)	173	
_	IF(RE1-C1) 11:19:19	174	
0	KC=3	175 176	
	GO TC 14	177	
•	DO 13 K=2.3 Cl=P(1.1.K)	178	
	IF(R21mC1) 12,13,13	179	•
2	KC=K	180	
-	GO TC 14	181	
3	CONTINUE	182	
4	DO 18 [=1,4]	183	
	CO 18 J=1,3	164	
	ARMAP(I,J,KC)		
	er=BP(I,J.KC)	136	
	CR#P(1+2,J,KC)	187 188	
-	XR=P(1,J,KC)	189	
	KL=KG-; AL=AP(I,J,KL)	190	
	EL-BP(I.J.KL)	191	
	CL=P(I+2,J,KL)	192	
	XL=P(1,J,KL)	193	
	CI=R Ei=XP	194	
•	Cl=CR+Cl+(BR+Cl+AR)	195	
	C2=R£1-xL	196	
	C2=CL+C2+(BL+C2+AL)	197 198	
١.	IF(KC-2)15,15,16	198	
ĺ	C2=C1	200	
ĺ		200	
5	GO TC 18	201	
5	IF(3~KC) 17,17,18	201 202	
5 67	ÎF(3~KC) 17,17,18 C1=C4		
5 6 7 8	IF(3~KC) 17,17,18 C1=C2 AA(I,J) =(C1+C2)/2, IF(NSES2-NE-1) GD TO 88	202	
5 6 7 8	IF(3~KC) 17,17,18 C1=C2 AA(I,J) =(C1+C2)/2, IF(NSES2-NE-1) GD TO 88	202 203 204 205	235
5 678	IF(3~KC) 17,17,18 C1=C4 AA(I,J) =(C1+C2)/2. IF(NSES2.NE.1) GO TO 88 WRITE(6,\$25)((AA(I,J),J=1,3),I=1.4)	202 203 204 205	235
5 678	IF(3~KC) 17,17,18 C1=C4 AA(I,J) =(C1+C2)/2. IF(NSES2.NE.1) GO TO 88 WRITE(6,\$25)((AA(I,J),J=1,3),I=1.4)	202 203 204 205	235
5 678	IF(3~KC) 17,17,18 C1=C4 AA(I,J) =(C1+C2)/2. IF(NSES2.NE.1) GO TO 88 WRITE(6,\$25)((AA(I,J),J=1,3),I=1.4)	202 203 204 205	235
5 678	IF(3~KC) 17,17,18 C1=C4 AA(I,J) =(C1+C2)/2. IF(NSES2.NE.1) GO TO 88 WRITE(6,\$25)((AA(I,J),J=1,3),I=1.4)	202 203 204 205	235
5 678	IF(3~KC) 17,17,18 C1=C4 AA(I,J) =(C1+C2)/2. IF(NSES2.NE.1) GO TO 88 WRITE(6,\$25)((AA(I,J),J=1,3),I=1.4)	202 203 204 205	235
5 678	IF(3~KC) 17,17,18 C1=C4 AA(1,J) =(C1+C2)/2. IF(NSES2.NE.1) GO TO 88 WRITE(6,525)((AA(1,J),J=1,3),1=1.4) DO 19 I=1,4 API(1,1)=0.0 API(1,3)=0.0 EPI(1,3)=0.0 EPI(1,1)=0.0	202 203 204 205	235

	MAIN	•	SFN	SOURCE	STATEMENT	- IFN(S) -	03/04/
	-		•			ALLEGE CONTRACTOR	
101	Y2=AA(1,1)+X2						•
	Y3+AA(1,2)+X3						
	CO TC LUE						
102	YZ=AA(1,1)						
	Y3=AA(I,2)						
103	DO 19 J=2,2						-
	Y1=Y2						
	Y2=Y3						•
	X1=X2						
	د X2=X						
	X3=P(2,J+1,1)						
	IF(1-4) 104,10	5.104					
104	Y3=AA(I,J+1)*)						
104	GO TC 106						
105	Y3=AA(I.J+1)						•
		-					
100	CT1=X2-X1						
	CT2= X3 X2						
	C1=Y2=Y1						
	C2=Y3-Y2						
	C3=X3-X1						
	C4=DT1/ET2						
	C24=C2+C4						
	AP1(1+J)=(C24-	CIB/(DT 3 *C	31			
	BP1(1,J)=(C244	C1/C4)/Ç3				
19	CONTINUE						
	C1=P(2.3.1)						
	IF(EP-C1) 21,2	0.20					
20	KA=3						
	GD TC 24						
21	DG 23 J=2,3						
••	C1=P(2,J,1)						
	IF(EP-C1) 2.2	2.92					
22	KA=J	- 1					
- 6£.	GO TC 24						
• • •	CONTINUE						
64	DO 109 I=1.4						
	AR=API(I KA)						
	BR=BP1(I,KA)						
	XR=P(2,KA,1)						
	CR=AA(I,KA)						
	IF(I-4) 131,13	2.132					
131	CR=CR+XR						
132	KB=KA-1						
	AL-APITT, KBT						•
	BL-BP1(I,KB)						
	VI -0/3 V						•
	CL=AA(1,KB) IF(1-4) 133,13						
	18/1-A1 133.13	4.834				-	
122	CL=CL+XL	71137					
	C1-60-V0	• • • • • •					•
139	C1=EP=XR						
	C1=CR+C1+(BR+C	TANK)	-				
	CZ=EP-XL						
	CZ=CL+CZ+(BL+C	ZPAL)					· · · · · · · · · · · · · · · · · · ·
	IF(KA-2) 25,25	,26					
9.5	C2=C1						

	MA IA	_	EEU	£01:00 C					03/04/69	
	78.17	_	EFA	100::00	STATEMENT	-	164121	-		
20	IF (3-KA) 27,2	7.2R								
2	C1=G2	,,,,							270	
21	IF(I-4) 107,1	C8.107	,						271	
10	SA(1)=(C1+G2)	112.85	D 1						272	
	CO TC 136		,,,						273	
101	SA([]=(C1+C2)	12.							274	
109	CONTINUE								275	
	RF=SA(1)								276	
	S1=SA(3)								277	
	RCFM= (SA(1)+S	F(2)1/	2.						278	
	ATT1=5A(4)								279	
	FT=(SA(1)-SA(2))/(5	P*S1)						280	
	C1=R2R1+#3								281	
	02=CC+CC								282	
	\$2=\$1+C1/(C2+	(1.+1.	/ANRT	1)					283	
	C1=Q(1,1,3)								284	
	1F(R=2-C1) 31	,30,33							285	
30	JC=3								286	
_	GD TC 34								287	
31	DO 33 K=2,3								268 289	
	C1=Q(1,1,K)								290	
	IF(R:2-C1) 32	13:33							291	
32	JC=K								292	
• • •	00 16 34								293	
33	CONTINUE								294	
34	CONTINUE CO 3d I=1,4 CO 36 J=1,3								295	
	AR=A(I,J,JC)								296	
	6R=8(I,J,JC)								297	
	CR=Q(1+2,J,JC)	ı							298	
	XR=4(1,J,JC)								299	
	JL=JC-:								300	
	AL=A(I,J,JL)								501	
	8L=8(1,J,JL)								302	
	XL=Q(I,J,JL)								3 23	
	CL=Q(I+2,J,JL)								204	
	Cl=Ri2··xR								305	
	C1=CA+C1+(8R4C	J#AR)							376	
	C2=RiZ=XL								307 308	
	C2=CL+C2+(BL+C	2*AL 1							309	
	IF(JC-2) 35,35	• 36							319	
35	C2=C1								319 311	
	GD TC 38								312	
30	IF(3-JC) 37,37	. 38							213	
	G1=G2	."							314	
20	BB(1,J)=(C1+C2	"						-	315	•
80	IF(NSES2.NE.1)	90 TO	90	•••					316	
90	WRITE(6,525)(()	E91.117	113-11	::::::::	4)				317	358
	NB=4~J								318	-
	C3=Q(2,J,1)								319	
	C1=C3+C3								± 2 0	
	BC(NE)=.C1/C1	•							321	
	BA(NB)=BE(3,J)								322	
. 59	CONT INUE								323	
	A1(3,1)=C.J	•	•						324	
									325	

MAIN - FFN SQUACE STATEMENT - IFR(3) - A1(3,3)=Cou	7 8 9 10 11 2
81(3,3)=0.0 61(3,3)=0.0 32 X2=8A(1) 33 X2=8A(2) 33 Y2=8C(1) 33 Y3=8C(2) 33 Y1=Y2 33 Y2=Y3 X1=X2 X2=X3 X3=8A(J*1) 33 X3=8A(J*1) 33 X3=8A(J*1) 33 X1=X2 X2=X3 X3=8C(J+1) 33 X1=X2 X2=X3 X3=X3-X1 C1=Y2=Y1 C2=Y3=X2 C3=X3=X1 C4=071/C72 C3=X3=X1 C4=071/C72 C24=C2*C4 A1(3,J)=(G24+C1/C4)/C3 81(3,J)=(G24+C1/C4)/C3	7 8 9 10 11 2
81(3,3)=0.0 X2=8A(1) X3=8A(2) Y2=8C(1) Y3=8C(2) D0 39 J=2,3 Y1=Y2 X2=Y3 X1=X2 X2=X3 X3=8A(J+1) Y3=8C(J+1) D1=X2-X1 DT2=X3-X2 C1=Y2-Y1 C2=Y3-Y2 C3=X3-X1 C4=DT1/CT2 C3=X3-X1 C4=C1/C72 C4=C1/C4+C1/C6) 81(3,J)=(C24+C1/C4)/C3	9
X2=BA(1) X3=BA(2) Y2=BC(1) Y3=BC(2) 33 D0 39 J=2,3 Y1=Y2 33 Y1=Y2 X2=Y3 X1=X2 X2=X3 X3=BA(J+1) 33 X3=BA(J+1) 33 DT1=X2-X1 0T2=X3-X2 C1=Y2-Y1 C2=Y3-Y2 C3=X3-X1 C4=DT1/CT2 C2=C2+C4 A1(3,J)=(C24+C1/C4)/C3 B1(3,J)=(C24+C1/C4)/C3	1
Y2=BC(1) Y3=BC(2) D0 39 J=2,3 Y1=Y2 Y2=Y3 X1=X2 X2=X3 X3=BA(J+1) Y3=BC(J+1) DT1=X2-X1 DT2=X3-X2 C1=Y2-Y1 C2=Y3-Y2 C3=X3-X1 C4-DT1/CT2 C3=X3-X1 C4-DT1/CT2 C24-C2+C4 A1(3,J)=(G24+C1)/(GT1+C3) B1(3,J)=(G24+C1/C4)/C3	2
Y2=BC(1) Y3=BC(2) D0 39 J=2,3 Y1=Y2 Y2=Y3 X1=X2 X2=X3 X3=BA(J+1) Y3=BC(J+1) DT1=X2-X1 DT2=X3-X2 C1=Y2-Y1 C2=Y3-Y2 C3=X3-X1 C4-DT1/CT2 C3=X3-X1 C4-DT1/CT2 C24-C2+C4 A1(3,J)=(G24+C1)/(GT1+C3) B1(3,J)=(G24+C1/C4)/C3	2
00 39 J=2,3	3
00 39 J=2,3	3
Y2=Y3 X1=X2 X2=X3 X3=BC(J+1) 33 Y3=BC(J+1) 0T1=X2-X1 0T2=X3-X2 C1=Y2-Y1 C2=Y3-Y2 C3=X3-X1 C3=X3-X1 C4-DT1/CT2 C24-C2*C4 A1(3,J)=(C24-C1)/(CT1*C3) B1(3,J)=(C24+C1/C4)/C3 33 33 33 33 34 35 34 35 35 36 37 36 37 37 38 38 38 38 38 38 38 38 38 38 38 38 38	
X1=X2 X2=X3 X3=BA(J+1) Y3=BC(J+1) DT1=X2-X1 DT2=X3-X2 C1=Y2-Y1 C2=Y3-Y2 C3=X3-X1 C4-DT1/CT2 C24-C2*C4 A1(3,J)=(C24-C1)/(DT1*C3) B1(3,J)=(C24+C1/C4)/C3	
X2=X3	
X3=6A(J+1) 33 33 34 34 35 35 35 35	-
Y3=BC(J+1) DT1=x2-x1 DT2=x3-x2 G1=Y2=Y1 G2=Y3-Y2 G3=x3-x1 G4=DT1/CT2 G2=C2+C4 A1(3,J)=(G24+C1)/(DT1+C3) B1(3,J)=(G24+C1/C4)/C3 34 B1(3,J)=(G24+C1/C4)/C3	
DT1=x2-x1 OT2=x3-x2 C1=y2-y1 C2=y3-y2 C3=x3-x1 C4=DT1/CT2 C24-C2*C4 A1(3,J)=(C24-C1)/(DT1*C3) B1(3,J)=(C24-C1/C4)/C3 34	-
012=x3=x2 C1=y2=y1 C2=y3=y2 C3=x3=x1 C4=011/C12 C24=C2+C4 A1(3,J)=(C24-C1)/(D11+C3) B1(3,J)=(C24+C1/C4)/C3	
C1-Y2-Y1 C2=Y3-Y2 C3=X3-X1 C4-D17/CT2 C24=C2+C4 A1(3,J)=(C24-C1)/(DT1+C3) B1(3,J)=(C24+C1/C4)/C3 34	
C2=Y3=Y2 C3=X3=X1 C4=DT1/CT2 C24=C2+C4 A1(3,J)=(G24=C1)/(DT1+C3) B1(3,J)=(G24+C1/C4)/C3	
C4=DT1/CT2 C24=C2+C4 A1(3,J)=(G24-C1)/(DT1+C3) B1(3,J)=(G24+C1/C4)/C3 34	
C24=C2+C4 A1(3,J)=(G24-C1)/(DT1+C3) B1(3,J)=(G24+C1/C4)/C3 34	4
A1(3,J)=(624-C1)/(011+C3) 34 B1(3,J)=(624-C1/C4)/C3 34	5
81(3 ₄ J)=(G24+C1/G4)/G3 34	6
	7
ag continue 34	
C1=8A(3)	
IF(S2-C1) 41.40.40	
40 NC=3 35 GO TC 44 35	
GO TC 44 41 DO 43 J=2,3	
C1•8A(J) 35	
IF(\$2-C1) 42,43,43 35	-
42 NC=J	
CO TC 44	-
43 CONTINUE	
44 AR=A1(3,NC) 36	ŋ
36 (3, NC)	1
CR=BC(NC)	2
XR#BA(NC)	
NL=NC=1 36	
AL=A1(3, NL) 36	-
8L=81(3, NL) 36	
CL=8C(NL) 36 XL=8A(NL) 36	
XL=BA(NL) 36 C1=S ₄ ⇒X# 36	
C1=32=AR C1=CR+ <u>C1*(BR+C1</u> +AR) 37	
C2=S2=XL 37	
C2=CL+C2*(BL+C2*AL) 37	
IF(NC-2) 45,45,46	
45 C2=C1 37	
GO TC 48	
46 ÎF(3~NC) 47,47,48 37	5
47 C1=C2 37	
48 C3=(C1+C2)/2.	6 7
C2=1 ₄ /C3 37	6 7 8
EP2=.1+SCRT(C2) 36	6 7 8 9
00 49 1=1.4	6 7 8 9 0 413

MAIN - EFN SOURCE STATEMENT - IFN	03/04/69
A1(I-1)=0.0	362
A1(1,3) *0.0	363
81(1,1)=0.0	384
B1(1,3)=0.0	385
X2=Q(2,1,1)	306
x3=Q(2,2,1)	367
[F([=4] 111,112,111	348
Y2=88(1,1)+X2	390
Y3=88(1,2)*X3 GO TC 113	391
Y2=86(1,1)	392
Y3=88(1,2)	393
DO 49 J=2,2	394
Y1=Y2	395
Y2=Y3	396
X1=X2	397
X2=X3	378
X3=Q(2,J+1,1)	399
IF(1-4) 114,115,114	400
Y3=88(I,J+1)=X3	401
GO TC 116	402
Y3=86([,J+1)	404
071=x2-x1 072=x3-x2	405
C1=A5=A1	406
C2=Y3=Y2	407
. C3=x3=x1	111
C4=DT1/C12	409
C24=C2+C4	410
A1(1,J)=(C24-C1)/(Df1+C3)	411
B1(1,J)=(C244C1/C4)/C3	412
CONTINUE	413
C1=Q(2,3,1) 1F(EP2=C1)61.60.60	414
.,	
LC=3	416
GO TC 64	417 418
00 63 J=2,3 C1=9(2,J,1)	419
IF(EP2-C1) 62,63,63	nČ∆
LC-J	421
CO TO AA	422
CONTINUE	423
DO 120 I=1,4	424
AR-AL(I,LC)	423
BR=B1 ([,LC)	426
XR=Q(2,LC,1)	427
CR-88(1,LC)	428
IF(I-4) 135,136,136	429
CR-CR+XR	430
LL-LC-1	431
AL=A1(I, LL)	432
8L-81(1, LL)	434
VI = 0.19. I I . 1 1	
XL=Q(2,LL,1)	
XL=Q(2,LL,1) CL=8R(1,LL) IF(1-4) 137,138,136	435 426

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Applied to the control of the obtains about the second of the second for the obtained of the second
MAIN - EFN SOURCE STATEMENT - IFR(S)	03/04/69
138 C1=EP2=XA	4/1
C1=CR+C1+(BR+C1+AR)	439
C2=EP2=XL	440
C2=CL+C2+(BL+C2+AL)	441
îF(LC=2) 55,55,56	442
- 25 25 7	193
GO TC 58	444
56 .013-LC) 57.57.58	445
57 C1=G2 58 IF(1-4) 118.119.118	446
38 1 (~)	447
118 SB(I)=(C1+C2)/(2.+EP2)	448
GO TC 120	449
119 SB(I)=(C1+.2)/2.	450 451
ATT2=\$B(4)	452
PI=3.1415926536	433
	454
RAD=PI/180. C1=EP2+CC	495
C2=180.=ATT1+ATT2	456
IF(C2-90.) 150,150,151	457
151 C2= 180C2	ARA
C2=C2=R4C	459
CA=-COS ((2)	460 6
GO TC 152	461
150 C2=C2+RAC	462
CA=CCS(C2)	463 4
LSZ CSA-SIN(CZ)	464 4
EPP=SQRT(EP*EF+C1=C1-2.+C1+EP+CA)	465
CSB=C1+CSA/EPP	466
CCB=SQRT(1.=CSB+CSB)	467
CT8=CS8/CC8	466
TB-ATAN(CTB)	419 4
	470
TO-TR/RAC	471
EPS=EPP/(1.+CC)	472
	473
RCF2=(SR(1)+SR(2))/2.	
RCF2=(SB(1)+SB(2))/2. FT2=(SB(1)-SB(2))/(S2+EP2)	
FT2=(SB(1)-58(2))/(S2+EP2)	474
FT2=(\$B(1)-5B(2))/(\$2*EF2) C1=(1ART)/(1.*ANRT)	474
FT2=(\$B(1)-\$B(2))/(\$2*EF2) C1=(1ART)/(1.4ART) IF (INPRD.NE.1) C1=1.	474
FT2=(\$B(1)-\$B(2))/(\$2*EF2) C1=(1ART)/(1.*ART) IF (INPRO.NE.1) C1=1. C2=RCFM+C1	474 475 476 477
FT2=(\$B(1)-5B(2))/(\$2*EP2) C1=(1ARRT)/(1.*ARRT) IF (INPRO.NE.1) C1=1. C2=RCFM+C1 C1=\$1+FT+EP/2.	474 475 476 477 478
FT2=(\$B(1)-\$B(2))/(\$2*EP2) C1=(1ARRY)/(1.*ARRY) IF (INPRD.NE.1) C1=1. C2=RCFM*C1 C1=\$1*FT*EP/2. RCFI=C2-C1	474 475 476 477
FT2=(SB(1)-SB(2))/(S2+EF2) C1=(1ARRY)/(1.*ANRY) IF (INPRO.NE.1) C1=1. C2=RCFM+C1 C1=S1+FT+EP/2. RCFI=C2-C1 C1=EP2+S2+FT2/2.	474 475 476 477 478 479 480
FT2=(\$B(1)-\$B(2))/(\$2*EF2) C1=(1ARRT)/(1.*ARRT) IF (INPRO.NE.1) C1=1. C2=RCFM+C1 C1=\$1*FT*EP/2. RCF1=C2-C1 C1=\$P2*\$2*FT2/2. RCFU=RCF2+C1	474 475 476 477 478
FT2=(\$B(1)-\$B(2))/(\$2*EF2) C1=(1ARRY)/(1.*ANRY) IF (INPRO.NE.1) C1=1. C2=RCFM+C1 C1=\$1*FT*EP/2. RCFI=C2-C1 C1=\$P2*\$2*FT2/2. RCFU=RCF2*C1	474 475 476 477 478 479 480
FT2=(\$B(1)=\$B(2))/(\$2*EF2) C1=(1.=ARRY)/(1.*ANRY) IF (INPRO.NE.1) C1=1. C2=RCFM+C1 C1=\$1*FT*EP/2. RCFI=C2=C1 C1=\$2*\$2*FT2/2. RCFU=RCF2*C1 RIO=RCF1/RCFC ER=RIO=CC	474 475 476 477 478 479 480 481 482 483
FT2=(\$B(1)-\$B(2))/(\$2*EF2) C1=(1ARRY)/(1.*ARRY) IF (INPRO.NE-1) C1=1. C2=RCFM*C1 C1=\$1*FT*EP/2. RCF1=C2-C1 C1=\$P2*\$2*FT2/2. RCF0=RCF2*C1 RIN=RCF1/RCFC ER=RIO-CC IF(NSES1.NE-1) GO TO 86	474 475 476 477 478 479 480 481 482 483 484
FT2=(\$B(1)=\$B(2))/(\$2*EF2) C1=(1.=ARRY)/(1.*ARRY) IF (INPRO.NE.1) C1=1. C2=RCFM+C1 C1=\$1*FT*EP/2. RCFI=C2-C1 C1=\$2*\$2*FT2/2. RCFO=RCF2+C1 RICH=RCF1/RCFC ER=RIO-CC IF(NSES1.NE.1) GO TO 86 85 WRITE(6.525)REI,REZ,ANRY,CC,EP WRITE(6.525)REFI,RCFO.ER.S1.S2	474 475 476 477 478 479 480 481 482 483 484
FT2=(\$B(1)=\$B(2))/(\$2*EF2) C1=(1.=ARRY)/(1.*ARRY) IF (INPRO.NE.1) C1=1. C2=RCFM**C1 C1=\$1*FT*EP/2. RCFI=C2-C1 C1=\$2*\$2*FT2/2. RCFO=RCF2*C1 RIC=RCF1/RCFC ER=RIO-CC IF(NSES1.NE.1) GO TO 86 85 WRITE(6.525)REI,REZ,ANRY,CC,EP WRITE(6.525)REFI,RCFO.ER.S1.S2	474 475 476 477 478 479 480 481 482 483 484 485 5
FT2=(\$B(1)-\$B(2))/(\$2*EF2) C1=(1ARRT)/(1.*ARRT) IF (INPRO.NE.1) C1=1. C2=RCFM+C1 C1=\$1*FT*EP/2. RCFI=C2-C1 C1=\$2*\$2*FT2/2. RCFO=RCF2+C1 RIO=RCF1/RCFC ER=R1O-CC IF(NSES1.NE.1) GO TO 86 85 WRITE(6.525)REI.REZ.ARRT.CC.EP WRITE(6.525)REFI.RCFO.ER.S1.S2 WRITL(6.525)EF2.FT.FT2.RCFM.RCF2	474 475 476 477 478 479 480 481 482 483 484 485 5
FT2=(\$B(1)=\$B(2))/(\$2*EF2) C1=(1ARRY)/(1.*ARRY) IF (INPRO.NE.1) C1=1. C2=RCFM+C1 C1=\$1*FT*EP/2. RCFI=C2-C1 C1=\$2*\$2*FT2/2. RCFO=RCF2+C1 RICH=RCFI/RCFC ER=RIO-CC IF(N\$E\$1.NE.1) GO TO 86 85 WRITE(6,525)REI,RE2,ANRY,CC,EP WRITE(6,525)RCFI,RCFO,ER,\$1,\$2 MRITL(6,525)EF2,FT,FT2,RCFM,RCF2 WRITE(6,525) \$B(1),\$B(2),\$B(2),\$B(4),ATT1,ATT2	474 475 476 477 478 479 480 481 482 483 484 485 5
FT2=(SB(1)-SB(2))/(S2*EF2) C1=(1ARRY)/(1.*ARRY) IF (INPRO.NE-1) C1=1. C2=RCFM+C1 C1=S1*FT*EP/2. RCF1=C2-C1 C1=EP2*S2*FT2/2. RCF0=RCF2*C1 RIN=RCF1/RCFC ER=RIO-CC IF(NSES1.NE-1) GO TO 86 85 WRITE(6,525)RE1,RE2,ANRY,CC,EP WRITE(6,525)RCF1,RCF0,ER,S1,S2 WRITE(6,525)EF2,FT,FT2,RCFM,RCF2 WRITE(6,525) EF1,FT2,RCFM,RCF2 WRITE(6,525) EF1,FT2,RCFM,RCF2 WRITE(6,525) EF1,FT2,RCFM,RCF2 WRITE(6,525) EF1,FT2,RCFM,RCF2 WRITE(6,525) EF1,FT2,RCFM,RCF2 WRITE(6,525) EF1,FT2,RCFM,RCF2	474 475 476 477 478 479 480 481 482 483 484 485 5
FT2=(SB(1)-SB(2))/(S2*EF2) C1=(1ARRY)/(1.*ARRY) IF (INPRO.NE-1) C1=1. C2=RCFM+C1 C1=S1*FT*EP/2. RCF1=C2-C1 C1=EP2*S2*FT2/2. RCF0=RCF2*C1 RIN=RCF1/RCFC ER=RIO-CC IF(NSES1.NE-1) GO TO 86 85 WRITE(6,525)RE1,RE2,ANRY,CC,EP WRITE(6,525)RCF1,RCF0,ER,S1,S2 WRITE(6,525)EF2,FT,FT2,RCFM,RCF2 WRITE(6,525) SB(1),SB(2),SB(3),SB(4),ATT1,ATT2 86 IF(NA-1) 70,71,72 70 D1=ER	474 475 476 477 478 479 480 481 482 483 484 485 5 486 5 487 5 488 5
FT2=(SB(1)-SB(2))/(S2*EF2) C1=(1ARRY)/(1.*ARRY) IF (INPRO.NE.1) C1=1. C2=RCFM+C1 C1=S1*FT*EP/2. RCFI=C2-C1 C1=2P2*S2*FT2/2. RCFO=RCF2*C1 RIM=RCFI/RCFC ER=RIO-CC IF(NSES1.NE.1) GO TO 86 85 WRITE(6,525)REI,REZ,ANRY,CC,EP WRITE(6,525)REFI,RCFO,ER,S1,S2 WRITE(6,525)EF2,FT,FT2,RCFM,RCF2 WRITE(6,525) SB(1),SB(2),SB(4),ATT1,ATT2	474 475 476 477 478 479 480 481 482 483 484 485 5 487 5 488 5

	MAIN - FEN SOURCE STATEMENT - IFN(S) -	03/04/69	
71	16/01/04 do 20	494	* *
73	NA=2	495	• .
•	NA=2 Q3=AART D3=ER ANRT=(Q1+Q3)/2. GQ TC 3Q C1=ANRT	496	
	03=ER	497	
	ANRT=(Q1+Q3)/2.	498	
	GO TC 30	499	-
74	CL#ANRT	500	
	DI=EK ANRT=Q1+EN	501	
	ANRT=Q1+EN ND=NC+1	502	
	TE (About) ed man	503 504	
700	ÎÊ (ND-NN) 50,700,700 WRITE (4.702) NN	204	3
702	FORMAT (154 PIVERGED ARRED AR AN ARRED		521
	GO TO 201	• • • •	
72	1F(NA-3) 76,75,79"		
76	GO TO 201 IF(NA-3) 76.75,79 IF(D1-ER) 78.77.77 GL-ANRT	506	
	CL-ANRT	507	
	Oløer.	508	
		509	
	ANTI-(01-03)/2	510 511	
7.	00 IU 3U '	512	
	D3a6a	513	
	ANRT=(01+031/2	514	
	NA=3	515	
	GO TO 50	516	
75	Q2-AART	517	
	4e :	211	
	DR-SA	518	
*	AART = (Q1+Q3)/2. GO TC 50 D3=AART D3=ER ANRT = (Q1+Q3)/2. NA=3 GD TD 50 GZ=AART DZ=ER NA=4	518 519	
	CZ=\$R NA=4 DTA=G3=C1	520	
	DTA=G3-C1 C1=DTA=CTA	520 521	
	DTA=Q3-C1 C1=DTA=CT4 C2=(C1+C3-2.+C2)+2./C1	520 521 522	
	DTA=Q3-C1 C1=DTA=CTA C2=(C1+C3-2.+C2)+2./C1 C3=(D3-C1)/CTA	520 521 522 523	
	DTA=03-C1 C1=DTA+CTA C2=(C1+C3-c2+C2)+2./C1 C3=(D3-C1)/CTA IF(C2) BC.B1.B0	520 521 522 523 524	
é1	DTA=03-C1 C1=DTA=CTA C2=(C1+C3-2.+C2)+2./C1 C3=(D3-C1)/CTA IF(C2) B0,81,80 C4=-02/C3 GO TC 82	520 521 522 523	• • • • • • • • • • • • • • • • • • • •
#1 #0	DTA=03-C1 C1=DTA=CTA C2=(C1+C3-2.+C2)+2./C1 C3=(D3-C1)/CTA IF(C2) 80.81.80 C4=-02/C3 GO TC 82 DTA=.5+C3/C2	520 521 522 523 524 525	• • • • • • • • • • • • • • • • • • • •
#1 #0	DTA=03-C1 C1=DTA+DTA C2=(C1+D3-2.+C2)+2./C1 C3=(D3-C1)/DTA IF(C2) 80.81.80 C4=02/C3 GD TU 82 DTA=.5*C3/C2 C4=\$GRT(CTA#DTA-D2/C2)	520 521 522 523 524 525 527 528	
#1 #0	DTA=03-C1 C1=DTA=DTA C2=(C1+D3-2.+C2)+2./C1 C3=(D3-C1)/DTA IF(C2) 80.81.80 C4=02/C3 GD TD 82 DTA=.SeC3/C2 C4=\$GRT(CTA#OTA=D2/C2) IFIDTA) 83.84.84	5212 5223 5223 5225 5225 527 529	538
#1 #0	DTA=03-C1 C1=DTA#CTA C2=(C1+C3-2.+C2)+2./C1 C3=(D3-C1)/CTA IF(C2) 80,81,80 C4=02/C3 GD TG 82 DTA=.S#C3/C2 C4=SCRT(CTA#DTA-D2/C2) IFIDTA) 83,84,84 C4=C4	5212 5212 5223 5235 524 528 528 529 530	538
#1 #0 #3 (#4 (DTA=03-C1 C1=DTA#CTA C2=(C1+C3-2.+C2)+2./C1 C3=(D3-C1)/CTA IF(C2) 8C,81.80 C4=02/C3 GD TC 82 DTA=.5+C3/C2 C4=5CRT(CTA#DTA-D2/C2) IPIDTA) 83,84,84 C4=C4-CTA	52123456785228 52223456785228 52255228 5227852355555555555555555555555555555555	538
81 80 83 84 84	DTA=03-C1 C1=DTA=CTA C2=(C1+C3-2.+C2)+2./C1 C3=(D3-C1)/CTA IF(C2) 80,81,80 C4=02/C3 GD TO 82 DTA=.5*C3/C2 C4=5GRT(CTA+DTA-D2/C2) IPIDTA) 83,84,84 C4=C4-C4	52123456789012 555555555555555555555555555555555555	538
81 80 83 84 82	DTA=03-C1 C1=DTA#CTA C2=(C1+C3-2.*£2)*2./C1 C3=(D3-C1)/CTA IF(C2) 80,81.80 C4=02/C3 GO TG 82 DTA=.S#C3/C2 C4=SCT(CTA#DTA=D2/C2) IFIDTA) 83,84,84 C4=C4 C4=C4	521234567890123555555555555555555555555555555555555	538
81 80 83 84 82	DTA=03-C1 C1=DTA#CTA C2=(C1+C3-2.*£2)*2./C1 C3=(D3-C1)/CTA IF(C2) 80,81.80 C4=02/C3 GO TG 82 DTA=.S#C3/C2 C4=SCT(CTA#DTA=D2/C2) IFIDTA) 83,84,84 C4=C4 C4=C4	5212345678901223455555555555555555555555555555555555	538
#1 #3 #4 #2 79	DTA=03-C1 C1=DTA#CTA C2=(C1+C3-2.*C2)*2./C1 C3=(D3-C1)/CTA IF(C2) 80,81,80 C4=02/C3 GD TG 82 DTA=.S#C3/C2 C4=SCCT(CTA*DTA-D2/C2) IFIDTA) 83,84,84 C4=C4 C4=C4-DTA BNRT=Q24C4 GD TG SD G3-S1/(1.+ANRT) IF(PDS) 91,92,91	5212345678901234555555555555555555555555555555555555	538
#1 #3 #4 #4 #7 92	DTA=03-C1 C1=DTA#CTA C2=(C1+C3-c+C2)#2./C1 C3=(D3-C1)/CTA IF(C2) #0,81,80 C4=02/C3 GD TC 82 DTA=.5#C3/C2 C4=SCRT(CTA#DTA=D2/C2) IFIDTA) #3,84,84 C4=C4 C4=C4 C4=C4 DTA=024C4 DTA	5212345678901223455555555555555555555555555555555555	538
81 80 84 84 82 83 84 92 85 86 86 87 92 86 86 86 86 86 86 86 86 86 86 86 86 86	DTA=03-C1 C1=DTA=CTA C2=(C1+C3-2.*C2)*2./C1 C3=(D3-C1)/CTA IF(C2) 80,81,80 C4=02/C3 GD TU 82 DTA=.5*C3/C2 C4=1GRT(CTA*DTA=D2/C2) IPIDTA) 83,84,84 C4=C4 C4=C4=C4 C4=C4=DTA PNRT=Q2*C4 30 TO 50 33-S1/(1.*ANRT) IF(PDS) 91,92,91 PDI=0.0 30 TC 93	5212345678901234555555555555555555555555555555555555	538
81 80 84 84 82 83 84 92 85 86 86 87 92 86 86 86 86 86 86 86 86 86 86 86 86 86	DTA=03-C1 C1=DTA=CTA C2=(C1+C3-2.*C2)*2./C1 C3=(D3-C1)/CTA IF(C2) 80,81.80 C4=02/C3 GO TO 82 DTA=.5*C3/C2 C4=ECT(CTA*OTA-D2/C2) IFIDTA) 83,84,84 C4=C4-C4 C4=C4-C4 C4=C4-C5 C4=C4-C5 C4=C4-C5 C4=C4-C5 C4=C4-C5 C4=C4-C5 C4=C4-C5 C4=C4-C5 C4=C4-C5 C4=C4-C5 C4=C4-C5 C4=C4-C5 C4=C4-C5 C4=C4-C5 C4=C4-C5 C4=C4-C5 C4=C4-C5 C4=C5 C4=C4-C5 C4=C5 C4-C4-C5 C5 C5 C5 C6 C6 C6 C7 C7 C7 C7 C7 C7 C7 C7 C7 C7 C7 C7 C7	58123456789012345678955555555555555555555555555555555555	538
81 80 64 64 62 63 64 67 79 92 64	DTA=03-C1 C1=DTA#CTA C2=(C1+C3-2.*£C2)*2./C1 C3=(D3-C1)/CTA IF(C2) 80,81,80 C4=02/C3 GO TG 82 DTA=.S#C3/C2 C4=SCRT(CTA*DTA-D2/C2) IP(DTA) 83,84,84 C4=C4-DTA ANRT=Q24C4 GO TG 50 GO TG 50 FO TG	5222345678901234567890 555555555555555555555555555555555555	538
81 80 64 64 62 64 67 79 64 67 67 67 67 67 67 67 67 67 67 67 67 67	DTA=03-C1 C1=DTA#CTA C2=(C1+C3-2.*£2)*2./C1 C3=(D3-C1)/CTA IF(C2) #0.81.80 C4=02/C3 GD TG 82 DTA=.3#C3/C2 C4=SCRT(CTA#DTA=D2/C2) IFIDTA) #3,84,84 C4=C4 C4=C4 C4=C4 C4=C4-DTA NNT=024C4 BNT=024C4	522234567890123345 5522355555555555555555555555555555	
81 83 (83 (84 (84 (84 (84 (84 (84 (84 (84 (84 (84	DTA=03-C1 C1=DTA#CTA C2=(C1+C3-2.*£C2)*2./C1 C3=(D3-C1)/CTA IF(C2) & 0.81.80 C4=02/C3 GD TU 82 DTA=.3&C3/C2 C4=SCRT(CTA*DTA-D2/C2) IFIDTA) & 3.84.84 C4=C4-DTA NNT=Q24C4 GO TO 50 S3=S1/(1.+ANRT) IF(PDS) \$1.92.91 PDI=0.0 PDI=0.0 PDI=0.0 PDI=0.0 PDI=DS/(1.4ANRT) PDZ=PDS*(CCR2/COR1)**2/ANRT RITE(6.501)	5812345678901234567890123555555555555555555555555555555555555	549
81 83 64 62 63 64 64 67 67 67 67 67 67 67 67 67 67 67 67 67	DTA=03-C1 C1=DTA#CTA C2=(C1+C3-2.*£C2)*2./C1 C3=(D3-C1)/CTA IF(C2) & 0.81.80 C4=02/C3 GD TC &2 DTA=.3eC3/C2 C4=SCRT(CTA*DTA-D2/C2) IFIDTA) & 3.84.84 C4=C4=DTA NNT=Q24C4 GO TC SO S3=S1/(1.+ANRT) IF(PDS) \$1.92.91 PDI=0.0 PDI=0.0 PDI=0.0 PDI=DS/(1.4ANRT) PDZ=PDS*(CCR2/COR1)**2/ANRT RITE(6.501) RITE(6.503)	58552245678901234567890123 5855555555555555555555555555555555555	549 550
81 80 83 84 82 84 82 84 87 92 84 84 84 84 84 84 84 84 84 84 84 84 84	DTA=03-C1 C1=DTA#CTA C2=(C1+C3-2.*£C2)*2./C1 C3=(D3-C1)/CTA IF(C2) & 0.81.80 C4=02/C3 GD TU 82 DTA=.3&C3/C2 C4=SCRT(CTA*DTA-D2/C2) IFIDTA) & 3.84.84 C4=C4-DTA NNT=Q24C4 GO TO 50 S3=S1/(1.+ANRT) IF(PDS) \$1.92.91 PDI=0.0 PDI=0.0 PDI=0.0 PDI=0.0 PDI=DS/(1.4ANRT) PDZ=PDS*(CCR2/COR1)**2/ANRT RITE(6.501)	5812345678901234567890123555555555555555555555555555555555555	549

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SZA) REZ, EPZ. IZXABH REYNOL ATT. ANGLE TO TO CUTPUT! THECCENTA/C (IXEII-4)	DS NO EGGENT ANG. FORCE		SUPPLY	PRES SOMM	\$25 \$55 \$55	-133
2203H REYNOL ATT. ANGLE T PH GUTPUT) ATH ECCENTA/C	DS NO EGGENT ANG. FORCE	RIC TORQU		PRES SOMM	- 318	
PH GUTPUT) 17H ECCENTA/C 1(1XE11.4))	I NEVNI			PRES BOMM	920	
PH GUTPUT) 17H ECCENTA/C 1(1XE11.4))	I NEVNI		AZZAI			
ith eccentric (1xell-4))		C37E3	A 27A1	7	335	
ith eccentric (1xell-4))		C2/C1	# 27#1	· F	335	
+(1xEl1.4))						
					593	
L2H IMNER RIN	6 ,7(1×811.4				334	
LZH OUTER AIN:	6 .7(1X211.4	111			525	
TH CVERALL	A I I Y I I . A				111	
	,	• • •			597	
				+		
		···	. مديدة بين المسيدة بين البينان		146	
2	2H OUTER AIN 2H CVERALL 3 32.51,52	2H CVERALL . 6(1X811.4	2H OUTER RING ,7(1X511.4)) 2H CVERALL ,6(1X511.4)) 3 52.51,52	2H CVERALL (4(1XE11.4))	2H CVERALL (4(1X811.4))	2H CVERALL (4(1XE11.4)) 556 557

"魔者不是不不好了,不是想 有了好年中一人的一切是不是我不死人。"

		03/04/69
	HERA - EFA SOURCE STATEMENT - IFA(S) -	
	DE 2.3 (e1.A)	
	DC 23 J=1,N NP(1,J)=0	
20	CONTINUE	Š
	00 30 J=1,N	
	um 4	-
	NP(1,))=1 NP(M,J)=1	· <u>- ·</u> · · · · · · · · · · · · · · · · · ·
30	CONTINUE	6
35	KK=1	6
00	AN=N	6
	PI=3.14159265258979	
	DTHETA=2. +PI/AN	. 6
	DTHE2=Q.5/DTHETA	6
	PFIX(1)=PRES(1)	
	SPRITO=RINSP	•
	PFIX(3)-PRES(3)	
	IF (PPASS.EC.1) CO TO 105	6
7-	GU TO 108	
05		7
· • · ·	06LS1=-C6LSP G0 70 107	
0.8	DELSIA CELSP	
7 T	DC 599 L841,3	
u 1	IF(MPASS.EQ.2) GU TO 120	
	ANMI-SPRITO-1.0	,
	ANPL=SPRITO+1.0	
	GOR-COR1	
	SIGN=ANF1/ANF1	
	PFIX(2)=PRES(2)*ANP1	
	ALOVD=BLCVD	
	REN= 880 4 A NM1 4 (-1.)	
	30 TC 130	
20	SIGN==1.	
	COR=COR2	6
-	PFIX(2)=PRES(2)+(COR2/CGR1)++2/SPRITO	•
	ALOVD-BLCVD/R2R1	•
	REN=REO+(R2R1)++2+COR2/COR1+SPR ITO	9
30	ELVD=ALCVD	9
	RATLO-2.0*ALOVC	9
	DO 592 L7=1.3	
	EPS=EPS1(LT)	
	PPS=2. +PI+SIGN	
	DN1 =6. + TPS	
	RADIAN 017493292519943	
	GA1=GAM+RADIAN	
	EDT=0.0 CON2=CON1/REN	
	cune=cun1/ren Turq=-fal5e-	10
	TPS1=TPS/8.0	16
	TRQ=TP3/660	
	DELX-DTHETA	
	DELZ=RATLD/BHM1	16
	TPS1=\2.*P1)**2*2.*ELVC	<u>-</u>
	AMS=MS	ič
	DELZ S=DELZ	ič
	PHIMC=PHCOT=(1SIGN)+0.5	īi

HCRR - EFR SOURCE STATEMENT - IFA(S)	03/04/69
IND=}	112
FRO2-1.	113
1 3 = 3	114
12-11	115
1 DG 40 J=1,N	116
CC(L1.J)=0.0	117
AXL(L1, J)=0.	118
CZ(L1, J)=0.	119
A1(L1:2:J)=0:C	120
A1(L1,3,J)=0.C	121
) AF7(L2,J)=0.0	122
IFIIND.EC.213C TO 48	123
16(VENI) GD TC 48	125
L1#2	257
L2=12	126
IND=2	127
GD TC 38	128
NR=1	1,29
PN=MG1	130
nn-15	
ISS=1 OEL=CELZ	132 133
OEL-CELZ	4.73
DZ-C.5/CELZ	134 135
[\$=1]	136
7=0,0	137
) BET-BETA(NA) *AACIAN Deph-Dep(na)	138
and the first of the first of the contract of	139
ALPHEALPEA(NR)	140
ALMI=1ALPH ALTALI=ALPH+ALMI	
SINB=SIN (BET)	142 99
COSB=COS(3ET)	143 10
67 NO 3-6 1 N G+6 1 N B	144
COSB2=CCSB+CCSB	145
COT2 = COS #2/SIN #2	148
CLZ-CEL+CTHETA	147
IF(TCRQ) GO TE 1001	148
00 2,00 I=IS,PM	149
XX (1)=7	150
2COR=2/CCR	
ED 7CU=CBCACA147CDB	152
EDZR-EDCT+GANCCT+ZCOR	153
EPZG-EPZGH+PHIMC	154
00 2001 JeleN	153
SI=SIN(ANG)	156 10
CO=CCS(ANG)	157
H=1.+CO+EPZGH	158
H9(1,J)=+	159
UZ-SUANAL	160
HG=H+DEPH	†at
HGHR=HG/F	162
AX9(1,J)=(&CZ#+CO+&PZG+\$1)+\$1NB+P1+24.0	163
HG3=HG=+3	164
HGHR3=HG3/H3	165
\$1=1./\$IAB2	166
S2=~COSB/SING?	167

HERN - EFN SOURCE STATEMENT - IFN(S) -	03/04/69
RENR-REA+H	168
RENG=REN+HG	169
GXR=GTCF(RENP)+12.	170 111
GXG=GTCF(RENG)+12.	171 110
GZR=GZCF(RENR)+12.	172 11
	173 11
GZG=GZCF(RENGI+12.	174
\$5=(GXR4GZR+CCT2)	175
S6=(GXG4GZG+CCT2)	- · · ·
\$7=G2G#\$2	176
\$8=GZR+\$2	1.77
\$9=GZG+\$1	178 179
\$10=GZR#\$1	
5114-55/S6/HGFR3	180
\$12-1\$11+ALPH-ALPH	181
\$13=(\$7-\$8/HGFR3)/\$6/\$12	183
\$14-RENR/HG3/\$12+[1,-+GFR)/\$6	183
ALH3=ALFF=HG3	184
A1S=SINB+(ALH3+S6+S11-ALM1+S5+H3)/S12	
A2==ALM1={ALPF=55=513+58}=H3	186
A2=(A2+ALH3+(ALH1+S6+S12-S71)+SINB	
A3=ALTAL1+S14+(S6+HG3-S5+H3)/REN	188
A3=CCN1+(A3+H+ALM1+HG+ALPH)+SINB	189
DHY=H3 +AL H1	190
S7H=HGHA3+S7	191
BIS=-H3/S12#(S8#ALM1-S7F#ALPF#S11)#S1NB B2=ALH3#(S9-S7#S13#ALM1)#DMY#(S10#ALPF#S8#S13)	192
B2=ALH3+(S9-S7+S13+ALM1)+DMY+(S13+ALP++S8+S13)	
B3=CCN1+ALTAL1+S14+(S6-S7H)	194
82=-82*SIN8	195
AX1(I,J)=A1S+A2+COSB	196
B3==B3+H3+SINE/REN	197
AX2(I,J)=42+SAB	198
WS11(I,J)=S11/S12	199
WS12(I,J)=1,/S12	200
WS13(I,J)=S13	201
H2+(I,J)=\$14	202
A3(1,1)=A3	203
AX6(1,J)=B15'+82*COSB	204
AX7(I,J)#82#SIN8	205
AX8(I,J)=B3	206
IF(MC.NE.Z) GO TO ZCOL	207
IF (I.ec.IS. ANC.J.EQ.1)	208
1 WRITE(6,2) AX1(1,J),AX2(1,J),AX3(1,J),AX4(1,J),AX7	1 209
11,J),AX9(1,J),AX9(1,J)	210 130
ANG=ANG4CTHETA	211
A NG=U.J	212
IF(I.EQ.PM) GC TO 2000	213
Z=Z+DEL	214
CONTINUE	215
IS(NR.EC.1) GC TO 201G	216
IF(NR.E3.3) GC TO 2014	217
IF(VENT) GO TC 2014	218
GO TO 2020	219
[K=1	220
GO TC 3800	221
IK=M#	222
CO YE 3800	223

	MERA - EFN SOURCE STATEMENT - [FN(S) -	/69
·	COMPUTE THE DIFFERENCES IN XS AND COEFFICIENT	224
1000	I I K DO 4 1 1 1 1 1 1 1 1 1	225
	DO 4010 J=1,K	226
	AFL(1:1)=0.0	227
	AF2([,J)=0.0 AF2([,J)=0.0	228
	AF3 (1. J)=0.0	229
	AP4(1.J)=0.0	230
	AFAII Abai	231
	AFTI - 11 mpZ TY (Ap)	232
010	CONTINUE	234
***	TETETELS	235
454	PMI = PM= PMI = PM=	236
	DO ADD THIST MM1	237
	10=1=1	238
	#F3([,J)=0.0 AF4([,J)=0.0 AF5([,J)=0.0 AF6([,J)=1.0 AF7([,J)=FFIX(NR) CONTINUE 	239
	[7-1+1 DD 4300 J=1,N DTH=DTHE2 IF(J=EQ-1=DR-J=EQ-N) GD TD 4004 JO=J=1 J1=J+1	240
	OTH-OTHE2	241
	IF(J.EQ.I.DR.J.EQ.N) GD TO 4004	242
	J0=J=1	243
	_17=1+\$	244
	GO TC 4008	245
004	IF(J.EQ.1) GO TO 4006	246
		247
	11 m1	248
	GO TC 4008	249
000	J0=N-1 GC TC 4006 IF(J.EG.1) GC TC 4006 JO=N-1 J1=1 GC TC 4008 J0=N	250
	J1=2 AF1(1,J)=\$inb=ax7(1,J)	251
na	AF2(1.J)=(AX2(1.J1)=AX2(1.J0)+COSB+(AX7(1.J1)=AX7(1.J0)))+DTH	252 253
	1 +SINE+(AX7(I7,J)=AX7(IQ,J))+DZ	254
	AF3(1,J)=AX2(1,J)+COSB=AX7(1,J)+SINB=AX6(1,J)	255
	HTD#11(OL.1)#XA=(1.J)#XA+0#B2O3#(DL.1)1XA+(1.J)1XA)#BA-	23 8
	HTD#((OL, I)&KA=(IL,I)&KA)#820>(OL,I)IXA~(IL,I)XA)#61-1)#4AA ZD#((L,OI)AXA-(L,I)XA)#617-1	256 257
	TOTAL TOTAL TOTAL TO THE STATE OF THE STATE	257 258
	I	257
	T	257 258
	I +5!W#(Ax6(17,J)-Ax6(10,J))#DZ AF5(1,J)=Ax1(1,J)+COS##Ax6(1,J) AF6(1,J)=0-0 AF7(1,J)=CAX3(1,J)=Ax3(1,J)+CX3(1,J)+DX+Ax6(1,J))#DTH I +5!N##IAX6(17,J)=Ax3(1,J)#DZ+Ax4(1,J)#Ax4(1,J))#DTH	257 258 259
	I +\$!WE#(Ax6(17,J)-Ax6(10,J))#DZ AF\$(I _p J)=Ax1(I,J)+COS##Ax6(I,J) AF\$(I _p J)=Ax1(I,J)+COS##Ax6(I,J) AF\$(I _p J)=O=O AF\$(I _p J)=OOO AF\$(I _p J)=OOOO AF\$(I _p J)=OOOOO AF\$(I _p J)=OOOOOOOOOOOOOOOOOOOOOOOOOOOOOOOOOOOO	257 258 259 260 261 262
	I +\$!W#\(Ax6(17,J)=Ax4(10,J)) +DZ AF\$(I _p J)=Ax1(I,J)+COS##Ax4(I,J) AF\$(I _p J)=0.0 AF\$(I _p J)=0.	257 258 259 260 261 262 263
	I +\$!W#(Ax6(17,J)=Axe(10,J))=DZ AF\$(I _p J)=Ax1(I,J)+COS#+Ax6(I,J) AF\$(I _p J)=0.0 AF7(1 _p J)	257 258 259 260 261 262 263 264
	I	257 258 259 260 261 262 263 264 265
	I	257 258 259 260 261 262 263 264 265 256
	I -SINE*(Ax6(17,J)-axe(10,J)) = DZ AFS(I _p J)=axl(I,J)+cose=ax6(I,J) AF6(I _p J)=axl(I,J)+cose=ax6(I _p J) AF6(I _p J)=axl(I,J)-axs(I _p J)+cose=(ax8(I _p J))-axe(I _p J)) + DTH I +SINE*(Ax6(I _p J)-axe(I _p J)) + DZ+axe(I _p J)-axe(I _p J)) + DTH IF (MD _p Eq _p 2 ,and _p J _p Eq _p I	257 258 259 260 261 262 263 264 265 256 267
	-\$!\deta(17,J)-\axe(10,J)) = DZ AF\$([p_J)=\axi(1,J)+\cos\deta(10,J)) = AF\$([p_J)=\axi(1,J)+\cos\deta(10,J))	257 258 259 261 262 263 264 265 267 268
	-\$!\dev(ax6(17,J)-axe(10,J))+DZ AF\$([,J)=Ax1(I,J)+COS8+Ax6(I,J) AF\$([,J]=0.0 AF7(1,J)=0.0 AF7(1,J)=0.0 AF7(1,J)=0.0 AF7(1,J)=0.0 AF7(1,J)=0.0 AF7(1,J)=0.0 AF7(1,J)=0.0 AF7(1,J)=0.0 I -\$!\dev(ax6(17,J)-ax3(I,J)+COSB+(ax8(I,J)-axe(I,J))+DTH I -\$!\dev(ax6(17,J)-ax3(I,J)+DT+(ax8(I,J)-ax4(I	257 258 259 260 261 262 263 264 265 256 265 268 269
oaa	+\$!\delta(in,j) = axe(in,j)	257 258 259 260 261 262 263 264 265 256 267 268 269 270
000	-\$!\dev(ix6(17,J)-axe(10,J))+DZ AF\$([,J)=ax1(1,J)+cOs8+axe(1,J) AF\$([,J)=0.0	257 258 259 260 261 262 263 264 265 265 267 268 270 271
000	-\$!\deta(17,J)-axe(10,J))=DZ AF\$(IpJ)=AX1(I,J)+COS\$*AX6(I,J) AF\$(IpJ)=AX1(I,J)+COS\$*AX6(I,J) AF\$(IpJ)=(AX3(IpJ)-AX3(IpJ)+COSB*(AX8(IpJ)-AX8(IpJ))+DTH -\$!\deta(17,J)-AX3(IpJ)-AX3(IpJ)+COSB*(AX8(IpJ)-AX8(IpJ))+DTH If (MD.Eq.2.aND.J.EC.1) If (MD.Eq.2.aND.J.EC.1) WRITE(0,2) AF\$(IpJ)-AF\$(IpJ	257 258 259 260 261 263 264 265 267 266 267 268 270 271 272
000	-\$!\deta(17,J)-axe(10,J))=DZ AF\$(IpJ)=AX1(I,J)+COS\$*AX6(I,J) AF\$(IpJ)=AX1(I,J)+COS\$*AX6(I,J) AF\$(IpJ)=(AX3(IpJ)-AX3(IpJ)+COSB*(AX8(IpJ)-AX8(IpJ))+DTH -\$!\deta(17,J)-AX3(IpJ)-AX3(IpJ)+COSB*(AX8(IpJ)-AX8(IpJ))+DTH If (MD.Eq.2.aND.J.EC.1) If (MD.Eq.2.aND.J.EC.1) WRITE(0,2) AF\$(IpJ)-AF\$(IpJ	257 258 259 261 262 263 264 265 267 268 269 270 271 272 273
000	-\$\$\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	257 258 259 261 262 263 264 265 267 268 269 270 271 273 274
000	-\$\$\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	257 258 259 260 262 263 264 265 265 267 268 269 270 271 273 274 275
000	-\$\$\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	257 258 259 260 261 262 263 264 265 268 269 270 271 272 274 275 276
000	-\$!\deta(17,J)-axe(10,J))=DZ AF\$(IpJ)=AX1(I,J)+COS\$*AX6(I,J) AF\$(IpJ)=AX1(I,J)+COS\$*AX6(I,J) AF\$(IpJ)=(AX3(IpJ)-AX3(IpJ)+COSB*(AX8(IpJ)-AX8(IpJ))+DTH -\$!\deta(17,J)-AX3(IpJ)-AX3(IpJ)+COSB*(AX8(IpJ)-AX8(IpJ))+DTH If (MD.Eq.2.aND.J.EC.1) If (MD.Eq.2.aND.J.EC.1) WRITE(0,2) AF\$(IpJ)-AF\$(IpJ	257 258 259 260 262 263 264 265 265 267 268 269 270 271 273 274 275

HERN - EFN SOURCE STATEMENT - IFNIS) -	03/04 69
TRSZ-TRS+DZ+2.0	280
A1(I1.4.J)==TRSZ	261
A1(11,2,J)=A1(11,2,J)=TRSZ*EFD2	_282
DUT#AX6(IE.J)+CTHE2	283
CC(II,J)=CZ(II,J)=COT	284
C2411431-C01	207
B1(II.J)=-CC(II.J)	286
Al(II+3,J)=Al(II,3,J)+TRSZ	287
AF7(IE, J)=AXL(II,J)-AX8(IE,J)	288
AXL(II,J)=Aye(IE,J)	289
AF1(1E, J)=0.0	290
AF2(IE, J)=0.0	291
AF3([E,])=0.0	292
AF4(IE, J)=J.D	293
AF5(IE, J)=0.0	294
AF6(IE, J)=0.0	295
IF(MC.EQ.2.AND.J.EC.AN)	296
1 WRITE(6,2) A1(11,2,J),A1(11,4,J),A1(11,3,J),B1(1	
1) (CC(II, J), AF7(IE, J)	298 28
LOG CONTINUE	299
IF(NR.EC.1) GC TO 4102	300
GD TC 4150	301
lQ2 IS=I1	302
NR=2	303
KW=[2	304
ER 02 = 0.	305
OEL=CEL ZS	306
CZ=J.5/CELZS	307
GO TC 200	308
60 IF(VENT) GO TC 4190	309
IF(KK.EC.1) GC TO 418C	310
IS=I2	311
MM=M	312
NR#3	213
ERO2=0.	314
DEL=CELZ	315
CZ=3.5/CELZ	316
GO TC 200	317
L80 IE=12	318
ERO2=1.	319
KK=2	320
11#2	321
GD TC 4090	322
ISO IF(NR.EC.2) GC TO 4160	323
L90 MTSR=MD	324
MD =FTSR	325
CALL CIC1 (MC)	326 31
MC=0	327
PPOUT=.FALSE.	328
IF (KDIAGANEA1) GO TO 571	329
IF(IAD3.EQ.1.CR.IND3.EQ.2) PPOUT=.JRUE.	330
IF(PPOUT) WRITE(6,9)	331 32
571 DO 575 1•1, M	332
[F(PPOUT) WRITE(6,4)(PHI(1,J),J=1,N)	333 33
00 575 J=1,N	324
KUPT(I, J)=0	335

いたが、このでは「ここ」 教徒の事を教育の教育をはませるを見るのではませい。本語に

		03/04/69	
	HERR - EFN SOURCE STATEMENT - IFA(S)		
	IF(PHI(I:J).GE.O.O) GC TO 575 PHI(I:J)=O.O KUPT(I:J)=1 CONTINUE DIMERSICALESS FLOW IP=I1=1 AFLOW=J.C	336	
	PH111.11=0.0	337	
	MIND TT. I) = (338	
246	CONTINUE	338 339	•
6 313	CURITATION TO REPORT TO THE PROPERTY OF THE PR	339 340 341	
6	DIMENSICALESS FLUM	341	
	ibalial	342	
4204	IP=12-1 AFLOW=J.C DO 4200 J=1.N IF(J.EQ.1.OR.J.EQ.N) GO TO 4220 VF1=(PHI(IP,J+1)=PHI(IP,J+1))+CTHE2	343	
	00 420ù J=1.N	393	
	TELL_EQ_1_QR_J_EQ_K1 EU TU 0/2U	344	
	YF1={PHI(IP,J+1}=PHI(IP,J=1})*CTHE2 AFLOW={YF1*AXE(IP,J)}+AXE(IP,J)+AX7(IP,J)*(PHI(IP+1,J)=PHI(IP=1,.	345	
4210	AFLOW=(YF1+AX6(IP,J))+A4(LP,J)+AA+(TP,J)+(PH1)IP+1-J)-YA+(IP-1-	J) 390	
	L)*DZ+AFLCW	347	
	IF(MCIAG.EG.2) WRITE(6.2)YF1,AFLOW	348	364
	GO TC 4230	349	
A220	1F(J.EQ.N) GC TO 4230	350	
4660	YF1=(PH1(1P,2)=PH1(1P,N))+DTFE2	351	
	GO TC 4210	352	
4440		353	
4230	YF1= (PHI(IP, 1) - PHI(IP, N=1)) +CTHE2	354	
	GO TC 4213	355	
4200	CONTINUE		
	AFLOW=AFLOW+DT+2TA/12.	356	
Ç	TORQUE CIVIDEC BY MUXAXRXRXRXC	357	
	NR=1	358	
	TORQ=-TRLE. TQ=J.u	359	
	Te=3.0	360	
		361	
	172=[1	362	
	761-6 A	363	
		364	
1001	GO TC 20C DD 1999 I=IT1+IT2 DD 1999 J=1+N TEKKUPT(I=I)-EC-1) GC TC 166C	365	
Toot	50 1300 1-114112	366	
	1F(KUPT(1,J).EC.1) GC TC 10CG	367	
	IFRUPICIO DE LA COLOR DE LA CO	368	
	IF(I.ēq.IT1.CR.I.eq.IT2) GD TO 180G DPDZ=(PHI(I+1,J)=PHI(I=1,J))/DZ		
		369	
	AFTR=1.0	370	
1200	IF(J.EQ.1.OR.J.EQ.N) GO TO 1600	371	
	OPOT=(PHI(I,J+1)=PHI(I,J-1))+DTHE2	372	
1240	H=H9 (I,J)	373	
	BQ=H+ALTALi+CEPH	374	
	AC=(-80+COS8+KS13(1-J)-++ALP1+WS12(1-J)-ALPH+WS11(I-J)+(H+CEPH))	+ 375	
	8Q=H+ALT#L1+CEPH AQ=(-8Q+COS8+h513(I,J)-++AL#1+HS12(I,J)-ALPH+HS11(I,J)+(H+CEPH1) 10PDT	376	
	AD=AC+RC+(=CGN2+MS:4(1.J)=MS!3(1.J)+DPDZ+SINB1	377	
	AQ=AC+BC+(-CGA2+HS14(I,J)-HS13(I,J)+DPDZ+SINB) TQ=TG+AC+DLZ+C.5+AFTR	378	
	GO TC 1010	379	
		380	
Tèda	IF(J.EQ.A) GC TO 1610	381	
	OPDT=(PHI(I,2)=PHI(I,N))+DT+52	382	
_	GD TC 1240		
1613	DPDT=(P+[([,1)-PHI([,K-1)]+CTHE2	383	
	GD TC 1240	384	
1800	AFTR=.5	385	
	IF(1.Eq.IT2) GC TO 1810	386	
	ĎPĎŽ=(PFI(IT1+1,J)-PFI(IT1,J))/CELZ	387	
	GG TC 1200	388	
1810	OPD2=(PHI(IT2.J)=PHI(IT2=1.J))/DELZ	389	
	GO TC 1200	390	
1010	RE=REN#H	391	
7010	ur and relation		

	HERN - EFN SOURCE STATEMENT - IFN(S) -	/04/69	
	TC2=TGC(FE)+ALFI	392	432
	RE=REN#(F+DEPF)	393	
	TC1=TC1+(TC2+TCC(RE)+ALPH)+TRQ+DLZ+AFTR	394	431
	IF (J. NE. 1) GO TO 1000	395	
	IF(MC.EC.2.ANC.I.EQ.IT1)	396	
		397	431
COO	CONTINUE	398_	
	IF(MC.EC.2)WAITE(6,2)WS11(I,J).WS12(I,J).WS13(I,J).WS14(I,J)	399	774
	IF(NR.EC.1) GC TO 1400	400 401	
	TF(NR.EC.2) GC TO 1410	402	
	GD TC 578	403	
400	NR=2	404	
	IT1=11 IT2=12	403	
	GO TC 203	406	
41 0	IF (VENT) GO TC 578	407	
-7 & U	NR=3	408	
	171:12	409	
	112=1	410	
	GO TC 200	411	
578	T00=(T0+TC1)	412	
- 1	THE=0.0	413	
	DQ 380 J=1.N	414	
•	QQQ(J)=SIN(THE)	415	466
	CQQQ(J)=COS(TFE)	416	470
580	THE=CTHETA+THE	417	
	00 593 1=1,M	418	
•	PP(I)=9.C	419	
	PPP(1)=0.0	420	
	00 600 J=1.N	421	
	CUM=PHI(1,J)	422	
	PP(1)=PP(1)+CCC(J)+CUM	423 424	
600	PPP(I)=PFP(I)+CCQQ(J)+CUM		
	PP(I)=FP(I)+CTFLTA	425	
	PPP(I)=FPP(I)+CTHETA	427	-
EGA	PPX(I)=FF(I)*XX(I) PPPX(I)=FPP(I)*XX(I)	428	
774	FSIN=SUM(PP.M.CELZ)	429	501
	FCOS=SUM(PPP,M,DELZ)	430	502
	FMSI N=SUP (PPX, P, DELZ)	431	503
	FMCOS=SUP(PPPX.M.DELZ)	432	504
	FCOS==FCCS		
	FNCOS==FPCOS		
	IF (KDIAG.NE.1) GO TC 594	435	
	WRITE(6,6)FSIN, FCOS	434	501
	WRITE(6,71FMSIN,FMCOS	435	508
594	hLOAC=FCCS++2+FSIN++2	436	
	WLUAC=ABS(WLCAC)	437	
	WLOAD=SQRT(WLCAD)	438	510
	SOMER=2.00*ELVC/WLOAC		
	PHEE=ATAN2(FSIN, FCOS)	440	511
	PHEE=PHEE/RACIAN	441	
	TQG=TQO/WLOAD	445	
	TQI=TQO4EPS+FSIN/WLOAC	446	
	WRITE (6.2) REN, EPS, TGI, TQD, SOMER, PHEE, AFLOW	447	512

· 计记录 网络阿朗维斯 计一个经济,该国际 医双线输出统治,如果他

HERN - EFE: SOURCE STATEMENT - IFN(S) -	ù3/04/69	
MRITE(10) REN.EPS.:GI.TGD.SOMER.PHEE	449	515
GO TC 591	450	
593 WRITE(9) REN, EPS, TQ1, TQU, SOMER, PHEE	451	517
591 INDS-INC3+KO IAG	452	
592 CONTINUE	453	
549 SPRITG-SPRITC+CELSI	454	
RETURN	455	
END	456	

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51 52

53 54

A(I, I-2)-A1(1,1,J) A(I, I-1)-A1(1,2,J)

A(I,I+1)=A1(1,4,J) A(I,I+2)=A1(1,5,J) B(I,I)=B1(1,J)

A(1,1)=A1(1,3,J)

							o:	3/04/69	
	CICI.	- EFN	SOURCE	STATEMENT	-	IFN(S)	-		
	C(1:1)=CC(::J)							57	
600	AFJI(1)=-AF7(1							58	
	GO TC 250							59	
	1F(NP(1,J1)209							60	
	IF(I-MG1-MS-1) IF(MS) 214,215		• 412					61 62	
	DZ1=0.5/CELZ	1614						63	
	D22=(1./CELZ)+	<u>*2</u>						64	
	IF (NC. 85.2) GC							65	
	A(1,1-2)=A1(2,							66 67	
-	A(1, 1-1)=A1(2, A(1, 1)=A1(2, 3, A(1, 1)=A1(2, 3, A(1, 1)=A(1, 1)=A(•		68	
	A(1,1+1)=A.(2,							69	
	A(1:1+2)=A1(2:							70	
	B(1.1)=81(2.J)							71	
401	C(1,1)=CC(2,3) AFJ1(1)==AF7(1							72 73	
	GO TC 250	• • •						74	
215	IF(NC+6C+2) GC B(I+1+1)=AF3(1	TO 632				•		. 75	
	B(I,1-1)=AF3(1	.J)+CX1+	DZ.	_				76	
	B(1,1)=AF5(1,J B(1,1+1)=~AF3(1+DX2=4F	→(I,J)+DX	1				77	
	A(1.1-1)=AF((1) +0.2.2-	AF2(I.J)*	EZ1				79	
	A(1,1)=AF6(1,J	102.54(4	F1(I,J)*0	22 +4F511.	J)+DX	121		80	
	U(1,1)=AF5(1,J B(1,1+1)=~AF3(A(1,1-1)=AF1(1 A(1,1+1)=AF1(1 A(1,1+1)=AF4(1,J C(1,1+1)=AF4(1,J C(1,1+1)=AF4(1,J C(1,1+1)=AF2(1	,J)+CZ24	AF2(1,J)+	DZ 1				91	
	C(1,1-1)=+AF3(I.1)+DX	*[2]	•			****	82	
	C(1.1+1)=AF2(1	*73*CX*4	C71	•				84	
602	AFJI(1)=~AF7(I	, 11						85	
250	CDIAL THAT					1		86	
	IF(NC.EC.2) GC	TO 503						97 88	
	00 260 I=1.M							89	
	AK([.]])=A(],]	1)						90	
	00 260 111=1.P							91	
263	AK([,[])=AK(],			1+11)				92 93	
	IF(MCIAGeLTe2) WRITE(6:101)J	60 10 2	₹ 4					94	188
	DG 201 1=1.M							95	
	WRITE(6,100) (96	191
	CALL MATINVIAK	. M. DUM. C	*COMI)				•	97	198
623	CONTINUE CD 404 1=1,#							98 99	
	BF(1)=AFJ!(1)							100	
	F(J+1,1)=0.							101	
	DO 404 II=1+M							102	
	£(1,11)=C.							103 104	
	8D{[,]]}=U. CU 4U3 1 =1.P							105	
	E(1,11)=f(1,11		11)+0(111	.11)				106	
	8D(1.11)=8C(1.	11)+2(1,	111)*C(11					107	
404	BF(1)=8F(1)8(1, I1) * F(J, II)					108	
	DD 496 I=1.M							109 110	
	D(1.11)=0.							111	
	CO 4J5 III=1.P							112	

-		4/49	
	CICIO - EFN SOURCE STATEMENT - IFA(S) -		
405	D(1,11)=C(1,11)-Ax(1,111)+8D(111,11)	113	
405	f(J+1,1)=f(J41,1)+AM(1,11)*BF(11)	114	
300	CONTINUE	115	
	00 505 I+1,K	116	
	CU 504 11=1,#	117	
20 T	CU 504 []=1,# DP([,[])==C(],[]) DD([,[])=1.+DC([,[])	118 119	
	DO(1,1)=1.+DC(1,1) IF(MDIAGaLT-2) GD TD 264 WRITE (6,101) DD 263 [=1,M]	120	
	WRITE (6.101)	121	267
	DO 263 I=1,M	122	
263	URITE (6:100) (CD([:II]:II=I:M) CAI MATTNY(FF. M. DUM-O. FUM)	123	271
264	CALL MATINV(CC, M, DUM, O, CUMI) DO 507 I=1, M \$(N, I)=G. DU 507 II=1, M GN(I, II)=G. DO 506 III=1. M GN(I, II)=GN(I, III+CO(I, III)+E(III, II) G(I, II)=GN(I, III+CO(I, III)+E(III, II)	124	279
	DU 507 1=1,M	- 125 -	
•	31mg17=U6	147	
	GN(I. I I) = 0.	134-	
	DO 506 [1]=1.W	129	
	GN(1,11)=GN(1,11)+CO(1,111)+E(111,11)	130	
506	G(1,11)=GN(1,11)		
507	G(1,11)=GN(1,11) S(N,1)=S(N,1)+CD(1,11)+F(N+1,11)	132	
	GATTER CONTRACTOR OF THE STATE	133	
	DO 512 K=2.N	135	309
· · · • · · ·	DO 512 K=2.N WRITE(8) ((G(1,11),[=1,*),[[=1,*]] BACKSPACE 7 PEADITA ((G(1,11),[],[],[],[],[],[],[],[],[],[],[],[],[],	136	317
	READ(7) ((E(I.11).D(I.11).I=1.M), II=1.M) BACKSPACE 7	137	316
· <u>-</u>	BACKSPACE 7	130	327
		139	328
		140	
	DG 309 I=1,K S(J=1,I)=F(J,I)		
	00 509 II=1,M	143	
	GI(1.11)=3.	144	
	ED 508 111=1.N	145	
• • • • • • • • • • • • • • • • • • • •	DO 508 111=1.0 G1(1,117=G171,11)+d(T,111)+GN(111,11)+E(T,111)+G(111,11) 1F(MC1AG.NE.2) GO TO 508 CONTINUE	146	
	IF(MDIAG.NE.2) GO TO 508	147	
500	GONTINUE	148	
301	CONTINUE S(J-1.1)=S(J-1.1)+E(I.II)+S(J.11)+D(I.11)+S(N.II) DO 512 J=1.M	-137	
	00 512 1=1,M CD 512 II=1,M G([,II)=G([,II]) DO 511 I=1,M	151	
512	G([, II) • GI([, II])	192	
280	DO 511 I=1,P	153	
	CO 210 11-11"	154	
	DD([,[])==G((,[])	122	
241	CD(1,1)=1.0CC(1,1) TE(MDIAG.:1.2) GD TO 266	1 47	
	WRITE (6.101)	· 158	396
	DO 265 [=1,M	159	
265	WRITE (6,100) (LD(1,11), 11=1,M)	160	400
266	MRITE (6,101) DD 265 I=1,M WRITE (6,100) (U0(I,II),II=1,M) CALL MATINY(DC,M,DUM,C,CUM1) TE(MRIAG,IT,2) GD TO 270	161	408
	I the same of the same	162	
	1=0 WAITE (6,101)1	TOS	413
	DO 273 I=1.M	165	743
213	DO 273 [=1,M WRITE (=1,00) (DD(1,f1),1[=1,M) DD 813 [4].M	166	417
270	DQ 515 [41,H	167	
	i 41(1,1)=0	168	

・ 様の 一世の話の の一番 通りの 連接権 ロックル・

ALA _ SEN ADURAG AVATEMENT . TRACA	03/04/07
CICI EFN SDURCE STATEMENT - IFN(S) -	
00 515 II=1,H	169
00 515 11=1,H 515 PHI([,1]=0D(1,11)+S(1,11)+PHI(1,1)	169 170
00 516 J=2+N	171
BACK SPACE 8	172 441
READ(8) ((G(1,11),1=1,M),IT=1,M)	173 442
TACKSPACE 8	174 450
DD 516 I=1, M	175
PHI(1,J)=S(J,I)	176
DO 516 Il=1.M	177
516 PHI(I,J) PHI(I,J)+G(I,II)+PHI(II,1)	178
REWIND 7	179 465
REWIND 8	180 466
IF (PC.EQ.2) GC TC 110	181
IF(MCIAG.LT.2) GO TO 268	182
110 WRITE (6-102)	183 473
DO 267 1-1.H	184
267 WRITE (6.100) (PHI(I.J).J=1.N)	185 477
268 RETURN	186
100 FORMAT(1x.1P1GE11.4)	187
101 FORMAT(SPOCICI, IS)	186
	189
102 FORMAT(110.30X10HFINAL PHI /1HO) 103 FORMAT (1X.197611.4)	190
END	191
END	474

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C REDUCE NON-PIVOT ROWS

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MATH EFN SOURCE STATEMENT - IFA(S) -	03/04/67
380 DO 550 L1=1, A	37
390 1F(L1-ICCLU) 400, 550, 400	50
400 Y=A(L), (COLU) 420 A(L), (COLU)=0.0	59
430 BO 450 L=1,N	60 61
450 A(L1,L)=A(L1,L)=A(ICGLU ,L)+7	62
455	63
460 DO 500 L=1,M	64
500 B(L1,L) = E(L1,L) = B(ICCLU ,L) + T	65
990 CONTINUE	66
INTERCHANGE CCLUKAS	67 68
400 DG 710 1-1.N	70
610 L=N+1-[620 IF (INDEX(L,1)-INDEX(L,2)) 620, 710, 630	71
020 IP (INDEX(L)1 = INDEX(L)2) 030, 710, 630	72
63G JRON=INCEX(L,1) 640 JCOLU = INDEX(L,2)	73 74
650 DU 705 K+1,N	75
650 DU 705 K#1,N 660 SWAP#A(K,JRCH)	76
470 A(K, JROW) A(K, JCOLU) 780 A(K, JCOLU) SWAP	
	76
705 CONTINUE 710 CONTINUE	79
TAG RETURN	80 91
END to the second of the secon	. 74

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							03/04/69	
	GTCF.	FFN	comece ci	ATEMENT	<u>= 154(5)</u>			
	FUNCTION GT	CE (REVS)				and the second second		,
	RE=REYN	O. (E.)					-	
• · · · •	IF (RE-LE-70.)	100 TO 20		•			· · · · · · · · · · · · · · · · · · ·	
	IFICRE.GT.70.	C).ANC.(RE						
10	IFILRE.GT.200				40		6	•
	IFICRE.GT.550		E.LE.2.0E4	104]]) <u>G</u> O Ț	0 50		7) The state of the
	GTCF=2J.5/(RE	1++0.784					•	14
	RETURN)
20	GTCF#1.0/12.0						10)
	RETURN							
ЭO	GTCF=.619E=08	+(RE)++2-3	465 E- 05*RE	+.08569			12	
	RETURN						13	l
40	GTCF=4.9G/(RE	144.628					14	18
	RETURN						15	i
50	GTCF=10.35/(R	E)**.716					16	20
	RETURN						17	•
	END		•				18	

GZCF EFN SOURCE STATEMENT - [FN(S) -	03/04/69
FUNCTION GZCF(REYN)	
RE-REYN	3
IF(RE.LE.70.0)GO TO 20 IF((RE.GT.70.G).AND.(RE.LE.4000.0))GO TO 30	4 5
10 1F((RE.GT.4000.0).ANC.(RE.LE.7.0E403)) GO TO 4C IF((RE.GT.7000.0).ANC.(RE.LE.2.0E404)) GO TO 90	6 7
G2CF=25.6/(RE)+4.756 RETURN	8 14
20 G2CF=1.0/12.0 RETURN	10
30 G2CF=1.858 E-09+LRE)++2-1.878E-05+RE+.0846 RETURN	12
40 GZCF=9.62/(RE)+4.652 RETURN	14 18 15
50 GZCF-11.3/(RE)++.674 Retuan	16 20 17
ENO	10

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	SUP.	- EFN	SOURCE ST	atement	<u>-</u>	[FH(S)	-		03	/04/69
	FUNCTION SUM(F)		~					·····		2 3
	K=2 KK=M-1									5
	KKK=2 Sum=0.0									4 7
	DO 20 I=K,KK,KI SUM=SUM4F(I)						• - ·· •			9
30	GO TC (30,40,50 SUM=SUM+CX/3.C)),K	Company of School of School of School							10 11
	RETURN K=3							, 		13 15
	SUM-SUM-2.0 GO TC 10								. ,	15
50	K=1 KK=H									17
	KKK=F-1 GD TC 45 END		• • • • • • •							18 19 20

									PA\A0\E0		
	TCC.	 .	EFN	SOURCE	STATEM	ENT	IFN(S)				
·	Tellingen errini					<u> </u>	***** ** · ·				
	FUNCTION TECHNO		TO 10							•	
	IFIRE.GT.100.0		in Ti	·							
	TCC=8./RE									2	
	GO TC 100									🤰 .	-
10	IFIRE.GT.4JO.C	GO	TO 20	3						6	
	TGC=4-175/(RE)4	*.86								7	9
	GO TC 100									8	
20	IF(RE-GT-1000-0) GO	TO 3	20						9	
	TCC=.547/(RE)+4			7.5	•					10	1
	GO TC 100									11	
	IFIRE-GT-4JOO.	11 50	TC /	Li)						12	
••				10						13	1
	TCC=.342/(RE)+1			L .							•
	GO TC 10C							•		14	_
	TCC=.064/(RE)+4	25				_	,			15	2
10	RETURN									16	
	END									17	

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IS. ABSTRACT	<u> </u>									

In this volume is presented an analysis of the static and dynamic characteristics of the spiral-grooved journal bearing operating with incompressible lubricant in both laminar and turbulent regimes. Both single film and floating ring bearing configurations are considered. Extensived derign data are presented giving load capacity, attitude angle, bearing torque, bearing flow rate, stiffness and damping coefficients and critical rotor mass for limit of stable operation. In addition, two computer programs accompany the volume, and instructions and listings of the programs are included. These programs may be used to obtain data for cases not covered by the presented design data.

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